

CLASS –XI
ASSIGNMENT- 2

SUBJECT – MATHEMATICS
TOPIC-BINOMIAL THEORUM

Q1. Using binomial theorem, write down the expansion of the following:-

(i) $\left(x + 1 - \frac{1}{x}\right)^3$ (ii) $(\sqrt[3]{x} - \sqrt[3]{a})^6$ (iii) $(2x + 3y)^4$

Q2. Evaluate the following :-

(i) $(\sqrt{3} + 1)^5 - (\sqrt{3} - 1)^5$ (ii) $(3 + \sqrt{2})^4 + (3 - \sqrt{2})^4$ (iii) $(.99)^3 + (1.01)^3$

Q3. Using binomial theorem, prove that $2^{3n} - 7n - 1$ is divisible by 49, where $n \in \mathbb{N}$.

Q4. Using binomial theorem determine which number is larger $(1.2)^{4000}$ or 800?

Q5. Find the coefficient of x^{10} in the expansion of $\left(2x - \frac{1}{x^2}\right)^{25}$

Q6. Find the fourth term from the end in the expansion of $\left(2x - \frac{1}{x^2}\right)^{25}$

Q7. Find the middle term / terms in the expansion of :-

(i) $\left(2x - \frac{3}{2x}\right)^{20}$ (ii) $\left(x^4 - \frac{1}{x^3}\right)^{11}$

Q8. Find the term independent of x in the expansion of :-

(i) $\left(2x - \frac{1}{x^2}\right)^{10}$ (ii) $\left(3x^2 - \frac{1}{2x}\right)^9$

Q9. If the fourth term in the expansion of $\left(ax + \frac{1}{x}\right)^n$ is $\frac{5}{2}$, then find the value of 'a' and 'n'.

Q10. Find the value of a so that the term independent of x in $\left(\sqrt{x} + \frac{a}{x^2}\right)^{10}$ is 405.

- Q11. In the binomial expansion of $(1 + x)^n$, the coefficient of the fifth, sixth and seventh terms are in A.P. Find all values of n for which this can happen.
- Q12. The 3rd, 4th and 5th terms in the expansion of $(x + a)^n$ are respectively 84, 280 and 560, find the values of x , a and n .
- Q13. If the coefficient of $(2r + 4)^{\text{th}}$ and $(r - 2)^{\text{th}}$ terms in the expansion of $(1 + x)^{18}$ are equal, find r .
- Q14. Find the coefficient of a^4 in the product $(1 + 2a)^4 (2 - a)^5$ using binomial theorem.
- Q15. The coefficients of three consecutive terms in the expansion of $(1 + x)^n$ be 76, 95 and 76, find n .
- Q16. Using binomial theorem, prove that $3^{2n+2} - 8n - 9$ is divisible by 64, for all natural numbers.