# 5. Factorization of Algebraic Expressions

### Exercise 5.1

## 1. Question

Factorize:

$$x^3+x-3x^2-3$$

#### **Answer**

Given.

$$x^3 + x - 3x^2 - 3$$

$$= x(x^2 + 1) - 3(x^2 + 1)$$

$$=(x-3)(x^2+1)$$

#### 2. Question

Factorize:

$$a(a+b)3-3a^{2}b(a+b)$$

#### **Answer**

Given,

$$a(a+b)^3 - 3a^2b(a+b)$$

$$= a(a+b)\{(a+b)^2 - 3ab\}$$
use the identity: $(a+b)^2 = a^2 + b^2 + 2ab$ 

$$= a(a+b)(a^2+b^2+2ab-3ab)$$

$$= a(a + b)(a^2 + b^2 - ab)$$

#### 3. Question

Factorize:

$$x(x^3-y^3)+3xy-(x-y)$$

## **Answer**

Given,

$$x(x^3-y^3)+3xy-(x-y)$$

As 
$$(x^3 - y^3) = (x - y)(x^2 + xy + y^2)$$

$$x(x^3-y^3)+3xy-(x-y) = x[(x-y)(x^2+xy+y^2)] + 3xy-(x-y)$$

Take x(x-y) common to get,

$$x(x-y)[(x^2 + xy + y^2) + 3y]$$

## 4. Question

Factorize:

$$a^2x^2+(ax^2+1)x+a$$

### **Answer**

$$a^2x^2 + (ax^2 + 1)x + a = a^2x^2 + ax^3 + x + a$$

$$= ax^2(a+x) + 1(x+a)$$

$$=(ax^2+1)(x+a)$$

Factorize:

$$x^2+y-xy-x$$

#### **Answer**

Given,

$$x^2 + y - xy - x = x^2 - x + y - xy$$

$$= x(x-1) + y(1-x)$$

$$= x(x-1) - y(x-1)$$

$$= (x-y)(x-1)$$

#### 6. Question

Factorize:

$$x^3-2x^2y+3xy^2-6y^3$$

#### **Answer**

Given,

$$x^3 - 2x^2y + 3xy^2 - 6y^3$$

$$= x^2(x-2y) + 3y^2(x-2y)$$

$$=(x-2y)(x^2+3y^2)$$

## 7. Question

Factorize:

#### **Answer**

Given,

$$6ab-b^2+12ac-2bc = b(6a-b)+2c(6a-b)$$

$$= (b+2c)(6a-b)$$

### 8. Question

Factorize:

$$\left(x^2 + \frac{1}{x^2}\right) - 4\left(x + \frac{1}{x}\right) + 6$$

## **Answer**

$$\left(x^2 + \frac{1}{x^2}\right) - 4\left(x + \frac{1}{x}\right) + 6$$

$$= \left(x^2 + \frac{1}{x^2} + 2\right) - 4\left(x + \frac{1}{x}\right) + 4$$

$$=\left(x+\frac{1}{x}\right)^{2}-4\left(x+\frac{1}{x}\right)+4$$

$$= \left\{ \left( x + \frac{1}{x} \right) - 2 \right\}^2$$

 $= \left\{ \left( x + \frac{1}{x} \right) - 2 \right\}^{2}$  [BY applying  $(a^{2} - 2ab + b^{2}) = (a-b)^{2}$ ]

## 9. Question

Factorize:

x(x-2)(x-4)+4x-8

#### **Answer**

Given,

$$X(x-2)(x-4)+4x-8 = x(x-2)(x-4)+4(x-2)$$

$$= (x-2) (x(x-4)+4)$$

$$= (x-2) (x^2 - 4x + 4)$$

$$= (x-2) (x-2)^2$$

$$= (x-2)^3$$

#### 10. Question

Factorize:

$$(x+2)(x^2+25)-10x^2-20x$$

#### **Answer**

Given,

$$(x+2)(x^2+25) - 10x^2 - 20x = (x+2)(x^2+25)-10x(x+2)$$

$$= (x+2) (x^2+25-10x)$$

$$= (x+2) (x-5)^2$$

#### 11. Question

Factorize:

$$2a^2+2\sqrt{6}ab+3b^2$$

#### **Answer**

Given.

$$2a^2\sqrt{6ab+3b^2} = (\sqrt{2}a)^2 + 2(\sqrt{3} \times \sqrt{2})ab + (\sqrt{3}b)^2$$

$$= (\sqrt{2a} + \sqrt{3b})^2$$

#### 12. Question

Factorize:

$$(a-b+c)^2+(b-c+a)^2+2(a-b+c)(b-c+a)$$

## **Answer**

$$(a-b+c)^2+(b-c+a)^2+2(a-b+c)(b-c+a)$$

= 
$$(a-(b-c))^2 + (a+(b-c))^2 + 2(a-(b-c)) (a+(b-c))$$

[Applying identity: 
$$x^2 + y^2 + 2xy = (x + y)^2$$
, where  $x = a-(b-c)$ ,  $y = a+(b-c)$ ]

$$=[(a-(b-c)) + (a+(b-c))]^2=(2a)^2=4a^2$$

Factorize:

$$a^{2}+b^{2}+2(ab+bc+ca)$$

#### **Answer**

Given,

$$a^{2}+b^{2}+2(ab+bc+ca)$$

$$= a^2+b^2+2ab+2bc+2ca$$

$$= (a+b)^2 + 2c(a+b)$$

$$= (a+b)(a+b+2c)$$

### 14. Question

Factorize:

$$4(x-y)^2-12(x-y)(x+y)+9(x+y)^2$$

#### **Answer**

Given,

$$4(x-y)^2 - 12(x-y)(x+y) + 9(x+y)^2 = 4(x^2-2xy+y^2) - 12(x^2-y^2) + 9(x^2+y^2+2xy)$$

$$= 4x^2-8xy+4y^2-12x^2+12y^2+9x^2+9y+18xy$$

$$= x^2 + 25y^2 + 10xy$$

$$= (x)^2 + (5y)^2 + 2 \times x \times 5y$$

$$= (x+5y)^2$$

### 15. Question

Factorize:

$$a^{2}-b^{2}+2ab-c^{2}$$

## Answer

Given,

$$a^2-b^2+2ab-c^2 = a^2-(b^2-2bc+c^2)$$

$$= a - (b-c)^2$$

$$= (a + (b-c)) (a-(b-c))$$

$$= (a+b-c) (a-b+c)$$

#### 16. Question

Factorize:

$$a^2+2ab+b^2-c^2$$

### **Answer**

Given,

$$a^2+2ab+b^2-c^2 = (a+b)^2 - c^2$$

$$= (a+b-c) (a+b+c)$$

### 17. Question

Factorize:

$$a^2+4b^2-4ab-4c^2$$

### Answer

Given,

$$a^2 + 4b^2 - 4ab - 4c^2 = (a)^2 + (2b)^2 - 2 \times a \times 2b - 4c^2$$

$$= (a-2b)^2 - (2c)^2$$

$$= (a-2b-2c)(a-2b+2c)$$

## 18. Question

Factorize:

$$xy^9-yx^9$$

## Answer

Given.

$$xy^9 - yx^9 = xy (y^8 - x^8)$$

$$= xy ((y^4)^2 - (x^4)^2)$$

$$= xy (y^4 + x^4) (y^4 - x^4)$$

$$= xy (y^4+x^4) (y^2-x^2) (y^2+x^2)$$

$$= xy (y^4+x^4) (y^2+x^2) (y - x) (y+x)$$

### 19. Question

Factorize:

$$x^4 + x^2y^2 + y^4$$

#### **Answer**

Given,

$$x^4 + x^2y^2 + y^4 = x^4 + 2x^2y^2 + y^4 - x^2y^2$$

$$= (x^2y^2)^2 - (xy)^2$$

$$= (x^2 + y^2 - xy) (x^2 + y^2 + xy)$$

## 20. Question

Factorize:

$$x^2-y^2-4xz+4z^2$$

## **Answer**

Given,

$$x^2 - y^2 - 4xz + 4z^2 = x^2 - 4xz + 4z^2 - y^2$$

$$= (x)^2 - 2 \times x \times 2z + (2z)^2 - y^2$$

$$= (x-2z)^2 - y^2$$

$$= (x - 2z - y) (x - 2z + y)$$

$$= (x - y - 2z) (x + y - 2z)$$

#### 21. Question

Factorize:

$$x^2+6\sqrt{2}x+10$$

#### **Answer**

Given,

$$x^2+6\sqrt{2}x+10 = x^2+\sqrt{2}x+10$$

$$= x(x+\sqrt{2}) + 5\sqrt{2} (x + \sqrt{2})$$

$$= (x+\sqrt{2}) (x+5\sqrt{2})$$

## 22. Question

Factorize:

$$x^2 - 2\sqrt{2}x - 30$$

### **Answer**

Given,

$$x^2 - 2\sqrt{2}x - 30 = x^2 - 5\sqrt{2}x + 3\sqrt{2}x - 30$$

$$= x(x-5\sqrt{2}) + 3\sqrt{2} (x - 5\sqrt{2})$$

$$= (x-5\sqrt{2}) (x+3\sqrt{2})$$

## 23. Question

Factorize:

$$x^2 - \sqrt{3} x - 6$$

#### **Answer**

Given,

$$X^2 - \sqrt{3}x - 6 = x^2 - 2\sqrt{3}x + \sqrt{3}x - 6$$

$$= x (x - 2\sqrt{3}) + \sqrt{3} (x-2\sqrt{3})$$

$$= (x + \sqrt{3}) (x - 2\sqrt{3})$$

### 24. Question

Factorize:

$$x^2 + 5\sqrt{5}x + 30$$

#### **A**nswer

Given,

$$x^2 + 5\sqrt{5}x + 30 = x^2 + 3\sqrt{5}x + 2\sqrt{5}x + 30$$

$$= x (x + 3\sqrt{5}) + 2\sqrt{5} (x + 3\sqrt{5})$$

$$= (x + 3\sqrt{5}) (x + 2\sqrt{5})$$

### 25. Question

Factorize:

$$x^2 + 2\sqrt{3}x - 24$$

### **Answer**

$$x^2 + 2\sqrt{3}x - 24 = x^2 + 4\sqrt{3}x - 2\sqrt{3}x - 24$$

$$= x(x + 4\sqrt{3}) - 2\sqrt{3} (x + 4\sqrt{3})$$

$$= (x + 4\sqrt{3}) (x - 2\sqrt{3})$$

Factorize:

$$2x^2 - \frac{5}{6}x + \frac{1}{12}$$

### **Answer**

Given,

$$2x^{2} - \frac{5}{6}x + \frac{1}{12}$$

$$= 2x^{2} - \frac{1}{3}x - \frac{1}{2}x + \frac{1}{12}$$

$$= x\left(2x - \frac{1}{3}\right) - \frac{1}{4}\left(2x - \frac{1}{3}\right)$$

## 27. Question

 $= \left(2x - \frac{1}{3}\right)\left(x - \frac{1}{4}\right)$ 

Factorize:

$$x^2 + \frac{12}{35}x + \frac{1}{35}$$

### **Answer**

Given,

$$x^{2} - \frac{12}{36}x + \frac{1}{36} = x^{2} - \frac{1}{7}x - \frac{1}{5}x + \frac{1}{35}$$
$$x\left(x + \frac{1}{7}\right) + \frac{1}{5}\left(x + \frac{1}{7}\right)$$
$$= \left(x - \frac{1}{7}\right)\left(x + \frac{1}{5}\right)$$

## 28. Question

Factorize:

$$21x^2-2x+\frac{1}{21}$$

### **Answer**

Given,

$$21x^{2} - 2x + \frac{1}{21} = 21x^{2} - x - x + \frac{1}{21}$$
$$= x(21x - 1) - \frac{1}{21}(21x - 1)$$
$$= \left(x - \frac{1}{21}\right)(21x - 1)$$

#### 29. Question

Factorize:

$$5\sqrt{5} x^2 + 20x + 3\sqrt{5}$$

## **Answer**

Given,

$$5\sqrt{5}x^2+20x+3\sqrt{5} = 5\sqrt{5}x^2 + 15x + 5x + 3\sqrt{5}$$

$$= 5x(\sqrt{5}x+3) + \sqrt{5}(\sqrt{5}x+3)$$

$$= (5x + \sqrt{5}) (\sqrt{5}x + 3)$$

## 30. Question

Factorize:

$$2x^2+3\sqrt{5}x+531.9(2a-b)^2-4(2a-b)-13$$

#### **Answer**

Given,

$$2x^2+3\sqrt{5}x+5 = 2x^2 + 2\sqrt{5}x + \sqrt{5}x+5$$

$$= 2x (x + \sqrt{5}) + \sqrt{5} (x + \sqrt{5})$$

$$= (2x+\sqrt{5})(x+\sqrt{5})$$

### 31. Question

Factorize:

$$9(2a - b)^2 - 4(2a - b) - 13$$

### **Answer**

Given,

$$9(2a - b)^2 - 4(2a - b) - 13$$

Let us assume (2a - b) = x

$$9x^2 - 4x - 13$$

$$9x^2 - 13x + 9x - 13$$

$$x(9x - 13) + 1(9x + 3)$$

$$(9x - 13)(x + 1)$$

$$[9(2a - b) - 13][2a - b + 1]$$

$$(18a - 9b - 13)(2a - b + 1)$$

### 32. Question

Factorize:

$$7(x-2y)^2-25(x-2y)+12$$

### **Answer**

Given,

$$7(x - 2y)^2 - 25(x - 2y) + 12$$

Let 
$$a = (x - 2y)$$
,

So we have,

$$= 7a^2 - 25a + 12$$

$$= 7a^{2} - 21a - 4a + 12$$

$$= 7a(a - 3) - 4 (a - 3)$$

$$= (7a - 4) (a - 3)$$
Put  $a = (x - 2y)$ 

$$= \{7(x - 2y) - 4\} (x - 2y - 3)$$

= (7x - 14y - 4) (x - 2y - 3)

### 33. Question

Factorize:

$$2(x+y)^2-9(x+y)-5$$

#### **Answer**

Given,

$$2(x+y)^2 - 9(x+y) - 5$$
,

$$= 2a^2 - 9a - 5$$

Let 
$$(x+y) = a$$

$$= 2a^2 - 10a + a - 5$$

$$= 2a (a-5) + 1(a-5)$$

$$= (2a+1) (a-5)$$

$$= \{2(x+y)+1\}(x+y-5)$$

$$(2x+2y+1)(x+y-5)$$

## 34. Question

Give possible expressions for the length and breadth of the rectangle having  $35y^2+13y-12$  as its area.

#### **Answer**

We know that,

Area of rectangle = length  $\times$  breadth

Given,

$$35y^2 + 13y - 12 = 35y^2 + 28y - 15y - 12$$

$$= 7y(5y+4) - 3(5y + 4)$$

$$= (7y - 3) (5y + 4)$$

Thus,

Length = 
$$(7y - 3)$$
, then breadth =  $(5y + 4)$ 

Length = 
$$(5y + 4)$$
, then breadth =  $(7y - 3)$ 

#### 35. Question

What are the possible expressions for the dimensions of the cuboid whose volume is  $3x^2-12x$ .

#### **Answer**

Given,

We know that.

Volume of cuboids = length  $\times$  breadth  $\times$  height

$$3x^2 - 12x = 3x (x-4)$$

Thus,

Dimensions of cuboids are -

Length	breadth	height
3	x	(x-4)
X	(x-4)	3
(x-4)	3	X

## **Exercise 5.2**

### 1. Question

Factorize each of the following expressions:

$$p^{3}+27$$

### **Answer**

Given,

$$P^3+27$$
,  
=  $p^3 + (3)^3$  [:  $a^3+b^3 = (a+b)(a^2 - 2ab + b^2)$   
=  $(p+3)(p^2 + 9 - 3p)$ 

### 2. Question

Factorize each of the following expressions:

$$y^3 + 125$$

#### **Answer**

Given,

$$y^3+125$$
,  
=  $y^3 + (5)^3$  [:  $a^3+b^3 = (a+b)(a^2 - 2ab + b^2)$   
=  $(y + 5) (y^2 - 5y + 25)$ 

## 3. Question

Factorize each of the following expressions:

#### **Answer**

Given,

$$1 - 27a^3$$
,  
=  $1 - (3a)^3$   
=  $(1 - 3a) (1+9a^2+3a)$ 

## 4. Question

Factorize each of the following expressions:

$$8x^3y^3 + 27a^3$$

### **Answer**

Given,

$$8x^{3}y^{3} + 27a^{3}$$
,  
=  $(2xy)^{3} + (3a)^{3}$   
=  $(2xy + 3a)(4x^{2}y^{2} + 9a^{2} - 6axy)$ 

#### 5. Question

Factorize each of the following expressions:

$$64a^{3}-b^{3}$$

#### **Answer**

Given,

$$64a^3 - b^3$$
,  
=  $(4a)^3 - (b)^3$   
=  $(4a - b) (16a^2 + b^2 + 4ab)$ 

### 6. Question

Factorize each of the following expressions:

$$\frac{x^3}{216}$$
-8y<sup>3</sup>

#### **Answer**

Given,

$$\frac{x^3}{216} - 8y^3 = \left(\frac{x}{6}\right)^3 - (2y)^3$$
$$= \left(\frac{x}{6} - 2y\right) \left(\frac{x^2}{36} + 4y^2 + \frac{xy}{3}\right)$$

### 7. Question

Factorize each of the following expressions:

$$10x^4y-10xy^4$$

### **Answer**

Given,

$$10x^{4} y - 10xy^{4},$$

$$= 10xy (x^{3} - y^{3})$$

$$= 10xy (x - y) (x^{2} + xy - y^{2})$$

#### 8. Question

Factorize each of the following expressions:

$$54x^6y + 2x^3y^4$$

#### **Answer**

$$54x^6 y + 2x^3 y^4,$$
  
=  $2x^3 y (27x^3 + y^3)$ 

$$= 2x^{3} y \{(3x)^{3} + (y)^{3}\}$$
$$= 2x^{3} y (3x + y) (9x^{2} + y^{2} - 3xy)$$

Factorize each of the following expressions:

$$32a^2 + 108b^3$$

#### **Answer**

Given,

$$32a^3 + 108b^3$$
,

$$= 4 (8a^3 + 27b^3)$$

$$= 4 \{ (2a)^3 + (3b)^3 \}$$

$$= 4 (2a + 3b) (4a^2 + 9b^2 - 6ab)$$

#### 10. Question

Factorize each of the following expressions:

$$(a-2b)^3-512b^3$$

#### **Answer**

Given,

$$(a - 2b)^3 - 512b^3$$

$$= (a - 2b)^3 - (8b)^3$$

= 
$$(a - 2b - 8b) \{(a - 2b)^2 + (8b)^2 + (a - 2b) 8b\}$$

$$= (a - 10b) (a^2 + 4b^2 - 4ab + 64b^2 + 8ab - 16b^2)$$

$$= (a - 10b) (a^2 + 52b^2 + 4ab)$$

### 11. Question

Factorize each of the following expressions:

$$(a+b)^3-8(a-b)^3$$

#### **Answer**

Given,

$$(a + b)^3 - {2(a - b)}^3$$

= 
$$\{(a + b) - 2(a - b)\}\ \{(a+b)^2 + 4(a-b)^2 + 2(a+b)(a - b)\}\ [By using: x^3 - y^3 = (x - y)(x^2 + y^2 + xy)\}$$

$$= (a + b - 2a + 2b)(a^2 + b^2 + 2ab + 4a^2 + 4b^2 - 8ab + 2a^2 - 2b^2)$$

$$= (3b - a) (7a^2 + 3b^2 - 6ab)$$

### 12. Question

Factorize each of the following expressions:

$$(x+2)^3+(x-2)^3$$

#### **Answer**

$$(x+2)^3 + (x-2)^3 = (x+2+x-2) \{ (x+2)^2 + (x-2)^2 - (x+2)(x-2) \}$$

$$= 2x (x^2 + 4 + 4x + x^2 + 4 - 4x - x^2 + 4)$$

$$= 2x (x^2 + 12)$$

Factorize each of the following expressions:

$$8x^2y^3-x^5$$

### **Answer**

Given,

$$8x^2y^3 - x^5$$

$$= x^2 (8y^3 - x^3)$$

$$= x^2 \{ (2y)^2 - (x)^3 \}$$

$$= x^2 (2y - x) (4y^2 + x^2 + 2xy)$$

#### 14. Question

Factorize each of the following expressions:

#### **Answer**

Given,

$$1029 - 3x^3$$

$$= 3 (343 - x^3)$$

$$= 3 \{ (7)^3 - (x)^3 \}$$

$$= 3 (7 - x) (49 + x^2 + 7x)$$

## 15. Question

Factorize each of the following expressions:

$$x^6 + y^6$$

#### **Answer**

Given,

$$X^6 + y^6 = (x^2)^3 + (y^2)^3$$

$$= (x^2 + y^2) (x^4 + y^4 - x^2y^2)$$

#### 16. Question

Factorize each of the following expressions:

$$x^{3}y^{3}+1$$

## Answer

Given,

$$X^3y^3 + 1 = (xy)^3 + (1)^3$$

$$= (xy + 1) (x^2 y^2 + 1 - xy)$$

### 17. Question

Factorize each of the following expressions:

$$x^4y^4-xy$$

#### **Answer**

Given,

$$X^4y^4 - xy = xy (x^3y^3 - 1)$$

$$= xy \{ (xy)^3 - (1)^3 \}$$

$$= xy (xy -1) (x^2y^2 +1+xy)$$

#### 18. Question

Factorize each of the following expressions:

$$a^{12}+b^{12}$$

## Answer

Given,

$$a^{12} + b^{12} = (a^4)^3 + (b^4)^3$$

$$= (a^4 + b^4)(a^3 + b^3 - a^4b^4)$$

### 19. Question

Factorize each of the following expressions:

$$x^3+6x^2+12x+16$$

#### **Answer**

Given,

$$X^3 + 6x^2 + 12x + 16 = (x^3 + 6x^2 + 12x + 8) + 8$$

$$= (x+2)^3 + 8 [\because (a+b)^3 = a^3 + b^3 + 3ab(a+b)]$$

$$=(x+2)^3+(2)^3$$

$$= (x+2+2) \{(x+2)^2 + 4 - 2(x+2)\}$$

$$= (x+4)(x^2+4+4x+4-2x-4)$$

$$= (x+4)(x^2+2x+4)$$

## 20. Question

Factorize each of the following expressions:

$$a^{3}+b^{3}+a+b$$

#### **Answer**

Given,

$$a^3+b^3+a+b = (a^3+b^3) + (a+b)$$

$$= (a+b) (a^2 - ab + b^2) + a+b$$

$$= (a+b)(a^2 - ab + b^2 + 1)$$

## 21. Question

Factorize each of the following expressions:

$$a^3 - \frac{1}{a^3} - 2a \frac{2}{a}$$

#### Answer

Given,

$$a^{3} - \frac{1}{a^{3}} - 2a + \frac{2}{a}$$

$$= a^{3} - \frac{1}{a^{3}} - 2\left(a - \frac{1}{a}\right)$$

$$= \left(a - \frac{1}{a}\right)\left(a^{2} + \frac{1}{a^{2}} + 1\right) - 2\left(a - \frac{1}{a}\right)$$

$$= \left(a - \frac{1}{a}\right)\left(a^{2} + \frac{1}{a^{2}} + 1 - 2\right)$$

$$= \left(a - \frac{1}{a}\right)\left(a^{2} + \frac{1}{a^{2}} - 1\right)$$

### 22. Question

Factorize each of the following expressions:

$$a^3+3a^2b^3+3ab^2+b^3-8$$

#### **Answer**

Given,

$$A^{3}+3a^{2}b+3ab^{2}+b^{3}-8 = (a^{3}+3a^{2}b+3ab^{2}+b^{3}) - 8$$

$$= (a+b)^{3}-8$$

$$= (a+b)^{3} - (2)^{3}$$

$$= (a+b-2) \{ (a+b)^{2} + (2)^{2} + 2(a+b) \}$$

$$= (a+b-2) (a^{2}+b^{2} + 2ab+4+2a+2b)$$

#### 23. Question

Factorize each of the following expressions:

$$8a^{3}-b^{3}-4ax+2bx$$

### Answer

Given.

$$8a^{3} - b^{3} - 4 ax + 2bx = (2a)^{3} - (b)^{3} - 2x(2a - b)$$

$$= (2a - b) (4a^{2} + b^{2} + 2ab) - 2x(2a - b)$$

$$= (2a - b) (4a^{2} + b^{2} + 2ab - 2x)$$

### 24. Question

Simplify

$$\text{(i)}\, \frac{173 \times 173 \times 173 + 127 \times 127 \times 127}{173 \times 173 - 173 \times 127 + 127 \times 127}$$

$$(ii)\frac{155 \times 155 \times 155 - 55 \times 55 \times 55}{155 \times 155 + 155 \times 55 + 55 \times 55}$$

(iii) 
$$\frac{1.2 \times 1.2 \times 1.2 - 0.2 \times 0.2 \times 0.2}{1.2 \times 1.2 + 1.2 \times 0.2 + 0.2 \times 0.2}$$

### **Answer**

(i) Given.

$$= \frac{173 \times 173 \times 173 + 127 \times 127 \times 127}{173 \times 173 - 173 \times 127 + 127 \times 127}$$

$$= \frac{(173)^3 + (127)^3}{(173)^2 - 173 \times 127 + (127)^2}$$

$$= \frac{(173 + 127)\{(173)^2 + (127)^2 - 173 \times 127\}}{(173)^2 - 173 \times 127 + (127)^2} = 300$$

(ii) Given,

$$=\frac{(155)^3-(55)^3}{(155)^2+155\times55+(55)^2}$$

$$=\frac{(155-55)\{(155)^2+155\times55+(55)^2\}}{(155)^2+155\times55+(55)^2}$$

$$=(155-55)=100$$

(ii) Given,

$$= \frac{1.2 \times 1.2 \times 1.2 - 0.2 \times 0.2 \times 0.2}{1.2 \times 1.2 + 1.2 \times 0.2 + 0.2 \times 0.2}$$

$$=\frac{(1.2)^3-(0.2)^3}{(1.2)^2+1.2\times0.2+(0.2)^2}$$

$$=\frac{(1.2-0.2)\{(1.2)^2+(0.2)^2+1.2\times0.2\}}{(1.2)^2+1.2\times0.2\times(0.2)^2}$$

$$=(1.2-0.2)=1$$

### Exercise 5.3

#### 1. Question

Factorize:

$$64a^3+125b^3+240a^2b+300ab^2$$

### Answer

Given,

$$64a^3 + 125b^3 + 240a^2b + 300ab^2$$
,

$$= (4a)^3 + (5b)^3 + 60ab (4a + 5b)$$

$$= (4a)^3 + (5b)^3 + 3 \times 4a \times 5b (4a + 5b)$$

$$= (4a+5b)^3$$

$$= (4a+5b)(4a+5b)(4a+5b)$$

### 2. Question

Factorize:

$$125x^3-27y^3-225x^2y+125xy^2$$

#### **Answer**

$$125x^3 - 27y^3 - 225x^2y + 125xy^2$$

$$= (5x)^3 - (3y)^3 - 45xy (5x - 3y)$$

$$= (5x)^3 - (3y)^3 - 3 \times 5x \times 3y (5x - 3y)$$

$$= (5x - 3y)^3$$

$$= (5x - 3y) (5x - 3y) (5x - 3y)$$

Factorize:

$$\frac{8}{27}x^3+1+\frac{4}{3}x^2+2x$$

#### **Answer**

Given,

$$\frac{8}{27}x^3 + 1 + \frac{4}{3}x^2 + 2x,$$

$$= \left(\frac{2}{3}x\right)^3 + (1)^3 + 2x\left(\frac{2}{3}x + 1\right)$$

$$= \left(\frac{2}{3}x\right)^3 + (1)^3 + 3x\frac{2}{3}x \times 1\left(\frac{2}{3}x + 1\right)$$

$$= \left(\frac{2}{3}x + 1\right)^3$$

## 4. Question

Factorize:

$$8x^3 + 27y^3 + 36x^2y + 54xy^2$$

 $=\left(\frac{2}{3}x+1\right)\left(\frac{2}{3}x+1\right)\left(\frac{2}{3}x+1\right)$ 

#### **Answer**

Given,

$$8x^3+27y^3+36x^2y+54xy^2$$
,  
=  $(2x)^3+(3y)^3+18xy(2x+3y)$ 

$$= (2x)^3 + (3y)^3 + 3 \times 2x \times 3y (2x + 3y)$$

$$= (2x+3y)^3$$

$$= (2x +3y) (2x +3y) (2x +3y)$$

### 5. Question

Factorize:

$$a^{3}-3a^{2}b+3ab^{2}-b^{3}+8$$

#### **Answer**

$$a^3 - 3a^2b + 3ab^2 - b^3 + 8,$$
  
= {(a)<sup>3</sup> - (b)<sup>3</sup> -3ab (a-b)} +8

$$= (a-b)^3 + (2)^3$$

= 
$$(a - b + 2) \{(a - b)^2 + (2)^2 + 2(a - b)\}$$

$$= (a - b + 2)(a^2 - 2ab + b^2 + 4 + 2a - 2b)$$

Factorize:

$$x^3+8y^3+6x^2y+12xy^2$$

#### **Answer**

Given,

$$x^3+8y^3+6x^2y+12xy^2$$

$$= (x)^3 + (2y)^3 + 6xy (x + 2y)$$

$$= (x)^3 + (2y)^3 + 3 \times x \times 2y (x + 2y)$$

$$= (x+2y)^3$$

$$= (x +2y) (x +2y) (x +2y)$$

### 7. Question

Factorize:

$$8x^3+y^3+12x^2y+6xy^2$$

#### **Answer**

Given,

$$8x^3+y^3+12x^2y+6xy^2$$
,

$$= (2x)^3 + (y)^3 + 6xy (2x + y)$$

$$= (2x)^3 + (y)^3 + 3 \times 2x \times y (2x + y)$$

$$= (2x+y)^3$$

$$= (2x + y) (2x + y) (2x + y)$$

### 8. Question

Factorize:

$$8a^3 + 27b^3 + 36a^2b + 54ab^2$$

#### **Answer**

Given,

$$8a^3 + 27b^3 + 36a^2b + 54ab^2$$
,

$$= (2a)^3 + (3b)^3 + 18ab (2a + 3b)$$

$$= (2a)^3 + (3b)^3 + 3 \times 2a \times 3b (2a + 3b)$$

$$= (2a + 3b)^3$$

$$= (2a + 3b) (2a + 3b) (2a + 3b)$$

### 9. Question

Factorize:

$$8a^3-27b^3-36a^2b+54ab^2$$

Answer

Given.

$$8a^3 - 27b^3 - 36a^2b + 54ab^2$$
,

$$= (2a)^3 - (3b)^3 - 18ab (2a - 3b)$$

$$= (2a)^3 - (3b)^3 - 3 \times 2a \times 3b (2a - 3b)$$

$$= (2a - 3b)^3$$

$$= (2a - 3b) (2a - 3b) (2a - 3b)$$

#### 10. Question

Factorize:

$$x^3-12x(x-4)-64$$

#### **Answer**

Given,

$$x^3-12x(x-4)-64$$

$$= (x)^3 -12x (x - 4) - (4)^3$$

$$= (x)^3 - (4)^3 - 3 \times x \times 4 (x - 4)$$

$$= (x - 4)^3$$

$$= (x - 4) (x - 4) (x - 4)$$

#### 11. Question

Factorize:

$$a^{3}x^{3}-3a^{2}bx^{2}+3ab^{2}x-b^{3}$$

#### **Answer**

Given,

$$a^{3}x^{3}-3a^{2}bx^{2}+3ab^{2}x-b^{3}$$
.

$$= (ax)^3 - 3abx(ax-b) - (b)^3$$

$$= (ax)^3 - (b)^3 - 3abx (ax-b)$$

$$= (ax-b)^3$$

$$=$$
 (ax-b) (ax-b) (ax-b)

## **Exercise 5.4**

## 1. Question

Factorize each of the following expressions:

$$a^3+8b^3+64c^3-24abc$$

#### **Answer**

Given,

$$= a^3 + 8b^3 + 64c^3 - 24abc$$

This can be written in form

$$= a^3 + 8b^3 + 64c^3 - 24abc = (a)^3 + (2b)^3 + (4c)^3 - 3 \times a \times 2b \times 4c$$

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

Hence.

$$= a^3 + 8b^3 + 64c^3 - 24abc = (a + 2b + 4c)\{(a)^2 + (2b)^2 + (4c)^2 - a \times 2b - 2b \times 4c - 4c \times a\}$$

$$= (a + 2b + 4c)(a^2 + 4b^2 + 16c^2 - 2ab - 8bc - 4ca)$$

Thus the required factors of  $a^3 + 8b^3 + 64c^3 - 24abc$  is  $(a + 2b + 4c)(a^2 + 4b^2 + 16c^2 - 2ab - 8bc - 4ca)$ 

#### 2. Question

Factorize each of the following expressions:

$$x^3-8y^3+27z^3+18xyz$$

#### **Answer**

Given,

$$= x^3 - 8y^3 + 27z^3 + 18xyz$$

This can be written in form,

$$= x^3 - 8y^3 + 27z^3 + 18xyz = (x)^3 + (-2y)^3 + (3z)^3 - 3xxx(-2y)x3z$$

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

$$= x^3 - 8y^3 + 27z^3 + 18xyz = \{x + (-2y) + 3z\}\{(x)^2 + (-2y)^2 + (3z)^2 - (x)(-2y) - (-2y)(3z) - (3z)(x)\}$$

$$= (x - 2y + 3z)(x^2 + 4y^2 + 9z^2 + 2xy + 6yz - 3zx)$$

Thus the required factors of  $x^3 - 8y^3 + 27z^3 + 18xyz$  is  $(x - 2y + 3z)(x^2 + 4y^2 + 9z^2 + 2xy + 6yz - 3zx)$ 

#### 3. Question

Factorize each of the following expressions:

$$27x^{3}-v^{3}-z^{3}-9xvz$$

#### **Answer**

Given,

$$= 27x^3 - y^3 - z^3 - 9xyz$$

This can be written in form,

$$=27x^3-y^3-z^3-9xyz=(3x)^3+(-y)^3+(-z)^3-3(3x)(-y)(-z)$$

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

So,

$$= 27x^3 - y^3 - z^3 - 9xyz = \{3x + (-y) + (-z)\}\{(3x)^2 + (-y)^2 + (-z)^2 - (3x)(-y) - y(-z) - z(3x)\}$$

$$=(3x-y-z)(9x^2+y^2+z^2+3xy-yz+3zx)$$

Thus the factors of  $27x^3 - y^3 - z^3 - 9xyz$  is  $(3x - y - z)(9x^2 + y^2 + z^2 + 3xy - yz + 3zx)$ 

#### 4. Question

Factorize:

$$\frac{1}{27}$$
x<sup>3</sup>-y<sup>3</sup>+125z<sup>3</sup>+5xyz

#### **Answer**

$$= \frac{1}{27} x^3 - y^3 + 125z^3 + 5xyz$$

This can be written in form,

$$= \frac{1}{27} x^3 - y^3 + 125z^3 + 5xyz = \left(\frac{1}{3}x\right)^3 + (-y)^3 + (5z)^3 - 3\left(\frac{1}{3}x\right)(-y)(5z)$$

$$=a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

$$= \frac{\frac{1}{27}x^3 - y^3 + 125z^3 + 5xyz = \left\{ \left( \frac{1}{3}x \right) + (-y) + (5z) \right\} \left\{ \left( \frac{1}{3}x \right)^2 + (-y)^2 + (5z)^2 - \left( \frac{1}{3}x \right) (-y) - y \right\} (5z) - (5z) \left( \frac{1}{3}x \right)$$

$$= \left(\frac{1}{3}x - y + 5z\right) \left(\frac{1}{9}x^2 + y^2 + 25z^2 + \frac{1}{3}xy + 5yz - \frac{5}{3}zx\right)$$

Thus the factors of 
$$\frac{1}{27}$$
  $x^3 - y^3 + 125z^3 + 5xyz$  is  $\left(\frac{1}{3}x - y + 5z\right)\left(\frac{1}{9}x^2 + y^2 + 25z^2 + \frac{1}{3}xy + 5yz - \frac{5}{3}zx\right)$ 

### 5. Question

Factorize each of the following expressions:

$$8x^3 + 27y^3 - 216z^3 + 108xyz$$

#### **Answer**

Given.

$$= 8x^3 + 27y^3 - 216z^3 + 108xyz$$

This can be written in form .

$$= 8x^3 + 27y^3 - 216z^3 + 108xyz = (2x)^3 + (3y)^3 + (-6z)^3 - 3(2x)(3y)(-6z)$$

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

$$= \frac{8x^3 + 27y^3 - 216z^3 + 108xyz = \{(2x) + (3y) + (-6z)\}\{(2x)^2 + (3y)^2 + (-6z)^2 - (2x)(3y) - (3y)((-6z) - (-6z)(2x)\}}{(2x)^2 + (2x)^2 + (2x)$$

$$= (2x + 3y - 6z)(4x^2 + 9y^2 + 36z^2 - 6xy + 18yz + 12zx)$$

Thus the factors of

$$8x^3 + 27y^3 - 216z^3 + 108xyz$$
 is  $(2x + 3y - 6z)(4x^2 + 9y^2 + 36z^2 - 6xy + 18yz + 12zx)$ 

### 6. Ouestion

Factorize each of the following expressions:

$$125 + 8x^3 - 27y^3 + 90xy$$

#### **Answer**

Given,

$$= 125 + 8x^3 - 27y^3 + 90xy$$

This can be written in form,

$$= 125 + 8x^3 - 27y^3 + 90xy = (5)^3 + (2x)^3 + (-3y)^3 - 3(5)(2x)(-3y)$$

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

$$= 125 + 8x^3 - 27y^3 + 90xy = \{5 + 2x - 3y\}\{(5)^2 + (2x)^2 + (-3y)^2 - (5)(2x) - (2x)(-3y) - (-3y)(5)\}$$

$$= (5 + 2x - 3y)(25 + 4x^2 + 9y^2 - 10x + 6xy + 15y)$$

Thus the factors of  $125 + 8x^3 - 27y^3 + 90xy$  is  $(5 + 2x - 3y)(25 + 4x^2 + 9y^2 - 10x + 6xy + 15y)$ 

Factorize:

$$(3x-2y)^3+(2y-4z)^3+(4z-3x)^3$$

#### **Answer**

Given,

$$= (3x-2y)^3 + (2y-4z)^3 + (4z-3x)^3$$

Let 
$$a = (3x - 2y)$$
,  $b = (2y - 4z)$ ,  $c = (4z - 3x)$ 

$$= (3x-2y)^3 + (2y-4z)^3 + (4z-3x)^3 = a^3 + b^3 + c^3$$

Here,

$$= a + b + c = (3x - 2y + 2y - 4z + 4z - 3x) = 0$$

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

Hence,

$$= a^3 + b^3 + c^3 - 3abc = 0 \times (a^2 + b^2 + c^2 - ab - bc - ca)$$

$$= a^3 + b^3 + c^3 = 3abc$$

$$= (3x - 2y)^3 + (2y - 4z)^3 + (4z - 3x)^3 = 3(3x - 2y)(2y - 4z)(4z - 3x)$$

### 8. Question

Factorize each of the following expressions:

$$(2x-3y)^3+(4z-2x)^3+(3y-4z)^3$$

### Answer

Given,

$$=(2x-3y)^3+(4z-2x)^3+(3y-4z)^3$$

Let 
$$a = (2x - 3y)$$
,  $b = (4z - 2x)$ ,  $c = (3y - 4z)$ 

Then,

$$= (2x-3y)^3 + (4z-2x)^3 + (3y-4z)^3 = a^3 + b^3 + c^3$$

Here,

$$= a + b + c = 2x - 3y + 4z - 2x + 3y - 4z = 0$$

Hence,

$$= a^3 + b^3 + c^3 - 3abc = 0 \times (a^2 + b^2 + c^2 - ab - bc - ca)$$

$$= a^3 + b^3 + c^3 = 3abc$$

$$= (2x - 3v)^3 + (4z - 2x)^3 + (3v - 4z)^3 = 3(2x - 3v)(4z - 2x)(3v - 4z)$$

#### 9. Question

Factorize each of the following expressions:

$$\left(\frac{x}{2} + y + \frac{z}{3}\right)^3 + \left(\frac{x}{3} - \frac{2y}{3} + y\right)^3 + \left(-\frac{5x}{6} - \frac{y}{3} - \frac{4z}{3}\right)^3$$

#### **Answer**

$$= \left(\frac{x}{2} + y + \frac{z}{3}\right)^3 + \left(\frac{x}{3} - \frac{2y}{3} + z\right)^3 + \left(-\frac{5x}{6} - \frac{y}{3} - \frac{4z}{3}\right)^3$$

Let 
$$a = (\frac{x}{2} + y + \frac{z}{3})$$
,  $b = (\frac{x}{3} - \frac{2y}{3} + z)$ ,  $c = (-\frac{5x}{6} - \frac{y}{3} - \frac{4z}{3})$ 

Then,

$$= \left(\frac{x}{2} + y + \frac{z}{3}\right)^3 + \left(\frac{x}{3} - \frac{2y}{3} + z\right)^3 + \left(-\frac{5x}{6} - \frac{y}{3} - \frac{4z}{3}\right)^3 = a^3 + b^3 + c^3$$

Here,

$$= a + b + c = \left(\frac{x}{2} + y + \frac{z}{3}\right) + \left(\frac{x}{3} - \frac{2y}{3} + z\right) + \left(-\frac{5x}{6} - \frac{y}{3} - \frac{4z}{3}\right) = 0$$

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

Hence,

$$= a^3 + b^3 + c^3 - 3abc = 0 \times (a^2 + b^2 + c^2 - ab - bc - ca)$$

$$= a^3 + b^3 + c^3 = 3abc$$

$$= \left(\frac{x}{2} + y + \frac{z}{2}\right)^3 + \left(\frac{x}{2} - \frac{2y}{2} + z\right)^3 + \left(-\frac{5x}{6} - \frac{y}{2} - \frac{4z}{2}\right)^3 = 3\left(\frac{x}{2} + y + \frac{z}{2}\right)\left(\frac{x}{2} - \frac{2y}{2} + z\right)\left(-\frac{5x}{6} - \frac{y}{2} - \frac{4z}{2}\right).$$

#### 10. Question

Factorize each of the following expressions:

$$(a-3b)^3+(3b-c)^3+(c-a)^3$$

#### **Answer**

Given,

$$=(a-3b)^3+(3b-c)^3+(c-a)^3$$

Let 
$$x = (a-3b), v = (3b-c), z = (c-a)$$

Then.

$$= (a-3b)^3 + (3b-c)^3 + (c-a)^3 = x^3 + y^3 + z^3$$

Here,

$$= x + y + z = a - 3b + 3b - c + c - a = 0$$

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

Hence,

$$= a^3 + b^3 + c^3 - 3abc = 0 \times (a^2 + b^2 + c^2 - ab - bc - ca)$$

$$= a^3 + b^3 + c^3 = 3abc$$

$$= (a-3b)^3 + (3b-c)^3 + (c-a)^3 = 3(a-3b)(3b-c)(c-a)$$

#### 11. Question

Factorize each of the following expressions:

$$2\sqrt{2} a^3 + 3\sqrt{3} b^3 + c^3 - 3\sqrt{6} abc$$

#### **Answer**

Given.

$$= 2\sqrt{2}a^3 + 3\sqrt{3}b^3 + c^3 - 3\sqrt{6}abc$$

This can be written in form,

$$=2\sqrt{2}a^{3}+3\sqrt{3}b^{3}+c^{3}-3\sqrt{6}abc=\left(\sqrt{2}a\right)^{3}+\left(\sqrt{3}b\right)^{3}+(c)^{3}-3\left(\sqrt{2}a\right)\left(\sqrt{3}b\right)(c)$$

And, 
$$a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

Hence,

$$= \frac{2\sqrt{2}a^3 + 3\sqrt{3}b^3 + c^3 - 3\sqrt{6}abc = \{\left(\sqrt{2}a\right) + \left(\sqrt{3}b\right) + c\}\} \left\{\left(\sqrt{2}a\right)^2 + \left(\sqrt{3}b\right)^2 + (c)^2 - \left(\sqrt{2}a\right)\left(\sqrt{3}b\right) - \left(\sqrt{3}b\right)(c) - (c)\left(\sqrt{2}a\right)\right\}}$$

$$=\sqrt{2}a + \sqrt{3}b + c$$
) $(2a^2 + 3b^2 + c^2 - \sqrt{6}ab - \sqrt{3}bc - \sqrt{2}ca$ 

### 12. Question

Factorize each of the following expressions:

$$3\sqrt{3} a^3-b^3-5\sqrt{5} c^3-3\sqrt{15} abc$$

#### **Answer**

Given,

$$= 3\sqrt{3}a^3 - b^3 - 5\sqrt{5}c^3 - 3\sqrt{15}abc$$

This can be written in form .

$$=3\sqrt{3}a^3-b^3-5\sqrt{5}c^3-3\sqrt{15}abc=\left(\sqrt{3}a\right)^3+\left(-b\right)^3+\left(-\sqrt{5}c\right)^3-3\left(\sqrt{3}a\right)\left(-b\right)\left(-\sqrt{5}c\right)$$

And, 
$$a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

$$= \frac{3\sqrt{3}a^3 - b^3 - 5\sqrt{5}c^3 - 3\sqrt{15}abc = \left\{ \left(\sqrt{3}a\right) + \left(-b\right) + \left(-\sqrt{5}c\right) \right\} \left\{ \left(\sqrt{3}a\right)^2 + \left(-b\right)^2 + \left(-\sqrt{5}c\right)^2 - \left(\sqrt{3}a\right)(-b) - b\right) \left(-\sqrt{5}c\right) - \left(-\sqrt{5}c\right)\left(\sqrt{3}a\right) \right\}$$

= 
$$(\sqrt{3}a - b - \sqrt{5}c)(3a^2 + b^2 + 5c^2 + \sqrt{3}ab - \sqrt{5}bc + \sqrt{15}ca$$

#### 13. Question

Factorize each of the following expressions:

$$8x^{3}-125y^{3}+180xy+216$$

#### **Answer**

Given,

$$= 8x^3 - 125y^3 + 180xy + 216$$

This can be written in form,

$$= 8x^3 - 125y^3 + 180xy + 216 = (2x)^3 + (-5y)^3 + 6^3 - 3(2x)(-5y)(6)$$

And , 
$$a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

Hence,

$$= 8x^3 - 125y^3 + 180xy + 216 = \{2x + (-5y) + 6\}\{(2x)^2 + (-5y)^2 + 6^2 - (2x)(-5y) - (-5y)(6) - (6)(2x)\}$$

$$= (2x - 5y + 6)(4x^2 + 25y^2 + 36 + 10xy + 30y - 12x)$$

Thus the factors of  $8x^3 - 125y^3 + 180xy + 216$  is

$$(2x - 5y + 6)(4x^2 + 25y^2 + 36 + 10xy + 30y - 12x)$$

#### 14. Question

Factorize each of the following expressions:

$$2\sqrt{2} a^3 + 16\sqrt{2} b^3 + c^3 - 12abc$$

#### **Answer**

Given.

$$= 2\sqrt{2}a^3 + 16\sqrt{2}b^3 + c^3 - 12abc$$

This can be written in form,

$$= 2\sqrt{2}a^3 + 16\sqrt{2}b^3 + c^3 - 12abc = (\sqrt{2}a)^3 + (2\sqrt{2}b)^3 + c^3 - 3(\sqrt{2}a)(2\sqrt{2}b)(c)$$

And, 
$$a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

Hence.

$$= 2\sqrt{2}a^3 + 16\sqrt{2}b^3 + c^3 - 12abc = \{\sqrt{2}a + 2\sqrt{2}b + c\}\{\left(\sqrt{2}a\right)^2 + \left(2\sqrt{2}b\right)^2 + c^2 - \left(\sqrt{2}a\right)\left(2\sqrt{2}b - \left(2\sqrt{2}b\right)(c) - (c)\left(\sqrt{2}a\right)\right\}$$

= 
$$(\sqrt{2}a + 2\sqrt{2}b + c)(2a^2 + 8b^2 + c^2 - 4ab - 2\sqrt{2}bc - \sqrt{2}ca)$$

Thus the factors of  $2\sqrt{2}a^3 + 16\sqrt{2}b^3 + c^3 - 12abc$  is  $(\sqrt{2}a + 2\sqrt{2}b + c)(2a^2 + 8b^2 + c^2 - 4ab - 2\sqrt{2}bc - \sqrt{2}ca)$ 

#### 15. Question

Find the value of  $x^3+y^3-12xy+64$ , when x+y=-4.

#### Answer

Given,

$$= x^3 + y^3 - 12xy + 64$$

$$= x + y = -4$$
 Given

$$= x + y + 4 = 0$$

This can be written in form,

$$= x^3 + y^3 - 12xy + 64 = x^3 + y^3 + 4^3 - 3(x)(y)(4)$$

And , 
$$a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

$$= x^3 + y^3 - 12xy + 64 = (x + y + 4)\{(x)^2 + (y)^2 + 4^2 - xy - 4y - 4x\}$$

$$= 0 \times (x^2 + y^2 + 16 - xy - 4y - 4x)$$

= 0

## 16. Question

Multiply:

(i) 
$$x^2+y^2+z^2-xy+xz+yzbyx+y-z$$

(ii) 
$$x^2+4y^2+z^2+2xy+xz-2yzbyx-2y-z$$

(iii) 
$$x^2+4y^2+2xy+-3x+6y+9byx-2y+3$$

(iv) 
$$9x^2+25y^2+15xy+12x-20y+16by3x-5y+4$$

## Answer

(i) Given.

$$= x^2 + y^2 + z^2 - xy + xz + yz$$

Multiply the above expression by (x + y - z)

$$= (x + y - z)(x^2 + y^2 + z^2 - xy + xz + yz)$$

$$= \{x + y + (-z)\}\{(x)^2 + (y)^2 + (-z)^2 - xy + yz + zx\}$$

$$= x^3 + y^3 + (-z)^3 - 3 \cdot x \cdot y(-z)$$

$$= x^3 + y^3 - z^3 + 3xyz$$

(ii) Given,

$$= x^2 + 4y^2 + z^2 + 2xy + xz - 2yz$$

Multiply above expression by (x-2y-z)

Then,

$$=(x-2y-z)(x^2+4y^2+z^2+2xy+xz-2yz)$$

$$= \{x + (-2y) + (-z)\}\{x^2 + 4y^2 + z^2 + 2xy - 2yz + zx\}$$

By formula...

$$= x^3 - 8y^3 - z^3 - 6xyz$$

iii) we have

$$= x^2 + 4y^2 + 2xy - 3x + 6y + 9$$

(iii) Given,

$$= x^2 + 4y^2 + 2xy - 3x + 6y + 9$$

Multiply above equation by (x-2y+3)

$$= (x-2y+3)(x^2+4y^2+2xy-3x+6y+9)$$

$$= \{x - 2y + 3\}\{x^2 + 4y^2 + 9 + 2xy + 6y - 3x\}$$

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

$$= x^3 - 8y^3 + 27 + 18xy$$

(iv) Given,

$$= 9x^2 + 25y^2 + 15xy + 12x - 20y + 16$$

Multiply above equation by (3x - 5y + 4)

We got,

$$= (3x - 5y + 4)(9x^2 + 25y^2 + 15xy + 12x - 20y + 16) = (3x + (-5y) + 4)((3x)^2 + (-5y)^2 + 4^2 - 3x(-5y) - (-5y)(4) - (4)(3x))$$

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

$$= (3x)^3 + (-5y)^3 + (4)^3 - 3.3x(-5y)(4)$$

$$= 27x^3 - 125y^3 + 64 + 180xy$$

#### **CCE - Formative Assessment**

#### 1. Question

Factorize:  $x^4+x^2+25$ .

#### **Answer**

We have,

First we rewrite the question,

$$x^4 + x^2 + 25 = (x^2)^2 + 2 \cdot x^2 \cdot 5 + 52 - 9x^2$$
  
=  $\{(x^2)^2 + 2 \cdot x^2 \cdot 5 + 52\} - (3x)^2$  [By using  $a^2 + 2ab + b^2 = (a + b)^2$ ]  
=  $\{x^2 + 5\}^2 - (3x)^2$  [By using  $a^2 - b^2 = (a + b)(a - b)$   
=  $(x^2 + 5 + 3x)(x^2 + 5 - 3x)$ 

Thus, the factors of  $x^4 + x^2 + 25$  are  $(x^2 + 5 + 3x)(x^2 + 5 - 3x)$ .

### 2. Question

Factorize:  $x^2-1-2a-a^2$ .

#### **Answer**

We have,

$$= x^2 - 1 - 2a - a^2$$

Taking -1 as common from last three terms

$$= x^2 - (1 + 2a + a^2)$$

$$= x^2 - (1^2 + 2 \times 1 \times a + a^2)$$

$$= x^2 - (1+a)^2 [a^2 - b^2 = (a+b)(a-b)]$$

$$= (x+1+a)(x-1-a)$$

Thus the factors of  $x^2 - 1 - 2a - a^2$  are (x + 1 + a)(x - 1 - a).

### 3. Question

If a + b + c = 0, then write the value of  $a^3 + b^3 + c^3$ .

#### **Answer**

We have,

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

When (a + b + c) = 0 Given

$$= a^3 + b^3 + c^3 - 3abc = 0 \times (a^2 + b^2 + c^2 - ab - bc - ca)$$

$$= a^3 + b^3 + c^3 - 3abc = 0$$

$$= a^3 + b^3 + c^3 = 3abc.$$

## 4. Question

 $Ifa^2+b^2+c^2=20$ , and a+b+c=0, find ab+bc+ca.

## **Answer**

We have,

$$= (a + b + c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca)$$
 By formula

$$= a^2 + b^2 + c^2 = 20$$
 Given

$$=(a+b+c)=0$$
 Given

Then.

$$= (a + b + c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca)$$

$$= (0)^2 = 20 + 2(ab + bc + ca)$$

$$= 2(ab + bc + ca) = -20$$

$$= (ab + bc + ca) = -10$$

If a + b + c = 9 and ab + bc + ca = 40, find  $a^2 + b^2 + c^2$ .

#### **Answer**

We have,

$$= (a + b + c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca)$$
 By formula

$$= a + b + c = 9$$
 Given

$$= ab + bc + ca = 40$$
 Given

Then,

$$= (a + b + c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca)$$

$$= (9)^2 = a^2 + b^2 + c^2 + 2 \times 40$$

$$= a^2 + b^2 + c^2 = 81 - 80$$

$$= a^2 + b^2 + c^2 = 1$$

#### 6. Question

If  $a^2 + b^2 + c^2 = 250$  and ab + bc + ca = 3, find a + b + c.

#### **Answer**

We have,

$$= (a + b + c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca)$$
 By formula

$$= a^2 + b^2 + c^2 = 250$$
 Given

$$= ab + bc + ca = 3$$
 Given

Then,

$$= (a+b+c)^2 = a^2+b^2+c^2+2(ab+bc+ca)$$

$$= (a + b + c)^2 = 250 + 2 \times 3$$

$$= (a+b+c)^2 = 256$$

$$= (a + b + c) = \sqrt{256} = \pm 16$$
.

## 7. Question

Write the value of:  $25^3 - 75^3 + 50^3$ .

### **Answer**

We have,

$$=25^3-75^3+50^3$$

Let 
$$a = 25$$
,  $b = -75$ ,  $c = 50$ ,

Then the expression becomes as ,

$$= 25^3 - 75^3 + 50^3 = a^3 + b^3 + c^3$$

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

Here, 
$$(a+b+c) = 25 + (-75) + 50 = 0$$

Hence,

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

$$= a^3 + b^3 + c^3 - 3abc = 0 \times (a^2 + b^2 + c^2 - ab - bc - ca)$$

$$= a^3 + b^3 + c^3 = 3abc$$

$$= 25^3 - 75^3 + 50^3 = 3 \times 25 \times -75 \times 50$$

$$= 25^3 - 75^3 + 50^3 = -281250.$$

#### 8. Question

Write the value of:  $48^3 - 30^3 - 18^3$ .

#### **Answer**

We have.

$$=48^3-30^3-18^3$$
 Given

Let 
$$a = 48$$
,  $b = -30$ ,  $c = -18$ 

Then the expression becomes,

$$=48^3-30^3-18^3=a^3+b^3+c^3$$

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

Here,

$$= (a+b+c) = 48 + (-30) + (-18) = 0$$

Hence,

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

$$= a^3 + b^3 + c^3 - 3abc = 0 \times (a^2 + b^2 + c^2 - ab - bc - ca)$$

$$= a^3 + b^3 + c^3 = 3abc$$

$$=48^3-30^3-18^3=3\times48\times-30\times-18$$

$$=48^3-30^3-18^3=77760.$$

#### 9. Question

Write the value of:  $\left(\frac{1}{2}\right)^3 + \left(\frac{1}{3}\right)^3 - \left(\frac{5}{6}\right)^3$ 

#### **Answer**

We have,

$$= \left(\frac{1}{2}\right)^3 + \left(\frac{1}{3}\right)^3 - \left(\frac{5}{6}\right)^3 \text{ Given}$$

Let  $a = \frac{1}{2}$ ,  $b = \frac{1}{3}$ ,  $c = -\frac{5}{6}$ , then the expression becomes

$$=\left(\frac{1}{2}\right)^3+\left(\frac{1}{2}\right)^3-\left(\frac{5}{6}\right)^3=a^3+b^3+c^3$$

Here,

$$= a + b + c = \frac{1}{2} + \frac{1}{3} - \frac{5}{6} = 0$$

Hence,

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

$$= a^3 + b^3 + c^3 - 3abc = 0 \times (a^2 + b^2 + c^2 - ab - bc - ca)$$

$$= a^3 + b^3 + c^3 = 3abc$$

$$= \left(\frac{1}{2}\right)^3 + \left(\frac{1}{3}\right)^3 - \left(\frac{5}{6}\right)^3 = 3 \times \frac{1}{2} \times \frac{1}{3} \times -\frac{5}{6}$$

$$=\left(\frac{1}{2}\right)^3+\left(\frac{1}{3}\right)^3-\left(\frac{5}{6}\right)^3=-\frac{5}{12}$$

Write the value of:  $30^3 + 20^3 - 50^3$ .

#### **Answer**

We have,

$$=30^3+20^3-50^3$$
 given

Let a = 30, b = 20, c = -50, then the expression becomes,

$$=30^3+20^3-50^3=a^3+b^3+c^3$$

Here,

$$= a + b + c = 30 + 20 - 50 = 0$$

Hence,

$$= a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$
 By formula

$$= a^3 + b^3 + c^3 - 3abc = 0 \times (a^2 + b^2 + c^2 - ab - bc - ca)$$

$$= a^3 + b^3 + c^3 = 3abc$$

$$=30^3+20^3-50^3=3\times30\times20\times-50$$

$$=30^3+20^3-50^3=-90000$$

#### 1. Question

The factors of  $a^2$ -1-2x- $x^2$  are

A. 
$$(a-x+1)(a-x-1)$$

B. 
$$(a+x-1)(a-x+1)$$

C. 
$$(a+x+1)(a-x-1)$$

D. none of these

#### **Answer**

We have,

$$= a^2 - 1 - 2x - x^2$$

$$= a^2 - (1 + 2x + x^2) = a^2 - (1 + x)^2$$

$$= (a-1-x)(a+1+x) [a^2-b^2 = (a+b)(a-b)]$$

Thus, the factors of  $a^2 - 1 - 2x - x^2$  are (a - 1 - x)(a + 1 + x).

### 2. Question

The factors of  $x^4+x^2=25$  are

A. 
$$(x^2+3x+5)(x^2-3x+5)$$

B. 
$$(x^2+3x+5)(x^2+3x-5)$$

C. 
$$(x^2+x+5)(x^2-x+5)$$

D. none of these

#### **Answer**

We have,

$$= x^4 + x^2 + 25$$

Adding and subtracting  $9x^2$  in the equation

$$=x^4 + 25 + x^2 + 9x^2 - 9x^2$$

$$= x^4 + 25 + 10x^2 - 9x^2 = (x^2 + 5)^2 - (3x)^2$$

$$=(x^2+5-3x)(x^2+5+3x)$$

Thus the factors of  $(x^4+x^2+25)$  are  $(x^2+5-3x)(x^2+5-3x)$ .

#### 3. Ouestion

The factors of  $x^2+4y^2+4y-4xy-2x-8$  are

A. 
$$(x-2y-4)(x-2y+2)$$

B. 
$$(x-y+2)(x-4y-4)$$

C. 
$$(x+2y-4)(x+2y+2)$$

D. none of these

#### **Answer**

We have,

$$= x^2 + 4y^2 + 4y - 4xy - 2x - 8$$

$$= x^2 + 4y^2 - 4xy + 4y - 2x - 8 = (x - 2y)^2 - 2(x - 2y) - 8$$

Let a = (x-2y), then the expression becomes,

$$= x^2 + 4y^2 + 4y - 4xy - 2x - 8 = a^2 - 2a - 8$$

$$= a^2 - 4a + 2a - 8$$

$$= a(a-4) + 2(a-4)$$

$$=(a-4)(a+2)$$

Put 
$$a = (x - 2y)$$

$$= x^{2} + 4y^{2} + 4y - 4xy - 2x - 8 = (x - 2y - 4)(x - 2y + 2)$$

Thus the factors of  $x^2 + 4y^2 + 4y - 4xy - 2x - 8$  are (x - 2y - 4)(x - 2y + 2)

## 4. Question

The factors of  $x^3-x^2y-xy^2+y^3$  are

A. 
$$(x+y)(x^2-xy+y^2)$$

B. 
$$(x+y)(x^2+xy+y^2)$$

C. 
$$(x+y)^2(x-y)$$

D. 
$$(x-y)^2(x+y)$$

#### Answer

We have.

$$= x^3 - x^2y - xy^2 + y^3$$

$$= x^3 + y^3 - x^2y - xy^2 = (x + y)^3 - 3x^2y - 3xy^2 - x^2y - xy^2$$

As 
$$x^3 + y^3 = (x + y)^3 - 3x^2y - 3xy^2$$

$$= (x + y)^3 - 4xy(x + y)$$

$$=(x + y) \{(x + y)^2 - 4xy\}$$

$$= (x + y)(x^2 + y^2 + 2xy - 2xy)$$

$$=(x + y)(x^2 + y^2 - 2xy) = (x + y)(x - y)^2$$

### 5. Question

The factors of  $x^3-1+y^3+3xy$  are

A. 
$$(x-1+y)(x^2+1+y^2+x+y-xy)$$

B. 
$$(x+y+1)(x^2+y^2+1-xy-x-y)$$

C. 
$$(x-1+y)(x^2-1-y^2+x+y+xy)$$

D. 
$$3(x+v-1)(x^2+v^2-1)$$

### Answer

We have,

$$= x^3 - 1 + y^3 + 3xy$$

$$= (x)^3 + (-1)^3 + (y)^3 - 3(x)(-1)(y)$$

$$= (x-1+y)(x^2+1+y^2+x+y-xy) \{(a^3+b^3+c^3-3abc = (a+b+c)(a^2+b^2+c^2-ab-bc-ca)\}$$

Thus the factors of  $x^3 - 1 + y^3 + 3xy$  are  $(x - 1 + y)(x^2 + 1 + y^2 + x + y - xy)$ 

#### 6. Question

The factors of 8a<sup>2</sup>+b<sup>3</sup>-6ab+1are

A. 
$$(2a+b-1)(4a^2+b^2+1-3ab-2a)$$

B. 
$$(2a-b+1)(4a^2+b^2-4ab+1-2a+b)$$

C. 
$$(2a+b+1)(4a^2+b^2+1-2ab-b-2a)$$

D. 
$$(2a-1+b)(4a^2+1-4a-b-2ab)$$

### **Answer**

We have,

$$= 8a^3 + b^3 - 6ab + 1$$

$$= (2a)^3 + (b)^3 - 3(2a)(b)(1) + (1)^3$$
 try to make  $(a^3 + b^3 + c^3 - 3abc)$ 

$$= (2a + b + 1)(4a^2 + b^2 + 1 - 2ab - b - 2a)$$

Thus the factors of  $8a^3 + b^3 - 6ab + 1$  are  $(2a + b + 1)(4a^2 + b^2 + 1 - 2ab - b - 2a)$ .

#### 7. Question

 $(x+y)^3$ - $(x-y)^3$  can be factorized as:

A. 
$$2y(3x^2+y^2)$$

B. 
$$2x(3x^2+y^2)$$

C. 
$$2y(3y^2+x^2)$$

D. 
$$2x(x^2+3y^2)$$

### **Answer**

We have,

$$=(x+y)^3-(x-y)^3$$

Applying formulas,

$$= x^3 + y^3 + 3x^2y + 3xy^2 - (x^3 - y^3 - 3x^2y + 3xy^2)$$

$$= x^3 + y^3 + 3x^2y + 3xy^2 - x^3 + y^3 + 3x^2y - 3xy^2$$

$$=2y^3+6x^2y$$

$$= 2y(y^2 + 3x^2)$$

Thus the factors of  $(x + y)^3 - (x - y)^3$  are  $2y(y^2 + 3x^2)$ 

## 8. Question

The factors of  $x^2-7x+6$  are

A. 
$$x(x-6)(x-1)$$

B. 
$$(x^2-6)(x-1)$$

C. 
$$(x+1)(x+2)(x-3)$$

D. 
$$(x-1)(x+3)(x-2)$$

#### **Answer**

We have,

$$= x^3 - 7x - 6$$

Adding and subtracting 1 in the equation

$$= x^3 - 7x - 6 - 1 + 1 = x^3 + 1^3 - 7x - 7$$

$$= (x+1)(x^2+1+x)-7(x+1)$$

$$=(x+1)(x^2-6+x)$$

$$=(x+1)(x^3-3x+2x+x)=(x+1)(x+2)(x-3)$$

Thus the factors of  $x^3 - 7x - 6$  are (x+1)(x+2)(x-3).

### 9. Question

The expression  $(a-b)^3+(b-c)^3+(c-a)^3$  can be factorized as:

A. 
$$(a-b)(b-c)(c-a)$$

D. 
$$(a+b+c)(a^2+b^2+c^2-ab-bc-ca)$$

#### **Answer**

We have,

Let 
$$x = (a - b), y = (b - c), z(c - a)$$

So, 
$$x + y + z = a - b + b - c + c - a$$

If a+b+c=0, then,

$$= a^3 + b^3 + c^3 = 3abc$$

$$= (a-b)^3 + (b-c)^3 + (c-a)^3 = 3(a-b)(b-c)(c-a).$$

### 10. Question

The expression  $x^4+4$  can be factorized as

A. 
$$(x^2+2x+2)(x^2-2x+2)$$

B. 
$$(x^2+2x+2)(x^2+2x-2)$$

C. 
$$(x^2-2x-2)(x^2-2x+2)$$

D. 
$$(x^2+2)(x^2-2)$$

#### Answer

We have .

$$= x^4 + 4$$

$$= x^4 + 4x^2 + 4 - 4x^2$$

$$=(x^2+2)^2-4x^2$$

$$= (x^2 + 2)^2 - (2x)^2 [x^2 - y^2 = (x - y)(x + y)]$$

$$=(x^2+2+2x)(x^2+2-2x)$$

### 11. Question

If 3x=a+b+c, then the value of  $(x-a)^3+(x-b)^3+(x-c)^3-3(x-a)(x-b)(x-c)$  is

A. 
$$a+b+c$$

D. 0

D. none of these

### **Answer**

We have,

$$= 3x = a+b+c$$

Let 
$$a_1 = x - a$$
,  $b_1 = x - b$ ,  $c_1 = x - c$ 

So, 
$$a_1 + b_1 + c_1 = x - a + x - b + x - c = 3x - (a + b + c)$$

$$= 3x - 3x = 0$$
 [ a +b + c = 3x ] given

$$= (x-a)^3 + (x-b)^3 + (x-c)^3 = 3(x-a)(x-b)(x-c)$$

Now, 
$$(x-a)^3 + (x-b)^3 + (x-c)^3 - 3(x-a)(x-b)(x-c) = 0$$
.

## 12. Question

If 
$$(x+y)^3-(x-y)^3-6y(x^2-y^2)=ky^2$$
 then  $k=$ 

A. 1

B. 2

#### **Answer**

We have,

$$=(x+y)^3-(x-y)^3-6y(x^2-y^2)=ky^3$$

$$= (x + y - x + y)^3 + 3(x + y)(x - y)(x + y - x + y) - 6y(x^2 - y^2) = ky^3$$

$$= 2y^3 + 6y(x^2 - y^2) - 6y(x^2 - y^2) = ky^3$$

$$= 8v^3 = kv^3$$

$$= k = 8$$
.

#### 13. Question

 $Ifx^3-3x^2+3x-7=(x+1)(ax^2+bx+c)$ , then a+b+c=

- A. 4
- B. 12
- C. -10
- D. 3

#### **Answer**

We have.

$$= x^3 - 3x^2 + 3x - 7 = (x + 1)(ax^2 + bx + c)$$

$$=x^3 - 3x^2 + 3x - 7 = ax^3 + bx^2 + cx + ax^2 + bx + c$$

$$= x^3 - 3x^2 + 3x - 7 = ax^3 + (a + b)x^2 + (b + c)x + c$$

By compairing both sides,

$$= a = 1$$

$$= a + b = -3$$

$$= b + c = 3$$

$$= c = -7$$

Thus, a + (b + c) = 1+3 = 4.

## 14. Question

The value of  $\frac{(2.3)^3 - 0.027}{(2.3)^2 + 0.69 + 0.09}$  is

- A. 2
- B. 3
- C. 2.327
- D. 2.273

#### Answer

We have,

$$=\frac{2.3^3-0.027}{2.3^2+0.69+0.09}$$

$$= \frac{2.3^{3} - 0.027}{2.3^{2} + 0.69 + 0.09} = \frac{2.3^{3} - 0.3^{3}}{2.3^{2} + 0.3^{2} + 2.3 \times 0.3} [a^{3} - b^{3} = (a - b)(a^{2} + b^{2} + ab)]$$

Hence,

$$= \frac{\{(a-b)(a^2+b^2+ab)\}}{a^2+b^2+ab} = a - b$$

$$= (2.3 - 0.3) = 2$$
.

## 15. Question

The value of  $\frac{(0.013)^3+(0.007)^3}{(0.013)^2-0.013\times0.013\times0.007+(0.007)^2}is$ 

- A. 0.006
- B. 0.02
- C. 0.0091
- D. 0.00185

#### **Answer**

We have,

$$= \frac{{}_{0.013^3 + 0.007^3}}{{}_{0.013^2 - 0.013 \times 0.007 + 0.007^2}} [a^3 + b^3 = (a + b)(a^2 + b^2 - ab)]$$

Hence,

$$= \frac{\{(a+b)(a^2+b^2-ab)\}}{a^2+b^2-ab} = a+b$$

$$= 0.013 + 0.007 = 0.020$$