# CHAPTER – 3 SQUARES AND SQUARE ROOTS

#### Exercise 3.1

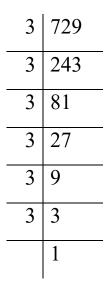
1. Which of the following natural numbers are perfect squares? Give reasons in support of your answer.

- (i) 729
- (ii) **5488**
- (iii) 1024
- (iv) 243

#### Solution:

(i) 729

We know that



It can be written as

 $729 = 3 \times 3 \times 3 \times 3 \times 3 \times 3$ 

Here

729 is the product of pairs of equal prime factors

Therefore, 729 is a perfect square.

(ii) 5488

We know that

2	5488
2	2744
2	1372
2	686
7	343
7	49
7	7
	1

It can be written as

 $5488 = 2 \times 2 \times 2 \times 2 \times 7 \times 7 \times 7$ 

Here

After pairing the same prime factors, one factor 7 is left unpaired.

Therefore, 5488 is not a perfect square.

(iii) 1024 We know that

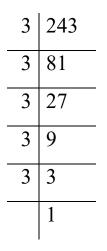
2	1024
2	512
2	256
2	128
2	64
2	32
2	16
2	8
2	4
2	2
	1

Here

After pairing the same prime factors, there is no factor left.

Therefore, 1024 is a perfect square.

(iv) 243



 $243 = 3 \times 3 \times 3 \times 3 \times 3$ 

Here

After pairing the same prime factors, factor 3 is left unpaired.

Therefore, 243 is not a perfect square.

2. Show that each of the following numbers is a perfect square. Also, find the number whose square is the given number.

- (i) 1296
- (ii) 1764
- (iii) **3025**
- (iv) **3969**

#### Solution:

(i) 1296

2	1294
2	648
2	324
2	162
3	81
3	27
3	9
3	3
	1

 $1296 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3$ 

Here

After pairing the same prime factors, no factor is left.

Therefore, 1296 is a perfect square of  $2 \times 2 \times 3 \times 3 = 36$ .

(ii) 1764

2	1764
2	882
7	441
7	63
3	9
3	3
	1

 $1764 = 2 \times 2 \times 3 \times 3 \times 7 \times 7$ 

Here

After pairing the same factors, no factor is left.

Therefore, 1764 is a perfect square of  $2 \times 3 \times 7 = 42$ .

(iii) 3025

We know that

2	3025
2	605
11	121
11	11
	1

It can be written as

 $3025 = 5 \times 5 \times 11 \times 11$ 

Here

After pairing the same prime factors, no factor is left.

Therefore, 3025 is a perfect square of  $5 \times 11 = 55$ .

(iv) 3969

3	3969
3	1323
3	441
3	147
7	49
7	7
	1

 $3969 = 3 \times 3 \times 3 \times 3 \times 7 \times 7$ 

Here

After pairing the same prime factors, no factor is left.

Therefore, 3969 is a perfect square of  $3 \times 3 \times 7 = 63$ .

# **3.** Find the smallest natural number by which 1008 should be multiplied to make it a perfect square.

#### Solution:

2	1008
2	504
2	252
2	126
3	63
3	21
7	7
	1

 $1008 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 7$ 

Here

After pairing the same kind of prime factors, one factor 7 is left.

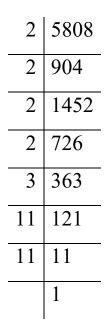
Now multiplying 1008 by 7

We get a perfect square

Therefore, the required smallest number is 7.

# 4. Find the smallest natural number by which 5808 should be divided to make it a perfect square. Also, find the number whose square is the resulting number.

#### Solution:



 $5808 = 2 \times 2 \times 2 \times 2 \times 3 \times 11 \times 11$ 

Here

After pairing the same kind of prime factors, factor 3 is left.

Now dividing the number by 3, we get a perfect square.

Therefore, the square root of the resulting number is  $2 \times 2 \times 11 = 44$ .

## Exercise 3.2

# 1. Write five numbers which you can decide by looking at their one's digit that they are not square numbers. Solution:

We know that

A number which ends with the digits 2, 3, 7 or 8 at its unit places is not a perfect square.

Example – 111, 372, 563, 978, 1282 are not square numbers.

# 2. What will be the unit digit of the squares of the following numbers?

- (i) 951
- (ii) **502**
- (iii) **329**
- (iv) 643
- (v) 5124
- (vi) 7625
- (vii) 68327
- (viii) 95628
- (ix) 99880
- (x) 12796

## Solution:

(i) 951

The unit digit of the square is 1.

(ii) 502

The unit digit of the square is 4.

(iii) 329

The unit digit of the square is 1.

(iv) 643

The unit digit of the square is 9.

(v) 5124

The unit digit of the square is 6.

(vi) 7625

The unit digit of the square is 5.

(vii) 68327

The unit digit of the square is 9.

(viii) 95628

The unit digit of the square is 4.

(ix) 99880

The unit digit of the square is 0.

(x) 12796

The unit digit of the square is 6.

# 3. The following numbers are obviously not perfect. Give reason.

- (i) **56**7
- (ii) 2453
- (iii) **5298**
- (iv) 46292

(v) 74000

#### Solution:

In the given numbers

If the square of a number does not have 2, 3, 7, 8 or 0 as its unit digit, the squares 567, 2453, 5208, 46292 and 74000 cannot be the perfect squares as they have 7, 2, 8, 2 digits at the unit place.

# 4. The square of which of the following numbers would be an odd number or an even number? Why?

(i) 573

(ii) 4096

(iii) **8267** 

(iv) 37916

#### Solution:

We know that

The square of an odd number is odd and a square of an even number is even.

So 573 and 8262 are odd numbers and their squares will be an odd number.

4096 and 37916 are even numbers and their square will also be even number.

5. How many natural numbers lie between square of the following numbers?

(i) 12 and 13

(ii) 90 and 91

#### Solution:

(i) We know that

No. of natural numbers between the squares of 12 and  $13 = (13^2 - 12^2) - 1$ 

By further calculation

=(13+12-1)

So we get

```
= 25 - 1
```

```
= 24
```

(ii) We know that

No. of natural numbers between the squares of 90 and  $91 = (91^2 - 90^2) - 1$ 

By further calculation

$$=(91+90-1)$$

So we get

= 181 - 1

```
= 180
```

## 6. Without adding, find the sum.

(i) 1 + 3 + 5 + 7 + 9 + 11 + 13 + 15

(ii) 1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 + 17 + 19 + 21 + 23 + 25 + 27 + 29

# Solution:

(i) We know that

 $1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 = n^{2}$ Here n = 8 So the sum = 8<sup>2</sup> = 64 (ii) We know that  $1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 + 17 + 19 + 21 + 23 + 25 + 27 + 29 = n^{2}$ Here n = 15 So the sum = 15<sup>2</sup> = 225

#### 7. (i) Express 64 as the sum of 8 odd numbers.

#### (ii) 121 as the sum of 11 odd numbers.

#### Solution:

(i) We know that 64 as the sum of 8 odd numbers =  $8^2 = n^2$ Here n = 8 It can be written as = 1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 (ii) We know that 121 as the sum of 11 odd numbers =  $11^2 = n^2$ Here n = 11 It can be written as

= 1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 + 17 + 19 + 21

#### 8. Express the following as the sum of two consecutive integers.

(i) 19<sup>2</sup>

(ii) 33<sup>2</sup>

(iii) 47<sup>2</sup>

#### Solution:

We know that

 $n^{2} = \frac{(n^{2}-1)}{2} + \frac{(n^{2}+1)}{2}$  is the sum of two consecutive integers when n is odd (i)  $19^{2} = \frac{(19^{2}-1)}{2} + \frac{(19^{2}+1)}{2}$ 

We know that

$$19^2 = 361$$

By further calculation

$$=\frac{(361-1)}{2} + \frac{(361+1)}{2}$$

So we get

= 
$$180 + 181$$
  
(ii)  $33^2 = \frac{(33^2 - 1)}{2} + \frac{(33^2 + 1)}{2}$ 

We know that

 $33^2 = 1089$ 

By further calculation

$$= \frac{(1089 - 1)}{2} + \frac{(1089 + 1)}{1}$$
  
So we get
$$= \frac{1088}{2} + \frac{1090}{2}$$
$$= 544 + 545$$

(iii) 
$$47^2 = \frac{(47^2 - 1)}{2} + \frac{(47^2 + 1)}{2}$$
  
We know that  
 $47^2 = 2209$   
By further calculation  
 $= \frac{(2209 - 1)}{2} + \frac{(2209 + 1)}{1}$   
So we get  
 $= \frac{2208}{2} + \frac{2210}{2}$   
 $= 1104 + 1105$ 

9. Find the squares of the following numbers without actual multiplication:

(i) **31** 

(ii) 42

(iii) 86

(iv) 94

#### Solution:

We know that

 $(a + b)^2 = a^2 + 2ab + b^2$ 

(i) 
$$31^2 = (30 + 1)^2$$

We can write it as

 $= 30^2 + 2 \times 30 \times 1 + 1^2$ 

By further calculation

= 
$$900 + 60 + 1$$
  
=  $961$   
(ii)  $42^2 = (40 + 2)^2$   
We can write it as  
=  $40^2 + 2 \times 40 \times 2 + 2^2$   
By further calculation  
=  $1600 + 160 + 4$   
=  $1764$   
(iii)  $86^2 = (80 + 6)^2$   
We can write it as  
=  $80^2 + 2 \times 80 \times 6 + 6^2$   
By further calculation  
=  $6400 + 960 + 36$   
=  $7396$   
(iv)  $94^2 = (90 + 4)^2$   
We can write it as  
=  $90^2 + 2 \times 90 \times 4 + 4^2$   
By further calculation  
=  $8100 + 720 + 16 = 8836$ 

**10.** Find the squares of the following numbers containing 5 in unit's place:

(i) 45

(ii) **305** 

(iii) **525** 

#### Solution:

(i)  $45^2 = n5^2$ 

It can be written as

= n (n + 1) hundred + 5<sup>2</sup>

Substituting the values

 $= 4 \times 5$  hundred + 25

By further calculation

= 2000 + 25

= 2025

(ii)  $305^2 = (30 \times 31)$  hundred + 25

By further calculation

= 93000 + 25

= 93025

(iii)  $525^2 = (52 \times 53)$  hundred + 25

By further calculation

= 275600 + 25

= 275625

#### 11. Write a Pythagorean triplet whose one number is

(i) **8** 

(ii) 15

(iii) **63** 

(iv) 80

#### Solution:

(i) 8

Take n = 8

So the triplet will be 2n,  $n^2 - 1$ ,  $n^2 + 1$ 

Here

If 2n = 8, then  $n = \frac{8}{2} = 4$ 

Substituting the values

 $n^2 - 1 = 4^2 - 1 = 16 - 1 = 15$ 

 $n^2 + 1 = 4^2 + 1 = 16 + 1 = 17$ 

Therefore, the triplets are 8, 15 and 17.

(ii) 15 Take 2n = 15So  $n = \frac{n}{2}$  is not possible  $n^2 - 1 = 15$ By further calculation  $n^2 = 15 + 1 = 16 = 4^2$  n = 4So we get  $2n = 2 \times 4 = 8$   $n^2 - 1 = 15$  $n^2 + 1 = 4^2 + 1 = 16 + 1 = 17$ 

Therefore, the triplets are 8, 15 and 17. (iii) 63 Take  $n^2 - 1 = 63$ By further calculation  $n^2 = 63 + 1 = 64 = 8^2$ So n = 8Here  $2n = 2 \times 8 = 16$  $n^2 - 1 = 63$  $n^2 + 1 = 8^2 + 1 = 64 + 1 = 65$ Therefore, the triplets are 16, 63 and 65. (iv) 80 Take 2n = 80 $n = \frac{80}{2} = 40$ Here  $n^2 - 1 = 40^2 - 1 = 1600 - 1 = 1599$  $n^2 + 1 = 40^2 + 1 = 1600 + 1 = 1601$ 

Therefore, the triplets are 80, 1599 and 1601.

# 12. Observe the following pattern and find the missing digits: 21<sup>2</sup> = 441 201<sup>2</sup> = 40401 2001<sup>2</sup> = 4004001

 $20001^{2} = 4 - 4 - 1$   $200001^{2} = ----$ Solution:  $21^{2} = 441$   $201^{2} = 40401$   $2001^{2} = 4004001$   $20001^{2} = 400040001$   $200001^{2} = 4000040001$ 

13. Observe the following pattern and find the missing digits:  $9^2 = 81$   $99^2 = 9801$   $999^2 = 998001$   $9999^2 = 99980001$   $99999^2 = 9-8-01$   $99999^2 = 9-0-1$ Solution:  $9^2 = 81$   $99^2 = 9801$   $999^2 = 998001$   $9999^2 = 99980001$  $99999^2 = 9999800001$  14. Observe the following pattern and find the missing digits:

 $7^{2} = 49$   $67^{2} = 4489$   $667^{2} = 444889$   $6667^{2} = 4448889$   $66667^{2} = 4-8-9$   $666667^{2} = 4-8-8-8$ Solution:  $7^{2} = 49$   $67^{2} = 4489$   $667^{2} = 444889$   $6667^{2} = 44448889$   $66667^{2} = 4444488889$  $66667^{2} = 44444888889$ 

#### Exercise 3.3

1. By repeated subtraction of odd numbers starting from 1, find whether the following numbers are perfect squares or not? If the number is a perfect square then find its square root:

- (i) 121
- (ii) 55
- (iii) **36**
- (iv) 90

#### Solution:

(i) We know that

Square root of 121

121 - 1 = 120 120 - 3 = 117 117 - 5 = 112 112 - 7 = 105 105 - 9 = 96 96 - 11 = 85 85 - 13 = 72 72 - 15 = 57 57 - 17 = 40 40 - 19 = 21 21 - 21 = 0

So the square root of 121 is 11

Hence, 121 is a perfect square.

(ii) We know that

Square root of 55

55 - 1 = 54 54 - 3 = 51 51 - 5 = 46 46 - 7 = 39 39 - 9 = 30 30 - 11 = 19 19 - 13 = 66 - 15 = -9 is not possible

Hence, 55 is not a perfect square.

(iii) We know that

Square root of 36

- 36 1 = 35
- 35 3 = 32
- 32 5 = 27
- 27 7 = 20
- 20 9 = 11
- 11 11 = 0

Hence, 36 is a perfect square and its square root is 6.

(iv) We know that

Square root of 90

90 - 1 = 89
89 - 3 = 86
86 - 5 = 81
81 - 7 = 74
74 - 9 = 65
65 - 11 = 54
54 - 13 = 41
41 - 15 = 26
26 - 17 = 9
9 - 19 = -10 which is not possible
Hanaa 00 is not a norfact square

Hence, 90 is not a perfect square.

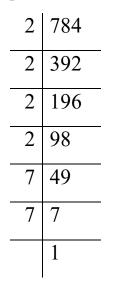
2. Find the square roots of the following numbers by prime factorization method:

- (i) 784
- (ii) 441
- (iii) 1849
- (iv) 4356
- (v) 6241
- (vi) 8836
- (vii) 8281
- (viii) 9025

# Solution:

(i) We know that

Square root of 784



It can be written as

 $\sqrt{784} = \sqrt{2 \times 2 \times 2 \times 2 \times 7 \times 7}$ 

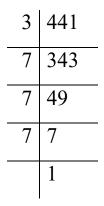
So we get

 $= 2 \times 2 \times 7$ 

= 28

(ii) We know that

Square root of 441



$$\sqrt{441} = \sqrt{3 \times 3 \times 7 \times 7}$$

So we get

 $= 3 \times 7$ 

(iii) We know that

Square root of 1849

It can be written as

$$\sqrt{1849} = \sqrt{43 \times 43} = 43$$

(iv) We know that

Square root of 4356

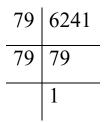
$$\sqrt{4356} = \sqrt{2 \times 2 \times 3 \times 3 \times 11 \times 11}$$

So we get

$$= 2 \times 3 \times 11$$

(v) We know that

Square root of 6241



It can be written as

 $\sqrt{6241} = \sqrt{79 \times 79} = 79$ 

(vi) We know that

Square root of 8836

It can be written as

$$\sqrt{8836} = \sqrt{2 \times 2 \times 47 \times 47}$$

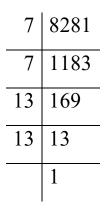
So we get

 $= 2 \times 47$ 

= 94

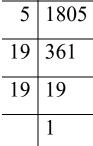
(vii) We know that

Square root of 8281



It can be written as

 $\sqrt{8281} = \sqrt{7 \times 7 \times 13 \times 13}$ So we get = 7 × 13 = 91 (viii) We know that Square root of 9025 <u>5 9025</u>



 $\sqrt{9025} = \sqrt{5 \times 5 \times 19 \times 19}$ So we get  $= 5 \times 19$ = 95

**3.** Find the square roots of the following numbers by prime factorization method:

(i)  $9\frac{67}{121}$ (ii)  $17\frac{13}{36}$ 

(iii) 1.96

(iv) 0.0064

Solution:

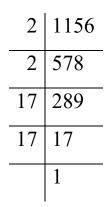
(i)  $9\frac{67}{121} = \frac{(9 \times 121 + 67)}{121}$ 

By further calculation

$$=\frac{(1089+67)}{121}$$
$$=\frac{1156}{121}$$

By squaring we get

$$\sqrt{\frac{1156}{121}} = \frac{\sqrt{1156}}{\sqrt{121}}$$



$$= \frac{\sqrt{2 \times 2 \times 17 \times 17}}{\sqrt{11 \times 11}}$$
  
So we get
$$= \frac{(2 \times 17)}{11}$$
$$= \frac{34}{11}$$
$$= 3\frac{1}{11}$$

(ii)  $17\frac{13}{36} = \frac{(17 \times 36 + 13)}{36}$ 

By further calculation

$$=\frac{(612+13)}{36} = \frac{625}{36}$$

By squaring we get

$$\sqrt{\frac{625}{36}} = \frac{\sqrt{625}}{\sqrt{36}}$$

# We know that

5	625		2	36
5	125	-	2	18
5	25	-	3	9
5	5		3	3
	1			1

#### It can be written as

 $= \frac{\sqrt{5 \times 5 \times 5 \times 5}}{\sqrt{2 \times 2 \times 3 \times 3}}$ So we get $= \frac{(5 \times 5)}{(2 \times 3)}$  $= \frac{25}{6}$  $= 4\frac{1}{6}$ (iii) 1.96 =  $\frac{196}{100}$ 

By squaring we get

196	_	$\sqrt{196}$
 100	_	$\sqrt{100}$

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	2	196	2	100
	2	98	2	50
7 7 5 5	7	49	5	25
	7	7	5	5
		1		1

\_

$$= \frac{\sqrt{2 \times 2 \times 7 \times 7}}{\sqrt{2 \times 2 \times 5 \times 5}}$$
  
So we get  
$$= \frac{(2 \times 7)}{(2 \times 5)}$$
  
$$= \frac{14}{10}$$
  
$$= 1.4$$
  
(iv) 0.0064 =  $\frac{64}{10000}$ 

By squaring we get

$$\sqrt{\frac{64}{10000}} = \frac{\sqrt{64}}{\sqrt{10000}}$$

2	10000
2	5000
2	2500
2	12500
5	625
5	125
5	25
5	5
	1

 $= \frac{\sqrt{2 \times 2 \times 2 \times 2 \times 2 \times 2}}{\sqrt{2 \times 2 \times 2 \times 2 \times 5 \times 5 \times 5 \times 5}}$ So we get $= \frac{(2 \times 2 \times 2)}{(2 \times 2 \times 5 \times 5)}$  $= \frac{8}{100}$ = 0.08

4. For each of the following numbers, find the smallest natural number by which it should be multiplied so as to get a perfect square. Also, find the square root of the square number so obtained:

(i) **588** 

(ii) 720

(iii) 2178

(iv) 3042

(v) 6300

#### Solution:

(i)  $588 = 2 \times 2 \times 3 \times 7 \times 7$ 

We know that

2	588
2	294
3	147
7	49
7	7
	1

By pairing the same kind of factors, one factor 3 is left unpaired.

So to make it a pair we must multiply it by 3

Required least number = 3

Square root of  $588 \times 3 = 1764$ 

Here

 $2 \times 3 \times 7 = 42$ 

(ii)  $720 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 5$ 

2	720
2	360
2	180
2	90
3	45
3	15
5	5
	1

By pairing the same kind of factors, one factor 5 is left unpaired.

So to make it a pair we must multiply it by 5

Required least number = 5

Square root of  $720 \times 5 = 3600$ 

Here

 $2 \times 2 \times 3 \times 5 = 60$ 

(iii)  $2178 = 2 \times 3 \times 3 \times 11 \times 11$ 

2	2178
3	1089
3	363
11	121
11	11
	1

By pairing the same kind of factors, one factor 2 is left unpaired.

So to make it a pair we must multiply it by 2

Required least number = 2

Square root of  $2178 \times 2 = 4356$ 

Here

- $2 \times 3 \times 11 = 66$
- (iv)  $3042 = 2 \times 3 \times 3 \times 13 \times 13$

We know that

2	3042
3	1521
3	507
13	169
13	13
	1

By pairing the same kind of factors, one factor 2 is left unpaired

So to make it a pair we must multiply it by 2

Required least number = 2

Square root of  $3042 \times 2 = 6084$ 

Here

 $2 \times 3 \times 13 = 78$ 

(v)  $6300 = 2 \times 2 \times 3 \times 3 \times 5 \times 5 \times 7$ 

We know that

2	6300
2	3150
3	1575
3	525
3	175
5	35
7	7
	1

By pairing the same kind of factors, one factor 7 is left unpaired

So to make it a pair we must multiply it by 7

Required least number = 7

Square root of  $6300 \times 7 = 44100$ 

Here

 $2 \times 3 \times 5 \times 7 = 210$ 

5. For each of the following numbers, find the smallest natural number by which it should be divided so that this quotient is a perfect square. Also, find the square root of the square number so obtained:

- (i) 1872
- (ii) 2592
- (iii) **3380**
- (iv) 16224
- (v) 61347

#### Solution:

(i)  $1872 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 13$ 

It can be written as

2	1872
2	936
2	468
2	234
3	117
3	39
13	13
	1

By pairing the same kind of factors, one factor 13 is left unpaired

Required least number = 13

The number 1872 should be divided by 13 so that the resultant number will be a perfect square

Resultant number =  $1872 \div 13 = 144$ 

Square root =  $2 \times 2 \times 3 = 12$ 

(ii)  $2592 = 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3$ 

2	2592
2	1296
2	648
2	324
2	162
3	81
3	27
3	9
3	3
	1

By pairing the same kind of factors, one factor 2 is left unpaired

Required least number = 2

The number 2592 should be divided by 2 so that the resultant number will be a perfect square

Resultant number =  $2592 \div 2 = 1296$ 

Square root =  $2 \times 2 \times 3 \times 3 = 36$ 

(iii)  $3380 = 2 \times 2 \times 5 \times 13 \times 13$ 

2	3380
2	1690
5	845
13	169
13	13
	1

By pairing the same kind of factors, one factor 5 is left unpaired

Required least number = 5

The number 3380 should be divided by 5 so that the resultant number will be a perfect square

Resultant number =  $3380 \div 5 = 676$ 

Square root =  $2 \times 13 = 26$ 

(iv)  $16224 = 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 13 \times 13$ 

2	16224
2	8112
2	4056
2	2028
2	1014
3	507
13	169
13	13
	1

By pairing the same kind of factors, two factors 2 and 3 is left unpaired

Required least number  $= 2 \times 3 = 6$ 

The number 16224 should be divided by 6 so that the resultant number will be a perfect square

Resultant number =  $16224 \div 6 = 2704$ 

Square root =  $2 \times 2 \times 13 = 52$ 

(v)  $61347 = 3 \times 11 \times 11 \times 13 \times 13$ 

It can be written as

3	61347
11	20449
11	1859
13	169
13	13
	1

By pairing the same kind of factors, one factor 3 is left unpaired

Required least number = 3

The number 61347 should be divided by 3 so that the resultant number will be a perfect square

Resultant number =  $61347 \div 3 = 20449$ 

Square root =  $11 \times 13 = 143$ 

6. Find the smallest square number that is divisible by each of the following numbers:

(i) 3, 6, 10, 15

(ii) 6, 9, 27, 36

(iii) 4, 7, 8, 16

#### Solution:

(i) 3, 6, 10, 15

Number which is divisible by

3, 6, 10, 15 = LCM of 3, 6, 10, 15

It can be written as

2	3, 6, 10, 15
3	3, 3, 5, 15
5	1, 1, 5, 5
	1, 1, 1, 1,

So we get

 $= 2 \times 3 \times 5$ 

= 30

(ii) 6, 9, 27, 36

Number which is divisible by

6, 9, 27, 36 = LCM of 6, 9, 27, 36

So we get  $= 3 \times 3 \times 2 \times 2 \times 3$  = 108Here the smallest square  $= 108 \times 3$  = 324

(iii) 4, 7, 8, 16

Number which is divisible by

4, 7, 8, 16 = LCM of 4, 7, 8, 16

It can be written as

2	4, 7, 8, 16
	2, 7, 4, 8
2	1, 7, 2, 4
	1, 7, 1, 2,

So we get

 $= 2 \times 2 \times 2 \times 2 \times 7$ 

= 112

Here the smallest square

= 112 × 7

= 784

## 7. 4225 plants are to be planted in a garden in such a way that each row contains as many plants as the number of rows. Find the number of rows and the number of plants in each row.

# Solution:

It is given that

Total number of plants = 4225

Here

Number of rows = Number of plant in each row

So the number of rows = square root of 4225

It can be written as

5	4225
5	845
13	169
13	13
	1

So we get

$$= \sqrt{5 \times 5 \times 13 \times 13}$$
$$= 5 \times 13$$
$$= 65$$

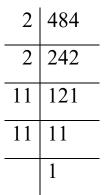
Hence, the number of rows is 65 and the number of plants in each row is 65.

# 8. The area of rectangle is 1936 sq. m. If the length of the rectangle is 4 times its breadth, find the dimensions of the rectangle.

## Solution:

It is given that Area of rectangle = 1936 sq. m Take breadth = x m Length = 4x m So we get  $4x^2 = 1936$ By further calculation  $x^2 = \frac{1936}{4} = 484$ 

We know that



It can be written as

 $x = \sqrt{484} = \sqrt{2 \times 2 \times 11 \times 11}$ 

By further calculation

 $= 2 \times 11$ 

= 22

Here

Length =  $4x = 4 \times 22 = 88$  m Breadth = x = 22 m

9. In a school a P.T. teacher wants to arrange 2000 students in the form of rows and columns for P.T. display. If the number of rows is equal to number of columns and 64 students could not be accommodated in this arrangement. Find the number of rows.

#### Solution:

It is given that

Total number of students in a school = 2000

The P.T. teacher arranges in such a way that

No. of rows = no. of students in each row

So 64 students are left

Required number of students = 2000 - 64 = 1936

No. of rows =  $\sqrt{1936}$ 

We know that

2	1936
2	968
2	484
2	242
11	121
11	11
	1

It can be written as

 $= \sqrt{2 \times 2 \times 2 \times 2 \times 11 \times 11}$ By further calculation  $= 2 \times 2 \times 11$ = 44

10. In a school, the students of class VIII collected ₹2304 for a picnic. Each student contributed as many rupees as the number of students in the class. Find the number of students in the class.

#### Solution:

It is given that

Amount collected for picnic = ₹2304

We know that

No. of students = no. of rupees contributed by each student =  $\sqrt{2304}$ 

Here

2	2304
2	1152
2	576
2	288
2	144
2	72
2	36
2	18
3	9
3	3
	1

It can be written as

 $= \sqrt{2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3}$ 

By further calculation

 $= 2 \times 2 \times 2 \times 2 \times 34 = 48$ 

Therefore, the number of students in class VIII is 4811.

# 11. The product of two numbers is 7260. If one number is 15 times the other number, find the numbers.

#### Solution:

It is given that

Product of two numbers = 7260

Consider one number = x

Second number = 15x

It can be written as

 $15x \times x = 7260$  $15x^2 = 7260$ 

By further calculation

 $x^{2} = \frac{7260}{15} = 484$   $x = \sqrt{484} = \sqrt{2 \times 2 \times 11 \times 11}$ So we get  $= 2 \times 11$  = 22Here
One number = 22

Second number =  $22 \times 15 = 330$ 

# 12. Find three positive numbers in the ratio 2: 3: 5, the sum of whose squares is 950.

#### Solution:

It is given that

Ratio of three positive numbers = 2: 3: 5

Sum of their squares = 950

Consider

First number = 2x

Second number = 3x

Third number = 5x It can be written as  $(2x)^{2+} (3x)^{2} + (5x)^{2} = 950$ By further calculation  $4x^{2} + 9x^{2} + 25x^{2} = 950$   $38x^{2} = 950$ So we get  $x^{2} = \frac{950}{38} = 25$   $x = \sqrt{25} = 5$ Here First number =  $2 \times 5 = 10$ Second number =  $3 \times 5 = 15$ Third number =  $5 \times 5 = 25$ 

13. The perimeter of two squares is 60 metres and 144 metres respectively. Find the perimeter of another square equal in area to the sum of the first two squares.

#### Solution:

It is given that

Perimeter of first square = 60 m

Side  $=\frac{60}{4} = 15$  m

Perimeter of second square = 144 m

Side 
$$=\frac{144}{4} = 36$$
 m

So the sum of perimeters of two squares = 60 + 144 = 204 m Sum of areas of these two squares =  $15^2 + 36^2$ 

= 225 + 1296

 $= 1521 \text{ m}^2$ 

Here

Area of third square =  $1521 \text{ m}^2$ 

We know that

3	1521
3	507
13	169
13	13
	1

So we get

Side =  $\sqrt{\text{Area}} = \sqrt{1521}$ It can be written as =  $\sqrt{3 \times 3 \times 13 \times 13}$ =  $3 \times 13$ = 39 mHere Perimeter =  $4 \times \text{side}$ Substituting the values =  $4 \times 39$ = 156 m

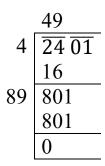
#### Exercise 3.4

- 1. Find the square root of each of the following by division method:
- (i) 2401
- (ii) 4489
- (iii) 106929
- (iv) 167281
- (v) 53824
- (vi) 213444

#### Solution:

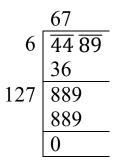
(i)  $\sqrt{2401} = 49$ 

By division method



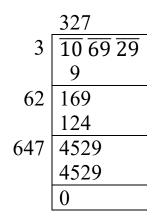
(ii)  $\sqrt{4489} = 67$ 

By division method



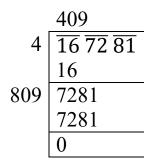
(iii) 
$$\sqrt{106929} = 327$$

By division method



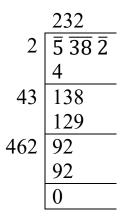
(iv)  $\sqrt{167281} = 409$ 

By division method



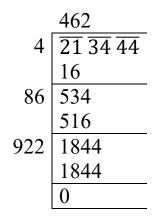
(v)  $\sqrt{53824} = 232$ 

By division method



(vi)  $\sqrt{213444} = 462$ 

By division method



2. Find the number of digits in the square root of each of the following (without any calculation):

(i) **8**1

- (ii) 169
- (iii) **4761**
- (iv) 27889

(v) 525625

Solution:

(i) 81

We know that

In 81, a group of two's is 1

Therefore, its square root has one digit.

(ii) 169

We know that

In 169, group of two's are 2

Therefore, its square root has two digits.

(iii) 4761

We know that

In 4761, group of two's are 2

Therefore, its square root has two digits.

(iv) 27889

We know that

In 27889, groups of two's are 3

Therefore, its square root has three digits.

(v) 525625

We know that

In 525625, groups of two's are 3

Therefore, its square root has three digits.

# **3.** Find the square root of the following decimal numbers by division method:

(i) **51.84** 

(ii) 42.25

(iii) **18.4041** 

(iv) 5.774409

#### Solution:

(i)  $\sqrt{51.84} = 7.2$ 

By division method

$$\begin{array}{r}
7.2 \\
7 \overline{42.84} \\
49 \\
142 284 \\
284 \\
0
\end{array}$$

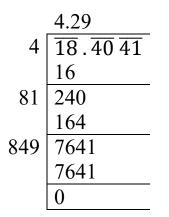
(ii) 
$$\sqrt{42.25} = 6.5$$

By division method

$$\begin{array}{r}
6.5 \\
6 \overline{42.25} \\
36 \\
125 \\
625 \\
0 \\
\end{array}$$

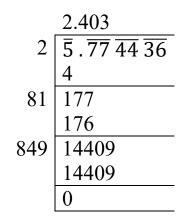
(iii)  $\sqrt{18.4041} = 4.29$ 

By division method



(iv)  $\sqrt{5.774409} = 2.403$ 

By division method



4. Find the square root of the following numbers correct to two decimal places:

(i) 645.8

(ii) 107.45

(iii) **5.462** 

(iv) 2

(v) 3

Solution:

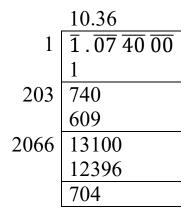
(i)  $\sqrt{645.8} = 25.41$ 

It can be written as

	25.41
2	$\overline{6}$ . $\overline{45}$ $\overline{80}$ $\overline{00}$
	4
45	245 225
	225
504	2080
	2016
5081	6400
	5081
	1319

(ii)  $\sqrt{107.45} = 10.36$ 

It can be written as

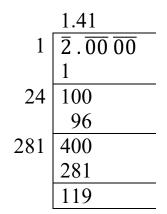


(iii)  $\sqrt{5.462} = 2.337 = 2.34$ 

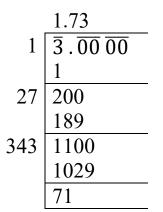
	2.337
2	$\overline{5}$ . $\overline{46}$ $\overline{20}$ $\overline{00}$
	4
43	146
	129
463	1720
	1389
4667	33100
	32669
	431

(iv) 
$$\sqrt{2} = 1.41$$

It can be written as



(v) 
$$\sqrt{3} = 1.73$$



#### 5. Find the square root of the following fractions by division method:

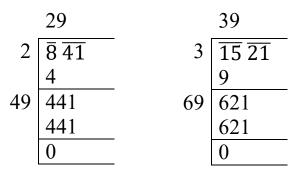
(i)  $\frac{841}{1521}$ (ii)  $8\frac{257}{529}$ (iii)  $16\frac{169}{441}$ 

Solution:

(i) 
$$\frac{841}{1521}$$

By squaring

 $\sqrt{\frac{841}{1521}} = \frac{\sqrt{841}}{\sqrt{1521}} = \frac{29}{39}$ 



(ii) 
$$8\frac{257}{529}$$

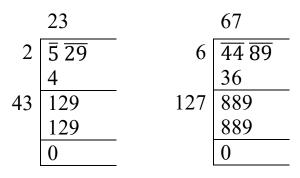
By squaring

$$\sqrt{8\frac{257}{529}} = \sqrt{\frac{4232 + 257}{529}} = \sqrt{\frac{4489}{529}}$$

So we get

$$=\frac{67}{23}=2\frac{21}{23}$$

It can be written as



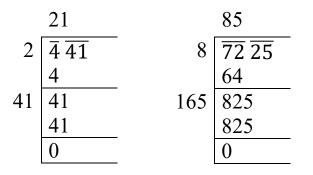
(iii) 
$$16\frac{169}{441}$$

By squaring

$$\sqrt{16\frac{169}{441}} = \sqrt{\frac{7056+169}{441}} = \sqrt{\frac{7225}{441}}$$

So we get

$$= \frac{\sqrt{7225}}{\sqrt{441}}$$
$$= \frac{85}{21} = 4\frac{1}{21}$$



6. Find the least number which must be subtracted from each of the following numbers to make them a perfect square. Also find the square root of the perfect square number so obtained:

(i) 2000

(ii) 984

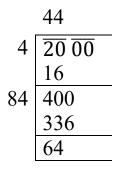
(iii) **8934** 

(iv) 11021

#### Solution:

(i) 2000

We know that



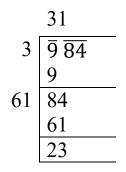
By taking square root, 64 is left as remainder

Subtracting 64 from 2000

We get 1936 which is a perfect square and its square root is 44.

(ii) 984

We know that



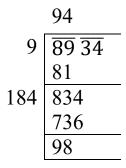
By taking square root, 23 is left as remainder

Subtracting 23 from 984

We get 961 which is a perfect square and its square root is 31.

(iii) 8934

We know that



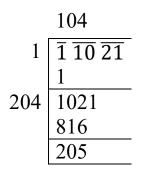
By taking square root, 98 is left as remainder

Subtracting 98 from 894

We get 8934 - 98 = 8836 which is a perfect square and its square root is 94.

(iv) 11021

We know that



By taking square root, 205 is left as remainder

Subtracting 205 from 11021

We get 11021 - 205 = 10816 which is a perfect square and its square root is 104.

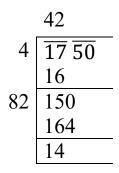
## 7. Find the least number which must be added to each of the following numbers to make them a perfect square. Also, find the square root of the perfect square number so obtained:

- (i) 1750
- (ii) 6412
- (iii) **6598**
- (iv) 8000

#### Solution:

(i) 1750

We know that



By taking square root

 $41^2$  is less than 1750

So by taking 42<sup>2</sup>

164 - 150 = 14 less

Adding 14 we get a square of 42 which is 1764.

(ii) 6412

We know that

$$\begin{array}{r}
81\\
8\overline{64}\overline{12}\\
64\\
161\\
12\\
161\\
149\\
\end{array}$$

By taking square root

 $80^2$  is less than 6412

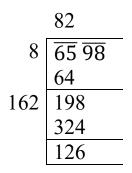
So by taking 81<sup>2</sup>

161 - 12 = 14 less

Adding 149 we get a square of 81 which is 6561.

(iii) 6598

We know that



By taking square root

 $81^2$  is less than 6598

So by taking  $82^2$ 

324 - 198 = 126 less

Adding 126 we get a square of 82 which is 6724.

(iv) 8000

We know that

By taking square root

 $89^2$  is less than 8000

So by taking  $90^2$ 

8100 - 8000 = 100 less

Adding 100 we get a square of 90 which is 8100.

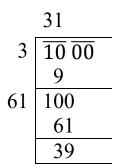
# 8. Find the smallest four-digit number which is a perfect square.

#### Solution:

It is given that

Smallest four - digit number = 1000

We know that



By taking square root, we find that 39 is left.

If we subtract any number from 1000 we get 3 digit number

Take  $32^2 = 1024$ 

Here 1024 - 1000 = 24 is to be added to get a perfect square of least 4 digit number

Therefore, the required 4 digit smallest number is 1024.

## 9. Find the greatest number of six digits which is a perfect square.

## Solution:

It is given that

Greatest six digit number = 999999

We know that

999	
9	<u>99</u> 99999
	81
189	1899
	1701
1989	19899
	17901
	1998

By taking square root, we find that 1998 is left

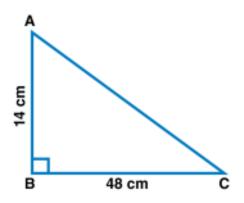
If we subtract 1998 from 999999 we get 998001 which is a perfect square.

Therefore, required six digit greatest number is 998001.

10. In a right triangle ABC,  $\angle B = 90^{\circ}$ . (i) If AB = 14 cm, BC = 48 cm, find AC. (ii) If AC = 37 cm, BC = 35 cm, find AB. Solution: (i) In a right angled triangle ABC

It is given that

AB = 14 cm and BC = 48 cm



Using Pythagoras theorem

 $AC^2 = AB^2 + BC^2$ 

Substituting the values

 $= 14^2 + 48^2$ 

By further calculation

$$= 196 + 2304$$

= 2500

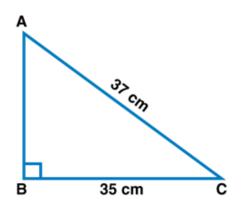
So we get

$$AC = \sqrt{2500} = 50 \text{ cm}$$

$$5 \begin{array}{r} 50 \\ \hline 25 \\ \hline 0 \end{array}$$

(ii) In right triangle ABC

 $B = 90^{\circ}$ , AC = 37 cm, BC = 35 cm



Using Pythagoras Theorem

 $AC^2 = AB^2 + BC^2$ 

Substituting the values

 $37^2 = AB^2 + 352$ 

By further calculation

 $1369 = AB^2 + 1225$  $AB^2 = 1369 - 1225 = 144$ 

So we get

$$AB = \sqrt{144} = 12 \text{ cm}$$
$$12$$
$$1 \overline{144}$$
$$1$$

$$\begin{array}{c|c} 22 & 44 \\ \hline 44 \\ \hline 0 \end{array}$$

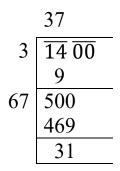
11. A gardener has 1400 plants. He wants to plant these in such a way that the number of rows and number of columns remains same. Find the minimum number of plants he needs more for this.

Solution:

It is given that

Total number of plants = 1400

We know that



Here

Number of columns = Number of rows

By taking the square root of 1400

 $37^2 < 1400$ 

So take  $38^2 = 1444$ 

We need 1444 - 1400 = 44 plants more

Therefore, the minimum number of plants he needs more for this is 44.

# 12. There are 1000 children in a school. For a P.T. drill they have to stand in such a way that the number of rows is equal to number of columns. How many children would be left out in this arrangement?

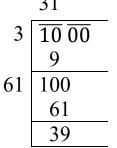
#### Solution:

It is given that

No. of total children in a school = 1000

For a P.T. drill, children have to stand in such a way that

No. of rows = No. of columns Take the square root of 1000 39 is left as remainder Left out children = 39 31



Hence, 39 children would be left out in this arrangement.

# 13. Amit walks 16 m south from his house and turns east to walk 63 m to reach his friend's house. While returning, he walks diagonally from his friend's house to reach back to his house. What distance did he walk while returning?

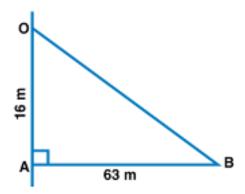
#### Solution:

It is given that

Amit walks 16 m south from his house and turns east to walk 63 m to reach his friend's house

Consider O as the house and A and B as the places

OA = 16 m, AO = 63 m



Using Pythagoras theorem

 $OB^2 = OA^2 + AB^2$ 

Substituting the values

 $= 16^2 + 63^2$ 

By further calculation

= 256 + 3969

= 4225

So we get

$$OB = \sqrt{4225} = 65$$

$$6 \overline{4225}$$

$$36$$

$$125 \overline{625}$$

$$0$$

Therefore, Amit has to walk 65 m to reach his house.

14. A ladder 6 m long leaned against a wall. The ladder reaches the wall to a height of 4.8 m. Find the distance between the wall and the foot of the ladder.

#### Solution:

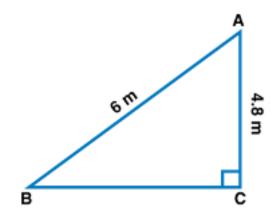
It is given that

Length of ladder = 6 m

Ladder reaches the wall to a height of 4.8 m

Consider AB as the ladder and AC as the height of the wall

AB = 6 m and AC = 4.8 m



Distance between the foot of ladder and wall is BC

Using Pythagoras theorem,

 $AB^2 = AC^2 + BC^2$ 

Substituting the values

$$6^2 = 4.8^2 + BC^2$$

By further calculation

 $BC^2 = 6^2 - 4.8^2$ 

 $BC^2 = 36 - 23.04 = 12.96$ 

So we get

 $BC = \sqrt{12.96} = 3.6 \text{ m}$ 

Hence, the distance between the wall and the foot of the ladder is 3.6 m.

#### **Mental Maths**

**Question 1: Fill in the blanks:** 

(i) A number ending in ..... is never a perfect square.

(ii) On combining two consecutive triangular number, we get a .....

(iii) If a number has digits ..... in the unit's place, then its square ends in 1.

(iv) Sum of first 10 odd natural numbers is ......

(v) Number of non-square numbers between 11<sup>2</sup> and 12<sup>2</sup> is .....

(vi) Number of zeros in the end of the square of 400 is .....

(vii) Square of any .....number can be expressed as the sum of two consecutive natural numbers.

(viii)For a natural number m > 1,  $(2m, m^2 - 1, m^2 + 1)$  is called .....

#### Solution:

(i) A number ending in 2,3,7 and 8 is never a perfect square.

(ii) On combining two consecutive triangular number, we get a square number.

(iii) If a number has digits 1 or 9 in the unit's place, then its square ends in 1.

(iv) Sum of first 10 odd natural numbers is  $(10)^2 = 100$ .

(v) Number of non-square numbers between  $11^2$  and  $12^2$  is  $(12^2 - 11^2) - 1 = 12 + 11 - 1 = 22$ .

(vi) Number of zeros in the end of the square of 400 is 0000 (four zeros).

(vii) Square of any odd number can be expressed as the sum of two consecutive natural numbers.

(viii) For a natural number m > 1,  $(2m, m^2 - 1, m^2 + 1)$  is called Pythagorean triplet.

Question 2: State whether the following statements are true (T) or false (F):

(i) All natural numbers are not perfect squares.

(ii) A perfect square can never be expressed as the product of pairs of equal prime factors.

(iii) A number having 2,3,7 or 8 at its unit place is never a square number.

(iv) A number having 0, 1, 4, 5, 6 or 9 at its unit place is always a square number.

(v) A number ending in an even number of zeros is always a perfect square.

(vi) Square of an odd number is always an odd number.

(vii) 1, 3, 6, 10, 15, are called triangular numbers.

(viii)There are 2n non-square numbers between the squares of consecutive numbers n and (n + 1).

#### (ix) (4, 6, 8) is a Pythagorean triplet.

#### Solution:

(i) All natural numbers are not perfect squares. (True)

(ii) A perfect square can never be expressed as

the product of pairs of equal prime factors. (True)

(iii) A number having 2, 3, 7 or 8 at its unit place is never a square number. (Time)

(iv) A number having 0, 1, 4, 5, 6 or 9 at its unit place is always a square number. (False)

Correct:

As 24, 14, 34, 26, 19, 50, 61, 35, etc are not a perfect square

(v) A number ending in an even number of zeros is always a perfect square. (False)

Correct:

As 200, 500, 8000, etc. are not perfect squares. (vi) Square of an odd number is always an odd number. (True) (vii) 1, 3, 6, 10, 15, are called triangular numbers. (True) (viii) There are 2n non-square numbers between the squares of consecutive numbers n and (n + 1). (True) (ix) (4, 6, 8) is a Pythagorean triplet. (False) Correct: As  $4^2 + 6^2 \neq 8^2 \Rightarrow 16 + 36 \neq 64$  $\Rightarrow 52 \neq 64$ 

#### **Multiple Choice Questions**

Choose the correct answer from the given four options (3 to 15):

Question 3: How many natural numbers lie between  $25^2$  and  $26^2$ ? (a) 49 (b) 50 (c) 51 (d) 52 Solution: Natural numbers between  $25^2$  and  $26^2$ 25 + 26 - 1 = 50 (b) Question 4: Square of an even number is always (a) even

(a) even
(b) odd
(c) even or odd
(d) none of these
Solution:

Square of an even number is always even. (a)

Question 5: 1+3+5+7+... up to n terms is equal to (a)  $n^2 - 1$ (b)  $(n + 1)^2$ (c)  $n^2 + 1$ (d)  $n^2$ Solution: 1+3+5+7+... Up to n terms is equal to  $n^2 + 1$  (c)

Question 6.  $\sqrt{\{208\} + \sqrt{\{2304\}}}$  is equal to (a) 18 (b) 16 (c) 14 (d) 22 Solution:  $\sqrt{208 + \sqrt{2304}}$ 

$$= \sqrt{208 + 48}$$
  
=  $\sqrt{256} = 16$  (b)  
$$1 \overline{2 \overline{56}}$$
  
$$1 \overline{26} \overline{156}$$
  
$$1 \overline{156}$$
  
$$0$$

$$\begin{array}{r}
 48 \\
 4 \overline{)23 04} \\
 16 \\
 66 \overline{)704} \\
 \overline{)704} \\
 0 \\
\end{array}$$

Question 7.  $\sqrt{0.0016}$  is equal to (a) 0.04 (b) 0.004 (c) 0.4 (d) none of these Solution:  $\sqrt{0.0016} = 0.04$  $04 \overline{0.0016} \overline{16}$ 16

0

Question 8: The smallest number by which 75 should be divided to make it a perfect square is

(a) 1
(b) 2
(c) 3
(d) 4
Solution:
75 = 3 × 5 × 5
Factor 3 is unpaired
∴ By dividing 75 by 3, we get a perfect square of 5.

Question 9	$0. \sqrt{3\frac{6}{25}} \text{ is equal to}$
$(a)^{\frac{5}{-}}$	(b) $\frac{4}{-}$

(a) 
$$\frac{9}{5}$$
 (b)  $\frac{5}{5}$   
(c)  $\frac{9}{5}$  (d)  $\frac{5}{4}$ 

Solution:

$$\sqrt{3\frac{6}{25}} = \sqrt{\frac{81}{25}} = \sqrt{\frac{81}{25}}$$
$$= \frac{9}{5} = 1\frac{4}{5}$$
(c)

### Question 10: The smallest number by which 162 should be multiplied to make it a perfect square is

- (a) 4
- **(b) 3**
- (c) 2
- (d) 1

#### Solution:

 $162 = 2 \times 3 \times 3 \times 3 \times 3$ 

For 2 is left unpairs. So, by multiplying 162 by 2,

we get a perfect square.

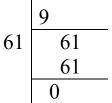
 $\therefore$  Required least number to be multiplied = 2 (c)

Question 11: If the area of a square field is 961 unit<sup>2</sup>, then the length of its side is

- (a) 29 units
- (b) 41 units
- (c) 31 units
- (d) 39 units

#### Solution:

Area of a square = 961 unit<sup>2</sup>  $\therefore$  It's side =  $\sqrt{961}$  unit = 31 unit (c)  $3\frac{31}{961}$ 



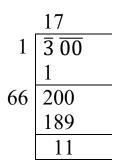
Question 12: The smallest number that should be subtracted from 300 to make it a perfect square is

- (a) 11
- (b) 12
- (c) 13
- (d) 14

#### Solution:

#### 300

Taking the square root of 300, we see that 11 is left unpaired.  $\therefore$  11 be subtracted. (a)



## Question 13: If one number of Pythagoream triplet is 6, then the triplet is (a) (4, 5, 6)

(b) (5, 6, 7) (c) (6, 7, 8) (d) (6, 8, 10) Solution: One number of a Pythagorean triplet is 6 Let  $2n = 6 \Rightarrow n = 3$  $n^2 - 1 = 3^2 - 1 = 8$  and  $n^2 + 1 = 3^2 + 1 = 10$ ∴ Triplet is (6, 8, 10) (d)

#### Question 14: *n*<sup>th</sup> triangular number is

(a)  $\frac{n(n+1)}{2}$ (b)  $\frac{n(n-1)}{2}$  $(c) \frac{(n-1)(n+1)}{2}$ 

(d) none of these

#### Solution:

nth triangular number =  $\frac{n(n+1)}{2}$  (a)

#### **Value Based Questions**

Question 1: In a school, students of class VIII collected ₹9216 to give a donation to an NGO working for the education of poor children. If each student donated as many rupees as the number of students in class VIII. Find the number of students in class VIII.

Why should we donate money for the education of poor children? What values are being promoted?

#### Solution:

Amount collected by students =  $\gtrless$  9216 and each donated amount equal to the number of students

Number of students =  $\sqrt{9261} = ₹96$ 

$$\begin{array}{r}
96 \\
9 \overline{92 \, \overline{16}} \\
81 \\
186 \overline{1116} \\
1116 \\
0
\end{array}$$

Donation to an NGO, who is working for the education of poor children is a noble cause.

Question 2: A person wants to plant 2704 medicinal plants with a board depicting the diseases in which that can be used. He planted these in the form of rows. If each row contains as many plants as the number of rows, then find the number of rows. Why should we plant medicinal plants? What values are being promoted?

#### Solution:

Total number of plants = 2704

These are planted in such a way that

Number of rows = number of plants in each row

$$\therefore$$
 Number of rows =  $\sqrt{2704}$ 

$$52 \\ 5 \overline{27 \ 04} \\ 25 \\ 102 \ 204 \\ 204 \\ 0 \\ 0 \\ 0 \\ 102 \ 0 \\ 102 \\$$

Medicinal plants = 52

These plants give us many kinds of medicines

Which are useful for different diseases.

So, it is a noble cause for society.

#### Higher Order Thinking Skills (Hots)

Question 1: A square field is to be ploughed. Ramu get it ploughed in ₹34560 at the rate of ₹15 per sq. m. Find the length of side of square field.

#### Solution:

Total expenditure for ploughing the field = ₹34560 The rate of ploughing = ₹15 per sq. m ∴ Total area of the square field =  $\frac{34560}{15}$ = 2304 m<sup>2</sup> Side of the square field =  $\sqrt{2304}$  m = 48 m  $4 \frac{48}{2304}$   $\frac{48}{16}$  $88 \frac{704}{704}$ 

Question 2: Lalit has some chocolates. He distributed these chocolates among 13 children in such a way that he gave one chocolate to first child, 3 chocolates to second child, 5 chocolates to third and so on. Find the number of chocolates Lalit had.

#### Solution:

Number of children = 13

 $\frac{704}{0}$ 

Lalit gave chocolates to the children in such a way that he gives one chocolate to first child, 3 chocolates to the second child 5 chocolates to a third child and so on

 $\therefore$  1 + 3 + 5 + up to 13 terms

 $(: 1 + 3 + 5 + 7 + \dots n \text{ terms} = n^2)$ 

#### **Check Your Progress**

Question 1: Show that 1089 is a perfect square. Also find the number whose square is 1089.

#### Solution:

 $1089 = 3 \times 3 \times 11 \times 11$ 3 | 1089

3	363
11	121
11	11
	1

• Prime factors are in pairs and no factor is left.

: It is a perfect square and its square root =  $3 \times 11 = 33$ 

## Question 2: Find the smallest number which should be multiplied by 3675 to make it a perfect square. Also find the square root of this perfect square.

#### Solution:

3675 Factorising, we get

 $3675 = 3 \times 5 \times 5 \times 7 \times 7$ 

Pairing the same kinds of factors, one factor 3 is left unpaired.

3675 should be multiplied by 3 We get 11025 is a perfect square of  $3 \times 5 \times 7 = 105$ 

## **Question 3: Express 121 as the sum of 11 odd numbers. Solution:**

121 = 1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 + 17 + 19 + 21

### Question 4: How many numbers lie between 99<sup>2</sup> and 100<sup>2</sup>? Solution:

Total numbers which lie between  $99^2$  and  $100^2$ = (99 + 100 - 1) = 198

#### **Question 5: Write a Pythagorean triplet whose one number is 17. Solution:**

One number of Pythagorean triplet = 17 Let  $n^2 + 1 = 17 \Rightarrow n^2 = 17 - 1 = 16 = (4)^2$   $\therefore n = 4$   $\therefore$  Numbers will be  $2n = 2 \times 4 = 8$   $n^2 - 1 = 4^2 - 1 = 15$  and  $n^2 + 1 = 17$  $\therefore$  Triplet is (8, 15, 17)

Question 6: Find the smallest square number which is divisible by each of the numbers 6, 8, 9.

#### Solution:

smallest Square which is divisible by 6, 8, 9

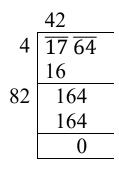
$$\begin{array}{r|rrrr}
 2 & 6, 8, 9 \\
 \hline
 3 & 3, 4, 9 \\
 \hline
 1, 4, 3
 \end{array}$$

LCM of 6, 8,  $9 = 2 \times 3 \times 3 \times 4$ =  $2 \times 2 \times 2 \times 3 \times 3 = 72$ Smallest square =  $2 \times 72 = 144$ 

Question 7: In an auditorium the number of rows is equal to number of chairs in each row. If the capacity of the auditorium is 1764. Find the number of chairs in each row.

#### Solution:

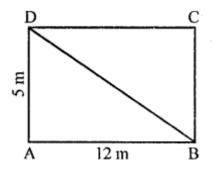
In an auditorium, there are Number of rows = Number of chairs in each row But, capacity is = 1764 persons  $\therefore$  Number of chairs =  $\sqrt{1764} = 42$ 



Question 8: Find the length of diagonal of a rectangle whose length and breadth are 12 m and 5 m respectively.

Solution:

Length of a rectangle = 12 mand breadth = 5 m



: Length of diagonal =  $\sqrt{AB^2 + AD^2}$ 

$$=\sqrt{12^{2} + 5^{2}} = \sqrt{144 + 25}$$
$$= \sqrt{169} = 13 \text{ m}$$
$$1 \frac{13}{169}$$
$$82 \frac{69}{69}$$
$$0$$

### **Question 9: Find the square root of 144 by successive subtraction. Solution:**

```
Square root of 144 = \sqrt{144}

144 = 144 - 1 = 143

143 = 143 - 3 = 140

140 = 140 - 5 = 135

135 = 135 - 7 = 128

128 = 128 - 9 = 119

119 = 119 - 11 = 108

108 = 108 - 13 = 95

95 = 95 - 15 = 80

80 = 80 - 17 = 63

63 = 63 - 19 = 44

44 - 21 = 23

23 - 23 = 0

\therefore Square root = 12
```

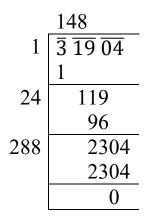
Question 10: Find the square root of following numbers by prime factorisation:

(i) 5625 (ii) 1521					
Solution:					
(i) $5625 = 3 \times 3 \times 5 \times 5 \times 5 \times 5$					
Sc	lna	re root of $5625 = \sqrt{5625}$			
=	3 ×	$5 \times 5 = 75$			
	3	5625			
	3	4875			
	5	625			
	5	125			
	5	25			
	5	5			
		1			

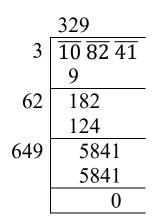
(ii)  $1521 = 3 \times 3 \times 13 \times 13$ Square root of  $1521 = \sqrt{1521}$   $= 3 \times 13 = 39$   $\frac{3 | 1521}{3 | 507}$  13 | 169 13 | 131

**Question 11: Find the square root of following numbers by long division method:** 

(i) 21904 (ii) 108241 Solution: (i)  $\sqrt{21904} = 148$ 

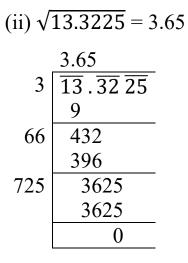


(ii)  $\sqrt{108241} = 329$ 



Question 12: Find the square root of following decimal numbers: (i) 17.64 (ii) 13.3225 Solution: (i)  $\sqrt{17.64} = 4.2$ 

$$\begin{array}{r}
 4.2 \\
 4 \overline{17.64} \\
 16 \\
 82 \overline{164} \\
 164 \\
 \overline{164} \\
 0 \\
 \end{array}$$



#### **Question 13: Find the square root of following fractions:**

(i) $1\frac{25}{44}$	(ii) 11 <sup>225</sup> / <sub>576</sub>
Solution:	

(i)  $1\frac{25}{144} = \frac{144+25}{144} = \frac{169}{144}$  $\therefore \sqrt{\frac{169}{144}} = \frac{\sqrt{169}}{\sqrt{144}} = \frac{\sqrt{13\times13}}{\sqrt{12\times12}}$   $= \frac{13}{12} = 1\frac{1}{12}$ 

(ii) 
$$11\frac{225}{576} = \frac{11 \times 576 + 225}{576}$$
  
=  $\frac{6336 + 225}{576} = \frac{6561}{576}$   
 $8\frac{81}{65.61}$ 

$$\begin{array}{c}
64 \\
161 \\
161 \\
161 \\
0
\end{array}$$

$$= \sqrt{\frac{6561}{576}} = \frac{\sqrt{656}}{\sqrt{576}} = \frac{81}{24}$$
$$= 3\frac{9}{24} = 3\frac{3}{8}$$

## Question 14: Find the least number which must be subtracted from 2311 to make it a perfect square. Solution:

2311

Taking square root, we see that 7 is left as remainder.

So, 7 is to be subtracted from 2311.

48		
4	23.11	
	16	
88	711	
	704	
	7	

Question 15: Find the least number which must be added to 520 to make it a perfect square.

#### Solution:

520 Taking square root of 520, we see that  $(22)^2 < 520$  Then we should take  $(23)^2$  which is 529 So, 529 - 520 = 9 is to be added So, that we resultant number will be a perfect square.

 $\therefore$  Required number = 9

$$\begin{array}{c|c}
2 & 22 \\
2 & \overline{5} \cdot \overline{20} \\
4 \\
42 & 120 \\
& 84 \\
& 36
\end{array}$$

Question 16: Find the greatest number of 5 digits which is a perfect square.

#### Solution:

Greatest 5 digits number = 99999

Taking square root we see that 143 is left as remainder.

So, by subtracting 143 from 99999,

we get the greatest 5 digits which is a perfect square.

Required number = 99999 - 143 = 99856

