

9. Triangle and Its Angles

Exercise 9.1

1. Question

In a $\triangle ABC$, if $\angle A = 55^\circ$, $\angle B = 40^\circ$, find $\angle C$

Answer

Given, $\angle A = 55^\circ$

$\angle B = 40^\circ$ and $\angle C = ?$

We know that, In $\triangle ABC$ sum of all angles of triangle is 180°

$$\angle A + \angle B + \angle C = 180^\circ$$

$$55^\circ + 40^\circ + \angle C = 180^\circ$$

$$95^\circ + \angle C = 180^\circ$$

$$\angle C = 85^\circ$$

2. Question

If the angles of a triangle are in the ratio 1 : 2 : 3, determine three angles.

Answer

Given that the angles of the triangle are in ratio 1 : 2 : 3

Let, the angles be a , $2a$, $3a$

Therefore, we know that

Sum of all angles if triangle is 180°

$$a + 2a + 3a = 180^\circ$$

$$6a = 180^\circ$$

$$a = \frac{180}{6}$$

$$a = 30^\circ$$

Since, $a = 30^\circ$

$$2a = 2 (30^\circ) = 60^\circ$$

$$3a = 3 (30^\circ) = 90^\circ$$

Therefore, angles are $a = 30^\circ$, $2a = 60^\circ$ and $3a = 90^\circ$

Hence, angles are 30° , 60° and 90° .

3. Question

The angles of a triangle are $(x-40)^\circ$, $(x-20)^\circ$ and $\left(\frac{1}{2}x - 10\right)^\circ$. Find the value of x .

Answer

Given that,

The angles of the triangle are $(x - 40^\circ)$, $(x - 20^\circ)$ and $\left(\frac{x}{2} - 10^\circ\right)$

We know that,

Sum of all angles of triangle is 180° .

Therefore,

$$x - 40^\circ + x - 20^\circ + \frac{x}{2} - 10^\circ = 180^\circ$$

$$2x + \frac{x}{2} - 70^\circ = 180^\circ$$

$$\frac{5x}{2} = 250^\circ$$

$$5x = 250^\circ \times 2$$

$$5x = 500^\circ$$

$$x = 100^\circ$$

Therefore, $x = 100^\circ$

4. Question

The angles of a triangle are arranged ascending order of magnitude. If the difference between two consecutive angles is 10° , find the three angles.

Answer

Given that,

The difference between two consecutive angles is 10° .

Let, x , $x + 10$ and $x + 20$ be the consecutive angles differ by 10° .

We know that,

$$x + x + 10 + x + 20 = 180^\circ$$

$$3x + 30^\circ = 180^\circ$$

$$3x = 180^\circ - 30^\circ$$

$$3x = 150^\circ$$

$$x = 50^\circ$$

Therefore, the required angles are:

$$x = 50^\circ$$

$$x + 10 = 50^\circ + 10^\circ$$

$$= 60^\circ$$

$$x + 20 = 50^\circ + 20^\circ$$

$$= 70^\circ$$

The difference between two consecutive angles is 10° then three angles are 50° , 60° and 70° .

5. Question

Two angles of a triangle are equal and the third angle is greater than each of those angles by 30° . Determine all the angles of the triangle.

Answer

Given that,

Two angles are equal and third angle is greater than each of those angles by 30° .

Let, x , x , $x + 30^\circ$ be the angles of the triangle.

We know that,

Sum of all angles of triangle is 180°

$$x + x + x + 30^\circ = 180^\circ$$

$$3x + 30^\circ = 180^\circ$$

$$3x = 180^\circ - 30^\circ$$

$$3x = 150^\circ$$

$$x = 50^\circ$$

Therefore,

The angles are:

$$x = 50^\circ$$

$$x = 50^\circ$$

$$x + 30^\circ = 50^\circ + 30^\circ$$

$$= 80^\circ$$

Therefore, the required angles are 50° , 50° , 80° .

6. Question

If one angle of a triangle is equal to the sum of the other two, show that the triangle is a right triangle.

Answer

If one of the angle of a triangle is equal to the sum of other two.

$$\text{i.e. } \angle B = \angle A + \angle C$$

Now, in $\triangle ABC$

Sum of all angles of triangle is 180°

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle B + \angle B = 180^\circ \text{ [Therefore, } \angle A + \angle C = \angle B]$$

$$2\angle B = 180^\circ$$

$$\angle B = 90^\circ$$

Therefore, ABC is right angled triangle.

7. Question

ABC is a triangle in which $\angle A = 72^\circ$, the internal bisectors of angles B and C meet in O . Find the magnitude of $\angle BOC$.

Answer

Given,

ABC is a triangle

$\angle A = 72^\circ$ and internal bisectors of B and C meet O .

In $\triangle ABC$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$72^\circ + \angle B + \angle C = 180^\circ$$

$$\angle B + \angle C = 180^\circ - 72^\circ$$

$$\angle B + \angle C = 108^\circ$$

Divide both sides by 2, we get

$$\frac{\angle B}{2} + \frac{\angle C}{2} = \frac{108}{2}$$

$$\frac{\angle B}{2} + \frac{\angle C}{2} = 54^\circ$$

$$\angle OBC + \angle OCB = 54^\circ \text{ (i)}$$

Now, in $\triangle BOC$

$$\angle OBC + \angle OCB + \angle BOC = 180^\circ$$

$$54^\circ + \angle BOC = 180^\circ \text{ [Using (i)]}$$

$$\angle BOC = 180^\circ - 54^\circ$$

$$= 126^\circ$$

8. Question

The bisectors of base angles of a triangle cannot enclose a right angle in any case.

Answer

In $\triangle ABC$ sum of all angles of a triangle is 180°

$$\angle A + \angle B + \angle C = 180^\circ$$

Divide both sides by 2, we get

$$\frac{1}{2}\angle A + \frac{1}{2}\angle B + \frac{1}{2}\angle C = 90^\circ$$

$$\frac{1}{2}\angle A + \angle OBC + \angle OCB = 90^\circ \text{ [Therefore, OB, OC bisects } \angle B \text{ and } \angle C]$$

$$\angle OBC + \angle OCB = 90^\circ - \frac{1}{2}\angle A$$

Now, in $\triangle BOC$

$$\angle BOC + \angle OBC + \angle OCB = 180^\circ$$

$$\angle BOC + 90^\circ - \frac{1}{2}\angle A = 180^\circ$$

$$\angle BOC = 90^\circ - \frac{1}{2}\angle A$$

Hence, bisector open base angle cannot enclose right angle.

9. Question

If the bisectors of the base angles of a triangle enclose an angle of 135° , prove that the triangle is a right triangle.

Answer

Given bisector of the base angles of a triangle enclose an angle of 135°

$$\text{i.e. } \angle BOC = 135^\circ$$

But,

$$135^\circ = 90^\circ + \frac{1}{2}\angle A$$

$$\frac{1}{2}\angle A = 135^\circ - 90^\circ$$

$$\angle A = 45^\circ \text{ (2)}$$

$$= 90^\circ$$

Therefore, $\triangle ABC$ is right angled triangle right angled at A.

10. Question

In a $\triangle ABC$, $\angle ABC = \angle ACB$ and the bisectors of $\angle ABC$ and $\angle ACB$ intersect at O such that $\angle BOC = 120^\circ$. Show that $\angle A = \angle B = \angle C = 60^\circ$.

Answer

Given,

In $\triangle ABC$

$$\angle ABC = \angle ACB$$

Divide both sides by 2, we get

$$\frac{1}{2}\angle ABC = \frac{1}{2}\angle ACB$$

$$\angle OBC = \angle OCB \text{ [Therefore, OB, OC bisects } \angle B \text{ and } \angle C]$$

Now,

$$\angle BOC = 90^\circ + \frac{1}{2}\angle A$$

$$120^\circ - 90^\circ = \frac{1}{2}\angle A$$

$$30^\circ \times 2 = \angle A$$

$$\angle A = 60^\circ$$

Now in $\triangle ABC$

$$\angle A + \angle ABC + \angle ACB = 180^\circ \text{ [Sum of all angles of a triangle]}$$

$$60^\circ + 2\angle ABC = 180^\circ \text{ [Therefore, } \angle ABC = \angle ACB]$$

$$2\angle ABC = 180^\circ - 60^\circ$$

$$2\angle ABC = 120^\circ$$

$$\angle ABC = 60^\circ$$

$$\text{Therefore, } \angle ABC = \angle ACB = 60^\circ$$

Hence, proved

11. Question

Can a triangle have:

- (i) Two right angles?
- (ii) Two obtuse angles?
- (iii) Two acute angles?
- (iv) All angles more than 60° ?
- (v) All angles less than 60° ?
- (vi) All angles equal to 60° ?

Justify your answer in each case.

Answer

(i) No, two right angles would add up to 180° so the third angle becomes zero. This is not possible. Therefore, the triangle cannot have two right angles.

(ii) No, a triangle can't have two obtuse angles as obtuse angle means more than 90° . So, the sum of the two sides exceeds more than 180° which is not possible. As the sum of all three angles of a triangle is 180° .

(iii) Yes, a triangle can have two acute angles as acute angle means less than 90° .

(iv) No, having angles more than 60° make that sum more than 180° which is not possible as the sum of all angles of a triangle is 180° .

(v) No, having all angles less than 60° will make that sum less than 180° which is not possible as the sum of all angles of a triangle is 180° .

(vi) Yes, a triangle can have three angles equal to 60° as in this case the sum of all three is equal to 180° which is possible. This type of triangle is known as equilateral triangle.

12. Question

If each angle of a triangle is less than the sum of the other two, show that the triangle is acute angled.

Answer

Given,

Each angle of a triangle is less than the sum of the other two.

Therefore,

$$\angle A + \angle B + \angle C$$

$$\angle A + \angle A < \angle A + \angle B + \angle C$$

$$2\angle A < 180^\circ \text{ [Sum of all angles of a triangle]}$$

$$\angle A < 90^\circ$$

Similarly,

$$\angle B < 90^\circ \text{ and } \angle C < 90^\circ$$

Hence, the triangle is acute angled.

Exercise 9.2

1. Question

The exterior angles, obtained on producing the base of a triangle both ways are 104° and 136° . Find all the angles of the triangle.

Answer

Let, ABC be a triangle and base BC produced to both sides. Exterior angles are $\angle ABD$ and $\angle ACE$.

$$\angle ABD = 104^\circ$$

$$\angle ACE = 136^\circ$$

$$\angle ABD + \angle ABC = 180^\circ \text{ (Linear pair)}$$

$$104^\circ + \angle ABC = 180^\circ$$

$$\angle ABC = 180^\circ - 104^\circ$$

$$= 76^\circ$$

$$\angle ACE + \angle ACB = 180^\circ$$

$$136^\circ + \angle ACB = 180^\circ$$

$$\angle ACB = 180^\circ - 136^\circ$$

$$= 44^\circ$$

In $\triangle ABC$

$$\angle A + \angle ABC + \angle ACB = 180^\circ$$

$$\angle A + 76^\circ + 44^\circ = 180^\circ$$

$$\angle A + 120^\circ = 180^\circ$$

$$\angle A = 180^\circ - 120^\circ$$

$$= 60^\circ$$

Thus, angles of triangle are 60° , 76° and 44° .

2. Question

In a $\triangle ABC$, the internal bisectors of $\angle B$ and $\angle C$ meet at P and the external bisectors of $\angle B$ and $\angle C$ meet at Q . Prove that $\angle BPC + \angle BQC = 180^\circ$.

Answer

Given that ABC is a triangle.

BP and CP are internal bisector of $\angle B$ and $\angle C$ respectively

BQ and CQ are external bisector of $\angle B$ and $\angle C$ respectively.

$$\text{External } \angle B = 180^\circ - \angle B$$

$$\text{External } \angle C = 180^\circ - \angle C$$

In $\triangle BPC$

$$\angle BPC + \frac{1}{2}\angle B + \frac{1}{2}\angle C = 180^\circ$$

$$\angle BPC = 180^\circ - \frac{1}{2}(\angle B + \angle C) \quad (i)$$

In $\triangle BQC$

$$\angle BQC + \frac{1}{2}(180^\circ - \angle B) + \frac{1}{2}(180^\circ - \angle C) = 180^\circ$$

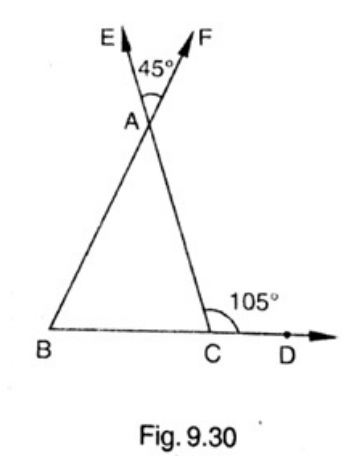
$$\angle BQC + 180^\circ - \frac{1}{2}(\angle B + \angle C) = 180^\circ$$

$$\angle BPC + \angle BQC = 180^\circ \text{ [From (i)]}$$

Hence, proved

3. Question

In Fig. 9.30, the sides BC , CA and AB of a $\triangle ABC$ have been produced to D , E and F respectively. If $\angle ACD = 105^\circ$ and $\angle EAF = 45^\circ$, find all the angles of the $\triangle ABC$.



Answer

Given,

$$\angle ACD = 105^\circ$$

$$\angle EAF = 45^\circ$$

$$\angle EAF = \angle BAC \text{ (Vertically opposite angle)}$$

$$\angle BAC = 45^\circ$$

$$\angle ACD + \angle ACB = 180^\circ \text{ (Linear pair)}$$

$$105^\circ + \angle ACB = 180^\circ$$

$$\angle ACB = 180^\circ - 105^\circ$$

$$= 75^\circ$$

In $\triangle ABC$

$$\angle BAC + \angle ABC + \angle ACB = 180^\circ$$

$$45^\circ + \angle ABC + 75^\circ = 180^\circ$$

$$\angle ABC = 180^\circ - 120^\circ$$

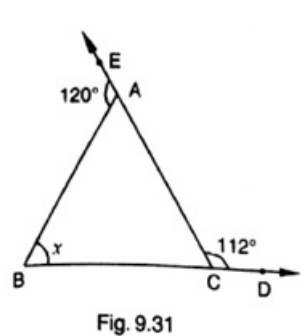
$$= 60^\circ$$

Thus, all three angles of a triangle are 45° , 60° and 75° .

4. Question

Compute the value of x in each of the following figures:

(i)



(ii)

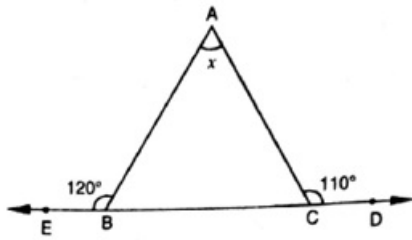


Fig. 9.32

(iii)

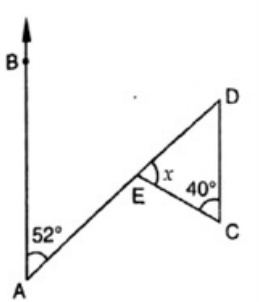


Fig. 9.33

(iv)

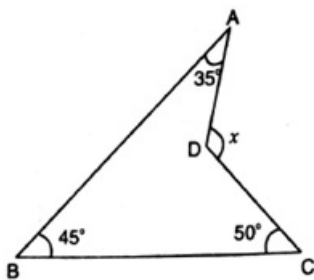


Fig. 9.34

Answer

(i) $\angle DAC + \angle BAC = 180^\circ$ (Linear pair)

$$120^\circ + \angle BAC = 180^\circ$$

$$\angle BAC = 180^\circ - 120^\circ$$

$$= 60^\circ$$

And,

$$\angle ACD + \angle ACB = 180^\circ$$

$$112^\circ + \angle ACB = 180^\circ$$

$$\angle ACB = 68^\circ$$

In $\triangle ABC$,

$$\angle BAC + \angle ACB + \angle ABC = 180^\circ$$

$$60^\circ + 68^\circ + x = 180^\circ$$

$$128^\circ + x = 180^\circ$$

$$x = 180^\circ - 128^\circ$$

$$= 52^\circ$$

(ii) $\angle ABE + \angle ABC = 180^\circ$ (Linear pair)

$$120^\circ + \angle ABC = 180^\circ$$

$$\angle ABC = 60^\circ$$

$\angle ACD + \angle ACB = 180^\circ$ (Linear pair)

$$110^\circ + \angle ACB = 180^\circ$$

$$\angle ACB = 70^\circ$$

In $\triangle ABC$

$$\angle A + \angle ACB + \angle ABC = 180^\circ$$

$$x + 70^\circ + 60^\circ = 180^\circ$$

$$x + 130^\circ = 180^\circ$$

$$x = 50^\circ$$

(iii) $AB \parallel CD$ and AD cuts them so,

$\angle BAE = \angle EDC$ (Alternate angles)

$$\angle EDC = 52^\circ$$

In $\triangle EDC$

$$\angle EDC + \angle ECD + \angle CED = 180^\circ$$

$$52^\circ + 40^\circ + x = 180^\circ$$

$$92^\circ + x = 180^\circ$$

$$x = 180^\circ - 92^\circ$$

$$= 88^\circ$$

(iv) Join AC

In $\triangle ABC$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$(35^\circ + \angle 1) + 45^\circ + (50^\circ + \angle 2) = 180^\circ$$

$$130^\circ + \angle 1 + \angle 2 = 180^\circ$$

$$\angle 1 + \angle 2 = 50^\circ$$

In $\triangle DAC$

$$\angle 1 + \angle 2 + \angle D = 180^\circ$$

$$50^\circ + x = 180^\circ$$

$$x = 180^\circ - 50^\circ$$

$$= 130^\circ$$

5. Question

In Fig. 9.35, AB divides $\angle DAC$ in the ratio 1: 3 and $AB = DB$. Determine the value of x .

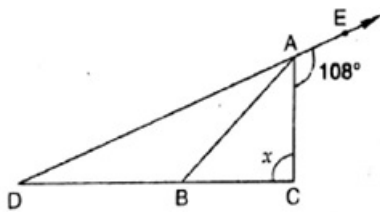


Fig. 9.35

Answer

Given,

AB divides $\angle DAC$ in the ratio 1: 3

$$\angle DAB: \angle BAC = 1: 3$$

$$\angle DAC + \angle EAC = 180^\circ$$

$$\angle DAC + 108^\circ = 180^\circ$$

$$\angle DAC = 180^\circ - 108^\circ$$

$$= 72^\circ$$

$$\angle DAB = \frac{1}{4} * 72^\circ = 18^\circ$$

$$\angle BAC = \frac{3}{4} * 72^\circ = 54^\circ$$

In $\triangle ADB$

$$\angle DAB + \angle ADB + \angle ABD = 180^\circ$$

$$18^\circ + 18^\circ + \angle ABD = 180^\circ$$

$$36^\circ + \angle ABD = 180^\circ$$

$$\angle ABD = 180^\circ - 36^\circ$$

$$= 144^\circ$$

$$\angle ABD + \angle ABC = 180^\circ \text{ (Linear pair)}$$

$$144^\circ + \angle ABC = 180^\circ$$

$$\angle ABC = 180^\circ - 144^\circ$$

$$= 36^\circ$$

In $\triangle ABC$

$$\angle BAC + \angle ABC + \angle ACB = 180^\circ$$

$$54^\circ + 36^\circ + x = 180^\circ$$

$$90^\circ + x = 180^\circ$$

$$x = 180^\circ - 90^\circ$$

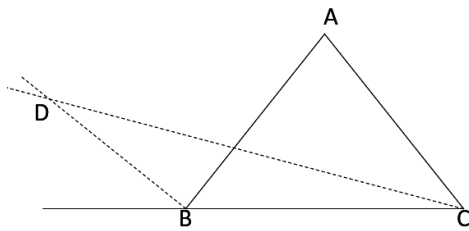
$$= 90^\circ$$

Thus, $x = 90^\circ$

6. Question

ABC is a triangle. The bisector of the exterior angle at B and the bisector of $\angle C$ intersect each other at D . Prove that $\angle D = \frac{1}{2} \angle A$.

Answer



$$\text{Exterior } \angle B = (180^\circ - \angle B)$$

$$\text{Exterior } \angle C = (180^\circ - \angle C)$$

In $\triangle ABC$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\frac{1}{2}(\angle A + \angle B + \angle C) = 180^\circ$$

$$\frac{1}{2}(\angle B + \angle C) = 180^\circ - \frac{1}{2}\angle A \quad (i)$$

In $\triangle BDC$

$$\angle D + \angle DBC + \angle DCB = 180^\circ$$

$$\angle D + \{180^\circ - \frac{1}{2}(180^\circ - \angle B) - \angle B\} + \{180^\circ - \frac{1}{2}(180^\circ - \angle C) - \angle C\} = 180^\circ$$

$$\angle D + 360^\circ - 90^\circ - 90^\circ - (\frac{1}{2}\angle B + \frac{1}{2}\angle C) = 180^\circ$$

$$\angle D + 180^\circ - 90^\circ - \frac{1}{2}\angle A = 180^\circ$$

$$\angle D = \frac{1}{2}\angle A$$

Hence, proved

7. Question

In Fig. 9.36, $AC \perp CE$ and $\angle A : \angle B : \angle C = 3:2:1$, find the value of $\angle ECD$.

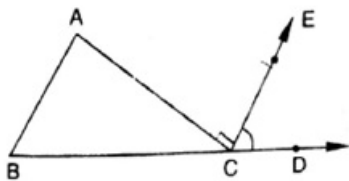


Fig. 9.36

Answer

Given,

AC is perpendicular to CE

$$\angle A : \angle B : \angle C = 3 : 2 : 1$$

Let,

$$\angle A = 3k$$

$$\angle B = 2k$$

$$\angle C = k$$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$3k + 2k + k = 180^\circ$$

$$6k = 180^\circ$$

$$k = 30^\circ$$

Therefore,

$$\angle A = 3k = 90^\circ$$

$$\angle B = 2k = 60^\circ$$

$$\angle C = k = 30^\circ$$

Now,

$$\angle C + \angle ACE + \angle ECD = 180^\circ \text{ (Linear pair)}$$

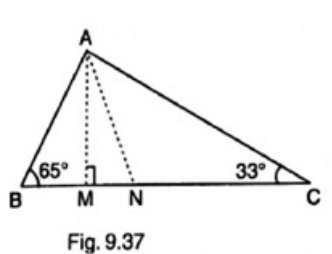
$$30^\circ + 90^\circ + \angle ECD = 180^\circ$$

$$\angle ECD = 180^\circ - 120^\circ$$

$$= 60^\circ$$

8. Question

In Fig. 9.37, $AM \perp BC$ and AN is the bisector of $\angle A$. If $\angle B = 65^\circ$ and $\angle C = 33^\circ$, find $\angle MAN$.



Answer

Given,

AM perpendicular to BC

AN is bisector of $\angle A$

Therefore, $\angle NAC = \angle NAB$

In $\triangle ABC$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + 65^\circ + 33^\circ = 180^\circ$$

$$\angle A = 180^\circ - 98^\circ$$

$$= 82^\circ$$

$$\angle NAC = \angle NAB = 41^\circ \text{ (Therefore, } AN \text{ is bisector of } \angle A)$$

In $\triangle AMB$

$$\angle AMB + \angle MAB + \angle ABM = 180^\circ$$

$$90^\circ + \angle MAB + 65^\circ = 180^\circ$$

$$\angle MAB + 155^\circ = 180^\circ$$

$$\angle MAB = 25^\circ$$

Therefore,

$$\angle MAB + \angle MAN = \angle BAN$$

$$25^\circ + \angle MAN = 41^\circ$$

$$\angle MAN = 41^\circ - 25^\circ$$

$$= 16^\circ$$

9. Question

In a $\triangle ABC$, AD bisects $\angle A$ and $\angle C > \angle B$. Prove that $\angle ADB > \angle ADC$.

Answer

Given,

AD bisects $\angle A$ ($\angle DAB = \angle DAC$)

$$\angle C > \angle B$$

In $\triangle ADB$,

$$\angle ADB + \angle DAB + \angle B = 180^\circ \text{ (i)}$$

In $\triangle ADC$,

$$\angle ADC + \angle DAC + \angle C = 180^\circ \text{ (ii)}$$

From (i) and (ii), we get

$$\angle ADB + \angle DAB + \angle B = \angle ADC + \angle DAC + \angle C$$

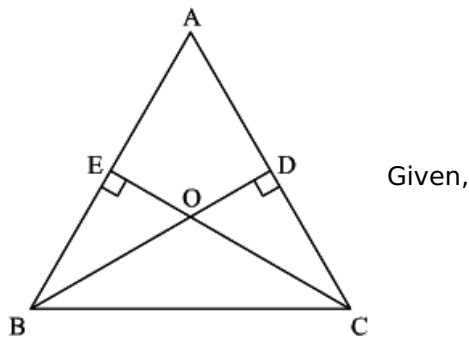
$$\angle ADB > \angle ADC \text{ (Therefore, } \angle C > \angle B \text{)}$$

Hence, proved

10. Question

In $\triangle ABC$, $BD \perp AC$ and $CE \perp AB$. If BD and CE intersect at O , prove that $\angle BOC = 180^\circ - \angle A$.

Answer



BD perpendicular to AC

And,

CE perpendicular to AB

In $\triangle BCE$

$$\angle E + \angle B + \angle ECB = 180^\circ$$

$$90^\circ + \angle B + \angle ECB = 180^\circ$$

$$\angle B + \angle ECB = 90^\circ$$

$$\angle B = 90^\circ - \angle ECB \text{(i)}$$

In $\triangle BCD$

$$\angle D + \angle C + \angle DBC = 180^\circ$$

$$90^\circ + \angle C + \angle DBC = 180^\circ$$

$$\angle C + \angle DBC = 90^\circ$$

$$\angle C = 90^\circ - \angle DBC \dots\dots(ii)$$

Adding (i) and (ii), we get

$$\angle B + \angle C = 180^\circ (\angle ECB + \angle DBC)$$

$$\angle 180^\circ - \angle A = 180^\circ (\angle ECB + \angle DBC)$$

$$\angle A = \angle ECB + \angle DBC$$

$$\angle A = \angle OCB + \angle OBC \text{ (Therefore, } \angle ECB = \angle OCB \text{ and } \angle DCB = \angle OCB) \dots (iii)$$

In $\triangle BOC$

$$\angle BOC + (\angle OBC + \angle OCB) = 180^\circ$$

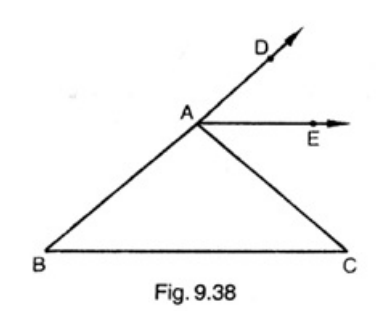
$$\angle BOC + \angle A = 180^\circ \text{ [From (iii)]}$$

$$\angle BOC = 180^\circ - \angle A$$

Hence, proved

11. Question

In Fig. 9.38, AE bisects $\angle CAD$ and $\angle B = \angle C$. Prove that $AE \parallel BC$.



Answer

Given,

AE bisects $\angle CAD$

$$\angle B = \angle C$$

In $\triangle ABC$

$$\angle CAD = \angle B + \angle C$$

$$\angle CAD = \angle C + \angle C$$

$$\angle CAD = 2\angle C$$

$$\angle 1 + \angle 2 = 2\angle C \text{ (Therefore, } \angle CAD = \angle 1 + \angle 2)$$

$$\angle 2 + \angle 2 = 2\angle C \text{ (Therefore, } AE \text{ bisects } \angle CAD)$$

$$2\angle 2 = 2\angle C$$

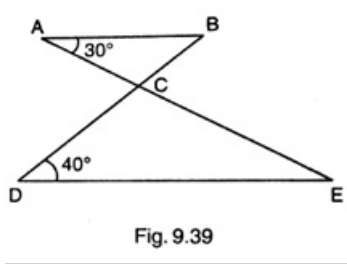
$$\angle 2 = \angle C \text{ (Alternate angles)}$$

Therefore, $AE \parallel BC$

Hence, proved

12. Question

In Fig. 9.39, $AB \parallel DE$. Find $\angle ACD$.



Answer

Since,

$AB \parallel DE$

$\angle ABC = \angle CDE$ (Alternate angles)

$$\angle ABC = 40^\circ$$

In $\triangle ABC$

$$\angle A + \angle B + \angle ACB = 180^\circ$$

$$30^\circ + 40^\circ + \angle ACB = 180^\circ$$

$$\angle ACB = 180^\circ - 70^\circ$$

$$= 110^\circ \text{ (i)}$$

Now,

$$\angle ACD + \angle ACB = 180^\circ \text{ (Linear pair)}$$

$$\angle ACD + 110^\circ = 180^\circ \text{ [From (i)]}$$

$$\angle ACD = 180^\circ - 110^\circ$$

$$= 70^\circ$$

Hence, $\angle ACD = 70^\circ$.

13. Question

Which of the following statements are true (T) and which are false (F).

- (i) Sum of the three angles of a triangle is 180° .
- (ii) A triangle can have two right angles.
- (iii) All the angles of a triangle can be less than 60° .
- (iv) All the angles of a triangle can be greater than 60° .
- (v) All the angles of a triangle can be equal to 60° .
- (vi) A triangle can have two obtuse angles.
- (vii) A triangle can have at most one obtuse angles.
- (viii) If one angle of a triangle is obtuse, then it cannot be a right angled triangle.
- (ix) An exterior angle of a triangle is less than either of its interior opposite angles.
- (x) An exterior angle of a triangle is equal to the sum of the two interior opposite angles.
- (xi) An exterior angle of a triangle is greater than the opposite interior angles.

Answer

- (i) True
- (ii) False
- (iii) False
- (iv) False
- (v) True
- (vi) False
- (vii) True
- (viii) True
- (ix) False
- (x) True
- (xi) True

14. Question

Fill in the blanks to make the following statements true :

- (i) Sum of the angles of a triangle is
- (ii) An exterior angle of a triangle is equal to the two opposite angles.
- (iii) An exterior angle of a triangle is alwaysthan either of the interior opposite angles.
- (iv) A triangle cannot have more thanright angles.
- (v) A triangles cannot have more than obtuse angles.

Answer

- (i) 180°
- (ii) Interior
- (iii) Greater
- (iv) One
- (v) One

CCE - Formative Assessment**1. Question**

Define a triangle.

Answer

A plane figure with three straight sides and three angles.

2. Question

Write the sum of the angles of an obtuse triangle.

Answer

A triangle where one of the internal angles is obtuse (greater than 90 degrees) is called an obtuse triangle. The sum of angles of obtuse triangle is also 180° .

3. Question

In ΔABC , if $\angle B = 60^\circ$, $\angle C = 80^\circ$ and the bisectors of angles $\angle ABC$ and $\angle ACB$ meet at a point O , then find the measure of $\angle BOC$.

Answer

In $\triangle BOC$,

$$\angle BOC + \angle OCB + \angle OBC = 180^\circ$$

$$\angle BOC + \frac{1}{2} \times (80) + \frac{1}{2} \times (40) = 180^\circ$$

$$\angle BOC = 180^\circ - 70^\circ$$

$$\angle BOC = 110^\circ$$

14. Question

If the angles of a triangle are in the ratio 2: 1: 3, then find the measure of smallest angle.

Answer

Let,

$$\angle 1 = 2k, \angle 2 = k \text{ and } \angle 3 = 3k$$

$$\angle 1 + \angle 2 + \angle 3 = 180^\circ$$

$$6k = 180$$

$$k = 30^\circ$$

Therefore, minimum angle be $\angle 2 = k = 30^\circ$.

5. Question

If the angles A , B and C of $\triangle ABC$ satisfy the relation $B - A = C - B$, then find the measure of $\angle B$.

Answer

Given,

In $\triangle ABC$,

$$B - A = C - B$$

$$B + B = A + C$$

$$2B = A + C \text{ (i)}$$

Now,

$$A + B + C = 180^\circ$$

$$B = 180 - (A + C) \text{ (ii)}$$

Using (i) in (ii), we get

$$B = 180 - 2B$$

$$3B = 180^\circ$$

$$B = 60^\circ$$

6. Question

In $\triangle ABC$, if bisectors of $\angle ABC$ and $\angle ACB$ intersect at O angle of 120° , then find the measure of $\angle A$.

Answer

In $\triangle BOC$

$$\angle BOC + \angle OBC + \angle OCB = 180^\circ$$

$$120^\circ + \frac{1}{2}\angle B + \frac{1}{2}\angle C = 180^\circ$$

$$\frac{1}{2}(\angle B + \angle C) = 60^\circ$$

$$\angle B + \angle C = 120^\circ \text{ (i)}$$

In $\triangle ABC$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + 120^\circ = 180^\circ \text{ [From (i)]}$$

$$\angle A = 60^\circ$$

7. Question

State exterior angle theorem.

Answer

If a side of a triangle is produced, the exterior angle so formed is equal to the sum of the two interior opposite angles.

8. Question

If the side BC of $\triangle ABC$ is produced on both sides, then write the difference between the sum of the exterior angles so formed and $\angle A$.

Answer

Given that,

BC produced on both sides

We know that,

$$\angle A + \angle ABC + \angle ACB = 180^\circ \text{ (i)}$$

$$\angle ABD = \angle A + \angle ACB \text{ (Exterior angle theorem) (ii)}$$

$$\angle ACE = \angle A + \angle ABC \text{ (Exterior angle theorem) (iii)}$$

Adding (ii) and (iii), we get

$$\angle ABD + \angle ACE = \angle A + (\angle A + \angle ACB + \angle ABC)$$

$$\angle ABD + \angle ACE = \angle A + 180^\circ$$

$$(\angle ABD + \angle ACE) - \angle A = 180^\circ$$

Thus, between the sum of the exterior angles so formed and $\angle A$ is 180° .

9. Question

In a triangle ABC , if $AB = AC$ and AB is produced to D such that $BD = BC$, find $\angle ACD$: $\angle ADC$.

Answer

Given,

$AB = AC$ and,

$BD = BC$

$$\angle 2 = \angle 3 \text{ (Since, } AB = AC)$$

$$\angle 4 = \angle 5 \text{ (Since, } BD = BC)$$

$$\frac{\angle ACD}{\angle ADC} = \frac{\angle 3 + \angle 4}{\angle 5} \text{ (i)}$$

In $\triangle BDC$

$$\angle 2 = \angle 4 + \angle 5$$

$$\angle 2 = 2\angle 4 \text{ (Since, } \angle 4 = \angle 5)$$

$$\angle 3 = 2\angle 4 \text{ (Since, } \angle 3 = \angle 2)$$

$$\frac{\angle ACD}{\angle ADC} = \frac{\frac{\angle 3 + \angle 3}{2}}{\frac{\angle 3}{2}}$$

$$= \frac{3}{1}$$

Thus, $\angle ACD : \angle ADC = 3 : 1$

10. Question

The sum of two angles of a triangle is equal to its third angle. Determine the measure of the third angle.

Answer

Let,

$\angle 1$, $\angle 2$ and $\angle 3$ be the angles of a triangle.

$$\angle 1 + \angle 2 = \angle 3 \text{ (Given) (i)}$$

We know that,

$$\angle 1 + \angle 2 + \angle 3 = 180^\circ$$

$$\angle 3 + \angle 3 = 180^\circ \text{ [From (i)]}$$

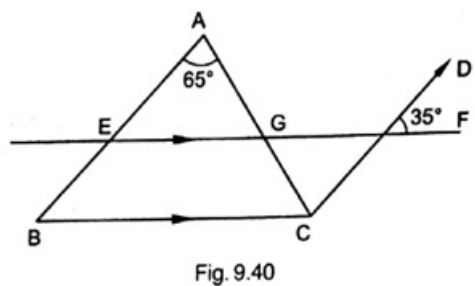
$$2\angle 3 = 180^\circ$$

$$\angle 3 = 90^\circ$$

Thus, third angle is 90° .

11. Question

In Fig. 9.40, if $AB \parallel CD$, $EF \parallel BC$, $\angle BAC = 65^\circ$ and $\angle DHF = 35^\circ$, find $\angle AGH$.



Answer

Given,

$AB \parallel CD$ and,

$EF \parallel BC$

$$\angle BAC = 65^\circ \text{ and } \angle DHF = 35^\circ$$

$$\angle BAC = \angle ACD \text{ (Alternate angles)}$$

$$\angle ACD = 65^\circ$$

$$\angle DHF = \angle GHC \text{ (Vertically opposite angles)}$$

$$\angle GHC = 35^\circ$$

In $\triangle AGH$

$$\angle GCH + \angle GHC + \angle HGC = 180^\circ$$

$$65^\circ + 35^\circ + \angle HGC = 180^\circ$$

$$\angle HGC = 80^\circ$$

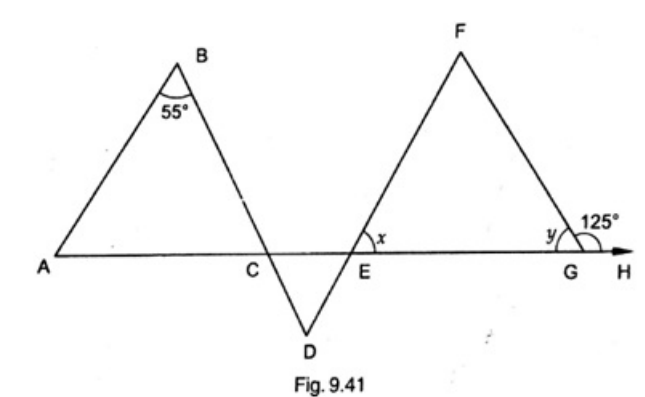
$$\angle AGH + \angle HGC = 180^\circ \text{ (Linear pair)}$$

$$\angle AGH + 80^\circ = 180^\circ$$

$$\angle AGH = 100^\circ$$

12. Question

In Fig. 9.41, if $AB \parallel DE$ and $BD \parallel FG$ such that $\angle FGH = 125^\circ$ and $\angle B = 55^\circ$, find a and y .



Answer

Given,

$AB \parallel DE$ and,

$BD \parallel FG$

$$\angle FGH + \angle FGE = 180^\circ \text{ (Linear pair)}$$

$$125^\circ + y = 180^\circ$$

$$y = 55^\circ$$

$$\angle ABC = \angle BDE \text{ (Alternate angles)}$$

$$\angle BDE = \angle FGE = 55^\circ \text{ (Alternate angles)}$$

$$\angle FGE + \angle FEG = 125^\circ \text{ (By exterior angle theorem)}$$

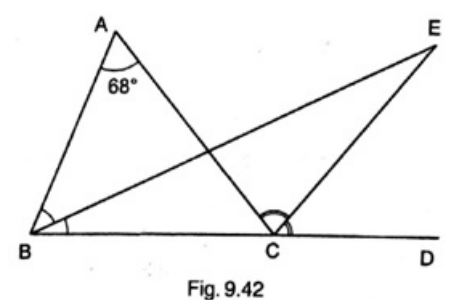
$$55^\circ + \angle FEG = 125^\circ$$

$$\angle FEG = x = 70^\circ$$

Thus, $x = 70^\circ$ and $y = 55^\circ$.

13. Question

In Fig. 9.42, side BC of $\triangle ABC$ is produced to point D such that bisectors of $\angle ABC$ and $\angle ACD$ meet at a point E . If $\angle BAC = 68^\circ$, find $\angle BEC$.



Answer

By exterior angle theorem,

$$\angle ACD = \angle A + \angle B$$

$$\angle ACD = 68^\circ + \angle B$$

$$\frac{1}{2} \angle ACD = 34^\circ + \frac{1}{2} \angle B$$

$$34^\circ = \frac{1}{2} \angle ACD - \angle EBC \text{ (i)}$$

Now,

In $\triangle BEC$

$$\angle ECD = \angle EBC + \angle E$$

$$\angle E = \angle ECD - \angle EBC$$

$$\angle E = \frac{1}{2} \angle ACD - \angle EBC \text{ (ii)}$$

From (i) and (ii), we get

$$\angle E = 34^\circ$$

1. Question

If all the three angles of a triangle are equal, then each one of them is equal to

- A. 90°
- B. 45°
- C. 60°
- D. 30°

Answer

Let,

A, B and C be the angles of $\triangle ABC$

$$A = B = C \text{ (Given)}$$

We know that,

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + \angle A + \angle A = 180^\circ$$

$$3\angle A = 180^\circ$$

$$\angle A = 60^\circ$$

Therefore,

$$\angle A = \angle B = \angle C = 60^\circ$$

Thus, each angle is equal to 60° .

2. Question

If two acute angles of a right triangle are equal, then each is equal to

- A. 30°
- B. 45°
- C. 60°

D. 90°

Answer

Given that the triangle is acute.

So, $\angle 1$, $\angle 2$ and $\angle 3$ be the angles of the triangle.

$$\angle 1 = 90^\circ \text{ (Given)}$$

$$\angle 2 = \angle 3$$

We know that,

$$\angle 1 + \angle 2 + \angle 3 = 180^\circ$$

$$90^\circ + \angle 2 + \angle 2 = 180^\circ$$

$$2\angle 2 = 180^\circ - 90^\circ$$

$$\angle 2 = 45^\circ$$

Therefore, $\angle 2 = \angle 3 = 45^\circ$

Thus, each acute angle is equal to 45° .

3. Question

An exterior angle of a triangle is equal to 100° and two interior opposite angles are equal, each of these angles is equal to

A. 75°

B. 80°

C. 40°

D. 50°

Answer

Let, $\angle 1$ and $\angle 2$ be two opposite interior angles and $\angle 3$ be exterior angle.

According to question,

$$\angle 1 + \angle 2 = \angle 3$$

$$\angle 1 + \angle 1 = 100^\circ$$

$$2\angle 1 = 100^\circ$$

$$\angle 1 = 50^\circ$$

Therefore, $\angle 1 = \angle 2 = 50^\circ$

Thus, of these angles is equal to 50° .

4. Question

If one angle of a triangle is equal to the sum of the other two angles, then the triangle is

A. An isosceles triangle

B. An obtuse triangle

C. An equilateral triangle

D. A right triangle

Answer

A right triangle

5. Question

Side BC of a triangle ABC has been produced to a point D such that $\angle ACD = 120^\circ$. If $\angle B = \frac{1}{2} \angle A$, then $\angle A$ is equal to

- A. 80°
- B. 75°
- C. 60°
- D. 90°

Answer

By exterior angle theorem:

$$\angle ACD = \angle A + \angle B$$

$$120^\circ = \angle A + \frac{1}{2} \angle A$$

$$120^\circ = \frac{2\angle A + \angle B}{2}$$

$$240^\circ = 3\angle A$$

$$\angle A = 80^\circ$$

6. Question

In $\triangle ABC$ $\angle B = \angle C$ and ray AX bisects the exterior angle $\angle DAC$. If $\angle DAX = 70^\circ$, then $\angle ACB =$

- A. 35°
- B. 90°
- C. 70°
- D. 55°

Answer

AX bisects $\angle DAC$

$$\angle CAD = 2 * \angle DAX$$

$$\angle CAD = 2 * 70^\circ$$

$$= 140^\circ$$

By exterior angle theorem,

$$\angle CAD = \angle B + \angle C$$

$$140^\circ = \angle C + \angle C \text{ (Therefore, } \angle B = \angle C \text{)}$$

$$140^\circ = 2\angle C$$

$$\angle C = 70^\circ$$

Therefore, $\angle C = \angle ACB = 70^\circ$

7. Question

In a triangle, an exterior angle at a vertex is 95° and its one of the interior opposite angle is 55° , then the measure of the other interior angle is

- A. 55°
- B. 85°
- C. 40°

D. 9.0°

Answer

We know that,

In a triangle an exterior angle is equal to sum of two interior opposite angle.

Let, the required interior opposite angle be x .

$$x + 55^\circ = 95^\circ$$

$$x = 95^\circ - 55^\circ$$

$$= 40^\circ$$

Thus, other interior angle is 40° .

8. Question

If the sides of a triangle are produced in order, then the sum of the three exterior angles so formed is

A. 90°

B. 180°

C. 270°

D. 360°

Answer

Let, ABC be a triangle and AB, BC and AC produced to D, E and F respectively.

$$\angle A + \angle B + \angle C = 180^\circ \text{ (i)}$$

$$\angle CBD = \angle C + \angle A \text{ (Exterior angle theorem) (ii)}$$

$$\angle ACE = \angle A + \angle B \text{ (Exterior angle theorem) (iii)}$$

$$\angle BAF = \angle B + \angle C \text{ (Exterior angle theorem) (iv)}$$

Adding (ii), (iii) and (iv) we get

$$\angle CBD + \angle ACE + \angle BAF = 2\angle A + 2\angle B + 2\angle C$$

$$\angle CBD + \angle ACE + \angle BAF = 2(\angle A + \angle B + \angle C)$$

$$\angle CBD + \angle ACE + \angle BAF = 2 * 180^\circ$$

$$\angle CBD + \angle ACE + \angle BAF = 360^\circ$$

Thus, sum of all three exterior angles is 360° .

9. Question

In $\triangle ABC$, if $\angle A = 100^\circ$ AD bisects $\angle A$ and $AD \perp BC$. Then, $\angle B =$

A. 50°

B. 90°

C. 40°

D. 100°

Answer

Given,

AD perpendicular to BC

$$\angle A = 100^\circ$$

In $\triangle ADB$,

$$\angle ADB + \angle B + \angle DAC = 180^\circ$$

$$90^\circ + \angle B + \frac{1}{2}\angle A = 180^\circ$$

$$\angle B + \frac{1}{2} * 100^\circ = 180^\circ - 90^\circ$$

$$\angle B + 50^\circ = 90^\circ$$

$$\angle B = 40^\circ$$

10. Question

An exterior angle of a triangle is 108° and its interior opposite angles are in the ratio 4 : 5. The angles of the triangle are

A. $48^\circ, 60^\circ, 72^\circ$

B. $50^\circ, 60^\circ, 70^\circ$

C. $52^\circ, 56^\circ, 72^\circ$

D. $42^\circ, 60^\circ, 76^\circ$

Answer

Let $\angle 1$, $\angle 2$ and $\angle 3$ be the angles of the triangle and $\angle 4$ be its exterior angle.

$$\angle 4 = 108^\circ \text{ (Given)}$$

$$\angle 1 : \angle 2 = 4 : 5 \text{ (Given)}$$

$$\text{Let, } \angle 1 = 4k$$

$$\angle 2 = 5k$$

Now,

$$\angle 1 + \angle 2 = 108^\circ \text{ (Exterior angle theorem)}$$

$$4k + 5k = 108^\circ$$

$$9k = 108^\circ$$

$$k = 12^\circ$$

Thus,

$$\angle 1 = 4 * 12 = 48^\circ$$

$$\angle 2 = 5 * 12 = 60^\circ$$

We know that,

$$\angle 1 + \angle 2 + \angle 3 = 180^\circ$$

$$48^\circ + 60^\circ + \angle 3 = 180^\circ$$

$$108^\circ + \angle 3 = 180^\circ$$

$$\angle 3 = 180^\circ - 108^\circ$$

$$= 72^\circ$$

Thus, angles of triangle are $48^\circ, 60^\circ, 72^\circ$.

11. Question

In a $\triangle ABC$, If $\angle A = 60^\circ$, $\angle B = 80^\circ$ and the bisectors of $\angle B$ and $\angle C$ meet at O , then $\angle BOC =$

- A. 60°
- B. 120°
- C. 150°
- D. 30°

Answer

In $\triangle ABC$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$60^\circ + \angle B + \angle C = 180^\circ$$

$$\angle B + \angle C = 120^\circ$$

$$\frac{1}{2} \angle B + \frac{1}{2} \angle C = 60^\circ \text{ (i)}$$

In $\triangle BOC$

$$\angle BOC + \angle OBC + \angle OCB = 180^\circ$$

$$\angle BOC + \frac{1}{2} \angle B + \frac{1}{2} \angle C = 180^\circ$$

$$\angle BOC + \frac{1}{2} (\angle B + \angle C) = 180^\circ$$

$$\angle BOC + 60^\circ = 180^\circ \text{ [From (i)]}$$

$$\angle BOC = 120^\circ$$

12. Question

If the bisectors of the acute angles of a right triangle meet at O , then the angle at O between the two bisectors is

- A. 45°
- B. 95°
- C. 135°
- D. 90°

Answer

Let ABC is an acute angled triangle.

$$\angle B = 90^\circ$$

We know that,

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + 90^\circ + \angle C = 180^\circ$$

$$\angle A + \angle C = 90^\circ \text{ (i)}$$

In $\triangle AOC$

$$\angle AOC + \angle ACD + \angle CAD = 180^\circ$$

$$\angle AOC + \frac{1}{2} \angle C + \frac{1}{2} \angle A = 180^\circ$$

$$\angle AOC + \frac{1}{2} (\angle A + \angle C) = 180^\circ$$

$$\angle AOC + \frac{1}{2} * 90^\circ = 180^\circ \text{ [From (i)]}$$

$$\angle AOC + 45^\circ = 180^\circ$$

$$\angle AOC = 180^\circ - 45^\circ$$

$$= 135^\circ$$

Thus, the angle at O between two bisectors is equal to 135° .

13. Question

Line segments AB and CD intersect at O such that $AC \parallel DB$. If $\angle CAB = 45^\circ$ and $\angle CDB = 55^\circ$, then $\angle BOD =$

A. 100°

B. 80°

C. 90°

D. 135°

Answer

$$AC \parallel BD$$

$$\angle CAD = 45^\circ$$

$$\angle CDB = 55^\circ$$

$$\angle 2 = \angle CAD \text{ (Alternate angle)}$$

$$\angle 2 = 45^\circ$$

In $\triangle BOD$

$$\angle BOD + \angle 2 + \angle CDB = 180^\circ$$

$$\angle BOD + 45^\circ + 55^\circ = 180^\circ$$

$$\angle BOD + 100^\circ = 180^\circ$$

$$\angle BOD = 180^\circ - 100^\circ$$

$$= 80^\circ$$

14. Question

The bisectors of exterior angles at B and C of $\triangle ABC$ meet at O , if $\angle A = x^\circ$, then $\angle BOC =$

A. $90^\circ + \frac{x^\circ}{2}$

B. $90^\circ - \frac{x^\circ}{2}$

C. $180^\circ + \frac{x^\circ}{2}$

D. $180^\circ - \frac{x^\circ}{2}$

Answer

$$\angle OBC = 180^\circ - \angle B - \frac{1}{2}(180^\circ - \angle B)$$

$$\angle OBC = 90^\circ - \frac{1}{2}\angle B$$

And,

$$\angle OCB = 180^\circ - \angle C - \frac{1}{2}(180^\circ - \angle C)$$

$$\angle OCB = 90^\circ - \frac{1}{2} \angle C$$

In $\triangle BOC$

$$\angle BOC + \angle OCB + \angle OBC = 180^\circ$$

$$\angle BOC + 90^\circ - \frac{1}{2} \angle C + 90^\circ - \frac{1}{2} \angle B = 180^\circ$$

$$\angle BOC = \frac{1}{2} (\angle B + \angle C)$$

$$\angle BOC = \frac{1}{2} (180^\circ - \angle A) \text{ [From } \triangle ABC]$$

$$\angle BOC = 90^\circ - \frac{1}{2} \angle A$$

$$\angle BOC = 90^\circ - \frac{x}{2}$$

15. Question

In $\triangle ABC$, $\angle A = 50^\circ$ and BC is produced to a point D . If the bisectors of $\angle ABC$ and $\angle ACD$ meet at E , then $\angle E =$

- A. 25°
- B. 50°
- C. 100°
- D. 75°

Answer

In $\triangle ABC$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$50^\circ + \angle B + \angle C = 180^\circ$$

$$\angle B + \angle C = 180^\circ - 50^\circ$$

$$\angle B + \angle C = 130^\circ \text{ (i)}$$

In $\triangle BEC$

$$\angle E + \angle BCE + \angle EBC = 180^\circ$$

$$\angle E + 180^\circ - \left(\frac{1}{2} \angle ACD\right) + \frac{1}{2} \angle B = 180^\circ \text{ (ii)}$$

By exterior angle theorem,

$$\angle ACD = 50^\circ + \angle B$$

Putting value of $\angle ACD$ in (ii), we get

$$\angle E + 180^\circ - \frac{1}{2} (50^\circ + \angle B) + \frac{1}{2} \angle B = 180^\circ$$

$$\angle E - 25^\circ - \frac{1}{2} \angle B + \frac{1}{2} \angle B = 0$$

$$\angle E - 25^\circ = 0$$

$$\angle E = 25^\circ$$

16. Question

The side BC of $\triangle ABC$ is produced to a point D . The bisector of $\angle A$ meets side BC in L . If $\angle ABC = 30^\circ$ and $\angle ACD = 115^\circ$, then $\angle ALC =$

- A. 85°

B. $72\frac{1}{2}^\circ$

C. 145°

D. None of these

Answer

Given,

$$\angle ABC = 30^\circ$$

$$\angle ACD = 115^\circ$$

By exterior angle theorem,

$$\angle ACD = \angle A + \angle B$$

$$115^\circ = \angle A + 30^\circ$$

$$\angle A = 85^\circ$$

$$\angle ACD + \angle ACL = 180^\circ \text{ (Linear pair)}$$

$$\angle ACL = 65^\circ$$

In $\triangle ALC$

$$\angle ALC + \angle LAC + \angle ACL = 180^\circ$$

$$\angle ALC + \frac{1}{2}\angle A + 65^\circ = 180^\circ$$

$$\angle ALC = 72.5^\circ$$

17. Question

In Fig. 9.43, if $EC \parallel AB$, $\angle ECD = 70^\circ$ and $\angle BDO = 20^\circ$, then $\angle OBD$ is

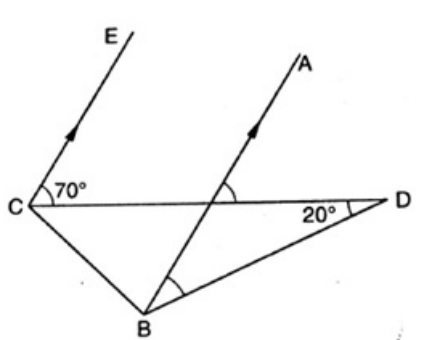


Fig. 9.43

A. 20°

B. 50°

C. 60°

D. 70°

Answer

Given,

$$EC \parallel AB$$

$$\angle ECD = 70^\circ$$

$$\angle BDO = 20^\circ$$

Since,

$EC \parallel AB$

And, OC cuts them so

$\angle ECD = \angle 1$ (Alternate angle)

$$\angle 1 = 70^\circ$$

$$\angle 1 + \angle 3 = 180^\circ \text{ (Linear pair)}$$

$$\angle 3 = 110^\circ$$

In $\triangle BOD$

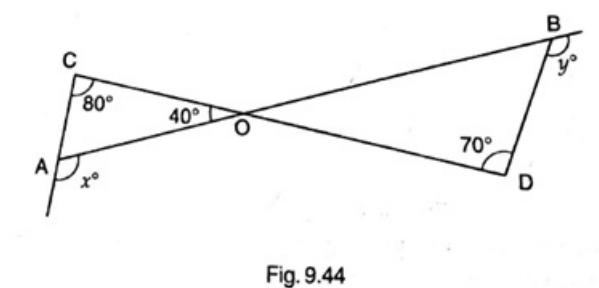
$$\angle BOD + \angle OBD + \angle BDO = 180^\circ$$

$$\angle 3 + \angle ODB + 20^\circ = 180^\circ$$

$$\angle ODB = 50^\circ$$

18. Question

In Fig. 9.44, $x + y =$



A. 270

B. 230

C. 210

D. 190°

Answer

By exterior angle theorem,

In $\triangle AOC$

$$\angle OCA + \angle AOC = x$$

$$x = 80^\circ + 40^\circ$$

$$= 120^\circ$$

$$\angle AOC = \angle DOB \text{ (Vertically opposite angle)}$$

$$\angle DOB = 40^\circ$$

By exterior angle theorem,

In $\triangle BOD$

$$y = \angle BOD + \angle ODB$$

$$= 40^\circ + 70^\circ$$

$$= 110^\circ$$

$$\text{Now, } x + y = 230^\circ$$

19. Question

If the measures of angles of a triangle are in the ratio of 3 : 4 : 5, what is the measure of the smallest angle of the triangle?

- A. 25°
B. 30°
C. 45°
D. 60°

Answer

Let,

$\angle 1$, $\angle 2$ and $\angle 3$ be the angles of the triangle which are in the ratio 3: 4: 5 respectively.

$$\angle 1 = 3k$$

$$L2 = 4k$$

$$\angle 3 = 5k$$

We know that,

$$\angle 1 + \angle 2 + \angle 3 = 180^\circ$$

$$3k + 4k + 5k = 180^\circ$$

$$k = 15^0$$

So,

$$\angle 1 = 3 * 15^{\circ} = 45^{\circ}$$

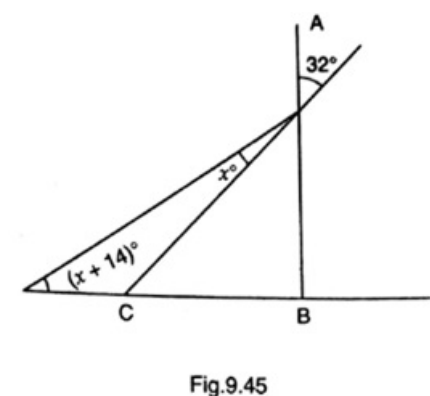
$$\angle 2 = 4 * 15^{\circ} = 60^{\circ}$$

$$\angle 3 = 5 * 15^{\circ} = 75^{\circ}$$

Thus, smallest angle is 45° .

20. Question

In Fig. 9.45, if $AB \perp BC$, then $x =$



- A. 18
B. 22
C. 25
D. 32

Answer

Given,

AB is perpendicular to BC so $\angle B = 90^\circ$

$\angle CED = 32^\circ$ (Vertically opposite angles)

In $\triangle BDE$

$$\angle BDE + \angle BED + \angle DBE = 180^\circ$$

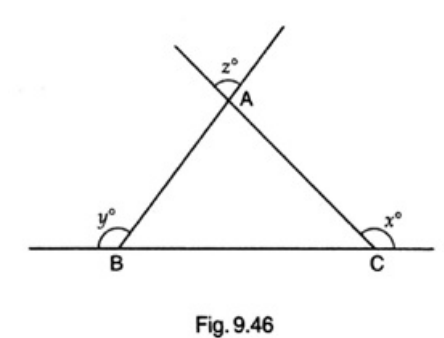
$$x + 14^\circ + 32^\circ + x + 90^\circ = 180^\circ$$

$$2x = 44^\circ$$

$$x = 22^\circ$$

21. Question

In Fig. 9.46, what is z in terms of x and y ?



- A. $x + y + 180$
- B. $x + y - 180$
- C. $180^\circ - (x + y)$
- D. $x + y + 360^\circ$

Answer

In $\triangle ABC$ given that,

$$x = \angle A + \angle B \text{ (Exterior angles)}$$

$$z = \angle A \text{ (Vertically opposite angles)}$$

$$y = \angle A + \angle C \text{ (Exterior angles)}$$

We know that,

$$\angle A + \angle B + \angle C = 180^\circ$$

$$z + x - \angle A + y - \angle A = 180^\circ$$

$$-z = 180^\circ - x - y$$

$$z = x + y - 180^\circ$$

22. Question

In Fig. 9.47, for which value of x is $l_1 \parallel l_2$?

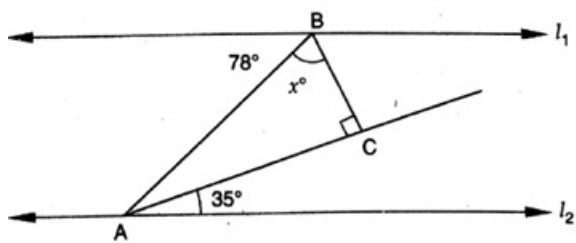


Fig. 9.47

- A. 37
- B. 43
- C. 45
- D. 47

Answer

Since,

$$l_1 \parallel l_2$$

And,

AB cuts them so,

$$\angle DBA = \angle BAE = 78^\circ$$

$$\angle BAC + 35^\circ = 78^\circ$$

$$\angle BAC = 43^\circ$$

In $\triangle ABC$

$$\angle BAC + \angle ABC + \angle ACB = 180^\circ$$

$$43^\circ + x + 90^\circ = 180^\circ$$

$$x = 47^\circ$$

23. Question

In Fig. 9.48, what is y in terms of x ?

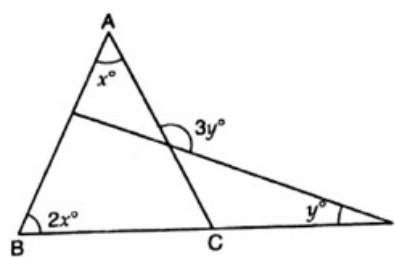


Fig. 9.48

- A. $\frac{3}{2}x$
- B. $\frac{4}{3}x$
- C. x
- D. $\frac{3}{4}x$

Answer

In $\triangle ABC$

$$x + 2x + \angle ACB = 180^\circ$$

$$\angle ACB = 180^\circ - 3x \text{ (i)}$$

In $\triangle ECD$

$$y + 180^\circ - 3y + \angle ECD = 180^\circ$$

$$y + 180^\circ - 3y + 180^\circ - \angle ACB = 180^\circ$$

$$y = \frac{3}{2}x$$

24. Question

In Fig. 9.49, if $l_1 \parallel l_2$, the value of x is

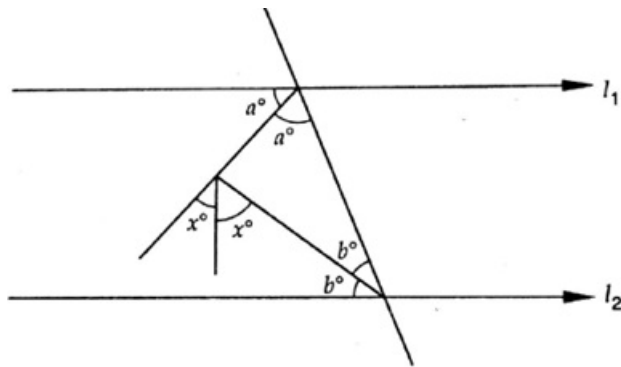


Fig. 9.49

A. $22\frac{1}{2}$

B. 30

C. 45

D. 60

Answer

Since,

$$l_1 \parallel l_2$$

And PQ cuts them

$$\angle DPQ + \angle PQE = 180^\circ \text{ (Consecutive interior angles)}$$

$$a + a + b + b = 180^\circ$$

$$2(a + b) = 180^\circ$$

$$a + b = 90^\circ \text{ (i)}$$

In $\triangle APQ$

$$\angle PAQ + a + b = 180^\circ$$

$$\angle PAQ = 90^\circ$$

$$\angle PAQ + x + x = 180^\circ \text{ (Linear pair)}$$

$$90^\circ + 2x = 180^\circ$$

$$x = 45^\circ$$

25. Question

In Fig. 9.50, what is value of x ?

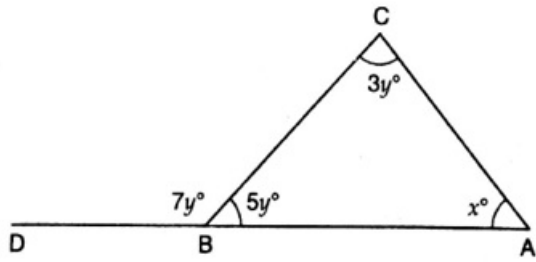


Fig. 9.50

- A. 35
- B. 45
- C. 50
- D. 60

Answer

In $\triangle ABC$

$$\angle ABC + \angle ACB + \angle CAB = 180^\circ$$

$$5y + 3y + x = 180^\circ$$

$$8y + x = 180^\circ \text{ (i)}$$

$$\angle ABC + \angle CBD = 180^\circ \text{ (Linear pair)}$$

$$5y + 7y = 180^\circ$$

$$y = 15^\circ$$

Putting values of y in (i), we get

$$8 * 15 + x^\circ = 180^\circ$$

$$x = 60^\circ$$

26. Question

In $\triangle RST$ (See Fig. 9.51), what is value of x ?

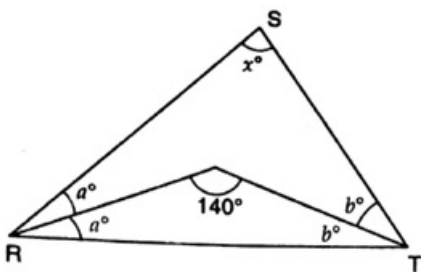


Fig. 9.51

- A. 40
- B. 90°
- C. 80°
- D. 100

Answer

In $\triangle ROT$

$$\angle ROT + \angle RTO + \angle TRO = 180^\circ$$

$$140^\circ + b + a = 180^\circ$$

$$a + b = 40^\circ \text{ (i)}$$

In $\triangle RST$

$$\angle RST + \angle SRT + \angle STR = 180^\circ$$

$$x + a + a + b + b = 180^\circ$$

$$x + 2(a + b) = 180^\circ$$

$$x + 80^\circ = 180^\circ$$

$$x = 100^\circ$$

27. Question

In Fig. 9.52, the value of x is

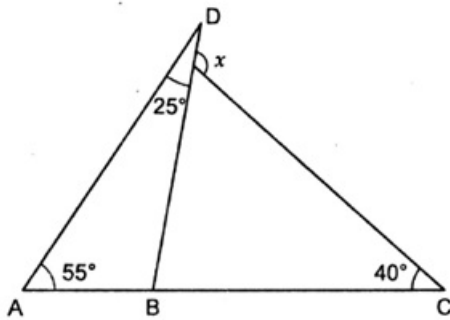


Fig. 9.52

A. 65°

B. 80°

C. 95°

D. 120°

Answer

In $\triangle ABD$

$$\angle A + \angle ABD + \angle BDA = 180^\circ$$

$$\angle ABD = 100^\circ$$

In $\triangle EBC$

$$\angle EBC + \angle ECB + \angle CEB = 180^\circ$$

$$-100^\circ + 40^\circ + \angle CEB = 0^\circ$$

$$\angle CEB = 60^\circ$$

$$\angle CEB + \angle CED = 180^\circ \text{ (Linear pair)}$$

$$60^\circ + x = 180^\circ$$

$$x = 120^\circ$$

28. Question

In Fig. 9.53, if $BP \parallel CQ$ and $AC = BC$, then the measure of x is

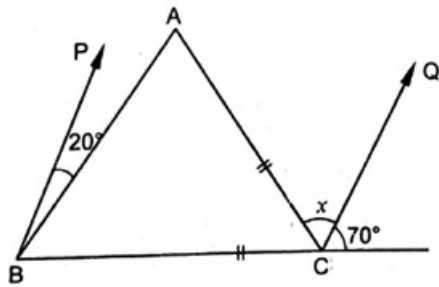


Fig. 9.53

- A. 20°
- B. 25°
- C. 30°
- D. 35°

Answer

Given,

$BP \parallel CQ$

And,

$AC = BC$

$\angle A = \angle ABC$ (Since, $AC = BC$)

In $\triangle ABC$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + \angle A + \angle C = 180^\circ$$

$$2\angle A + \angle C = 180^\circ \text{ (i)}$$

$$\angle ACB + \angle ACQ + \angle QCD = 180^\circ \text{ (Linear pair)}$$

$$\angle ACB + x = 110^\circ \text{ (ii)}$$

$$\angle PBC + \angle BCQ = 180^\circ \text{ (Co. interior angle)}$$

$$20^\circ + \angle A + \angle ACB + x = 180^\circ$$

$$\angle A = 50^\circ \text{ (iii)}$$

Using (iii) in (i), we get

$$2 * 50^\circ + \angle ACB = 180^\circ$$

$$\angle ACB = 80^\circ$$

Using value of $\angle ACB$ in (ii) we get

$$80^\circ + x = 110^\circ$$

$$x = 30^\circ$$

29. Question

In Fig. 9.54, AB and CD are parallel lines and transversal EF intersects them at P and Q respectively. If

$\angle APR = 25^\circ$, $\angle RQC = 30^\circ$ and $\angle CQF = 65^\circ$, then

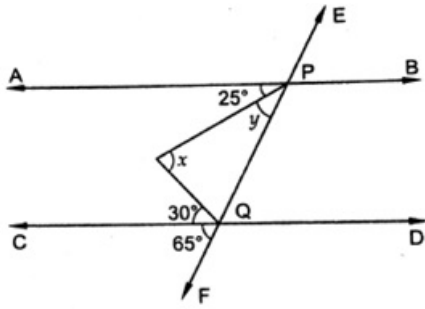


Fig. 9.54

- A. $x = 55^\circ$, $y = 40^\circ$
- B. $x = 50^\circ$, $y = 45^\circ$
- C. $x = 60^\circ$, $y = 35^\circ$
- D. $x = 35^\circ$, $y = 60^\circ$

Answer

Given,

$AB \parallel CD$

And, EF cuts them

$$\text{So, } 30^\circ + 65^\circ + \angle PQR = 180^\circ$$

$$95^\circ + \angle PQR = 180^\circ$$

$$\angle PQR = 85^\circ$$

$$\angle APQ + \angle PQC = 180^\circ \text{ (Co. interior angle)}$$

$$25^\circ + y + 85^\circ + 30^\circ = 180^\circ$$

$$y = 40^\circ$$

In $\triangle PQR$

$$\angle PQR + \angle PRQ + \angle QPR = 180^\circ$$

$$85^\circ + x + y = 180^\circ$$

$$x = 55^\circ$$

Thus, $x = 55^\circ$ and $y = 40^\circ$

30. Question

The base BC of triangle ABC is produced both ways and the measure of exterior angles formed are 94° and 126° . Then, $\angle BAC =$

- A. 94°
- B. 54°
- C. 40°
- D. 44°

Answer

Given,

$$\angle ABD = 94^\circ \text{ and}$$

$$\angle ACE = 126^\circ$$

$$\angle ABD + \angle ABC = 180^\circ \text{ (Linear pair)}$$

$$\angle ABC = 86^\circ \text{ (i)}$$

$$\angle ACE + \angle ACB = 180^\circ \text{ (Linear pair)}$$

$$\angle ACB = 54^\circ \text{ (ii)}$$

In $\triangle ABC$

$$\angle ABC + \angle ACB + \angle BAC = 180^\circ$$

$$86^\circ + 54^\circ + \angle BAC = 180^\circ$$

$$\angle BAC = 40^\circ$$