#### **Short Answer Type Questions**

- **Q. 1** Find the equation of the straight line which passes through the point (1 2) and cuts off equal intercepts from axes.
- Sol. Let the intercepts along the X and Y-axes are a and a respectively.
  - $\therefore \text{ Equation of the line is} \qquad \frac{x}{a} + \frac{y}{a} = 1 \qquad \dots (i)$ Since, the point (1, -2) lies on the line,  $\therefore \qquad \qquad \frac{1}{a} - \frac{2}{a} = 1$  $\Rightarrow \qquad \qquad \frac{1-2}{a} = 1$  $\Rightarrow \qquad \qquad a = -1$ On putting a = -1 in Eq. (i), we get  $\frac{x}{-1} + \frac{y}{-1} = 1$  $\Rightarrow \qquad \qquad x + y = -1 \Rightarrow x + y + 1 = 0$
- **Q. 2** Find the equation of the line passing through the point (5, 2) and perpendicular to the line joining the points (2, 3) and (3, -1).
  - **Thinking Process**

First of all find the slope, using the formula 
$$=\frac{y_2 - y_1}{x_2 - x_1}$$
. Then, slope of perpendicular line is  $-\frac{1}{m}$ .

**Sol.** Consider the given points A(5, 2), B(2, 3) and C(3, -1). Slope of the line passing through the points B and C,  $m_{BC} = \frac{-1-3}{2} = -4$ 

So, the slope of required line is  $\frac{1}{4}$ 

Since, the equation of a line passing the point A(5, 2) and having slope  $\frac{1}{4}$  is  $y - 2 = \frac{1}{4}(x - 5)$ .

$$\Rightarrow \qquad 4y - 8 = x - 5$$
$$\Rightarrow \qquad x - 4y + 3 = 0$$

## **Q. 3** Find the angle between the lines $y = (2 - \sqrt{3})(x+5)$ and $y = (2 + \sqrt{3})(x-7)$ . **•** Thinking Process

If the angle between the lines having the slope  $m_1$  and  $m_2$  is  $\theta$ , then  $\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right|$ 

Use this formula to solve the above problem.

 $y = (2 - \sqrt{3})(x + 5)$ Sol. Given lines, ...(i)  $m_1 = (2 - \sqrt{3})$ y = (2 +  $\sqrt{3}$ )(x - 7) Slope of this line, and ...(ii) Slope of this line,  $m_2 = (2 + \sqrt{3})$ Let  $\theta$  be the angle between lines (i) and (ii), then  $\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right|$  $\tan \theta = \left| \frac{(2 - \sqrt{3}) - (2 + \sqrt{3})}{1 + (2 - \sqrt{3})(2 + \sqrt{3})} \right| \implies \tan \theta = \left| \frac{-2\sqrt{3}}{1 + 4 - 3} \right|$  $\Rightarrow$  $\tan \theta = \sqrt{3}$  $\Rightarrow$  $\tan \theta = \tan \pi/3$  $\Rightarrow$  $\theta = \pi/3 = 60^{\circ}$ *.*.. For obtuse angle =  $\pi - \pi/3 = 2\pi/3 = 120^{\circ}$ Hence, the angle between the lines are 60° or 120°.

## **Q. 4** Find the equation of the lines which passes through the point (3, 4) and cuts off intercepts from the coordinate axes such that their sum is 14.

Sol. Let the intercept along the axes be a and b. Given.  $a + b = 14 \implies b = 14 - a$ Now, the equation of line is  $\frac{x}{a} + \frac{y}{b} = 1$ . ...(i)  $\frac{x}{a} + \frac{y}{14 - a} = 1$  $\Rightarrow$ Since, the point (3, 4) lies on the line.  $\frac{3}{a} + \frac{4}{14 - a} = 1$ *.*..  $\frac{42 - 3a + 4a}{a(14 - a)} = 1 \implies 42 + a = 14a - a^2$  $\Rightarrow$  $a^{2} - 13a + 42 = 0 \Rightarrow a^{2} - 7a - 6a + 42 = 0$  $\Rightarrow$  $a(a-7) - 6(a-7) = 0 \implies (a-7)(a-6) = 0$  $\Rightarrow$ a - 7 = 0 or a - 6 = 0 $\Rightarrow$ *a* = 7 or *a* = 6 *.*.. When a = 7, then b = 7When a = 6, then b = 8: The equation of line, when a = 7 and b = 7 is  $\frac{x}{7} + \frac{y}{7} = 1 \implies x + y = 7$ So, the equation of line, when a = 6 and b = 8 is  $\frac{x}{6} + \frac{y}{8} = 1$ 

- **Q. 5** Find the points on the line x + y = 4 which lie at a unit distance from the line 4x + 3y = 10.
  - Thinking Process

The perpendicular distance of a point  $(x_1, y_1)$  from the line Ax + By + C = 0, is d', where

$$d = \frac{Ax_1 + By_1 + C}{\sqrt{A^2 + B^2}}$$

**Sol.** Let the required point be (h, k) and point (h, k) lies on the line x + y = 4*i.e.*, h + k = 4 ...(i) The distance of the point (h, k) from the line 4x + 3y = 10 is  $\left|\frac{4h + 3k - 10}{\sqrt{16 + 9}}\right| = 1$  $4h + 3k - 10 = \pm 5$ Taking positive sign, 4h + 3k = 15 ...(ii) From Eq. (i) h = 4 - k put in Eq. (ii), we get

4(4-k) + 3k = 1516 - 4k + 3k = 15 $\Rightarrow$ k = 1⇒ On putting k = 1 in Eq. (i), we get  $h + 1 = 4 \Longrightarrow h = 3$ So, the point is (3,1). Taking negative sign, 4h + 3k - 10 = -54(4-k) + 3k = 5⇒ 16 - 4k + 3k = 5 $\Rightarrow$  $\Rightarrow$ -k = 5 - 16 = -11k = 11*.*.. On putting k = 11 in Eq. (i), we get  $h + 11 = 4 \Longrightarrow h = -7$ Hence, the required points are (3, 1) and (-7, 11).

**Q. 6** Show that the tangent of an angle between the lines  $\frac{x}{a} + \frac{y}{b} = 1$  and  $\frac{x}{a} - \frac{y}{b} = 1$  is  $\frac{2ab}{a^2 - b^2}$ .

**Sol.** Given equation of lines are

 $\frac{x}{a} + \frac{y}{b} = 1 \qquad \dots (i)$ 

(ii)

$$\therefore \qquad \text{Slope, } m_1 = -\frac{b}{a}$$
  
and 
$$\frac{x}{a} - \frac{y}{b} = 1$$
  
$$\therefore \qquad \text{Slope, } m_2 = \frac{b}{a}$$

Let  $\theta$  be the angle between the given lines, then

$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right| \implies \tan \theta = \left| \frac{-\frac{b}{a} - \frac{b}{a}}{1 + \left(\frac{-b}{a}\right)\left(-\frac{b}{a}\right)} \right|$$
$$\Rightarrow \qquad \tan \theta = \left| \frac{\frac{-2b}{a}}{\frac{a^2 - b^2}{a^2}} \right| \implies \tan \theta = \frac{2ab}{a^2 - b^2} \qquad \text{Hence proved.}$$

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 $\mathbf{Q}$ . **7** Find the equation of lines passing through (1, 2) and making angle 30° with Y-axis.

#### Thinking Process

Equation of a line passing through the point  $(x_1, y_1)$  and having slope m is  $y - y_1 = m(x - x_1)$ 

**Sol.** Given that, angle with Y-axis =  $30^{\circ}$ angle with X-axis =  $60^{\circ}$ and

: Slope of the line,  $m = \tan 60^\circ = \sqrt{3}$ So, the equation of a line passing through (1, 2) and having slope  $\sqrt{3}$ , is

$$y - 2 = \sqrt{3}(x - 1)$$
  

$$\Rightarrow \qquad y - 2 = \sqrt{3}x - \sqrt{3}$$
  

$$\Rightarrow \qquad y - \sqrt{3}x - 2 + \sqrt{3} = 0$$

 ${f Q}_{f s}$   ${f 8}$  Find the equation of the line passing through the point of intersection of 2x + y = 5 and x + 3y + 8 = 0 and parallel to the line 3x + 4y = 7.

#### Thinking Process

First of all solve the given equation of lines to get the point of intersection. Then, if a line having slope  $m_1$  is parallel to another line having slope,  $m_2$ , then  $m_1 = m_2$ . Now, use the formula i.e., equation of a line passing through the point  $(x_1, y_1)$  with slope m is  $y - y_1 = m(x - x_1)$ .

Sol. Given equation of lines 2x + y = 5...(i) x + 3y = -8and ...(ii) y = 5 - 2xFrom Eq. (i), Now, put the value of y in Eq. (ii), we get x + 3(5 - 2x) = -8x + 15 - 6x = -8 $\Rightarrow$  $-5x = -23 \Longrightarrow x = \frac{23}{5}$ ⇒ Now,  $x = \frac{23}{5}$  put in Eq. (i), we get  $y = 5 - \frac{46}{5} = \frac{25 - 46}{5} = \frac{-21}{5}$ 

Since, the required line is parallel to the line 3x + 4y = 7. So, slope of the line is  $m = \frac{-3}{4}$ .

So, the equation of the line passing through the point  $\left(\frac{23}{5}, \frac{-21}{5}\right)$  having slope  $\frac{-3}{4}$  is

$$y + \frac{21}{5} = \frac{-3}{4} \left( x - \frac{23}{5} \right)$$
  

$$\Rightarrow \qquad 4y + \frac{84}{5} = -3x + \frac{69}{5}$$
  

$$\Rightarrow \qquad 3x + 4y = \frac{84 - 69}{5} \Rightarrow 3x + 4y + \frac{15}{5} = 0$$
  

$$\Rightarrow \qquad 3x + 4y + 3 = 0$$

 $\mathbf{Q}$ . 9 For what values of a and b the intercepts cut off on the coordinate axes by the line ax + by + 8 = 0 are equal in length but opposite in signs to those cut off by the line 2x - 3y + 6 = 0 on the axes?

**Sol.** Given equation of line  

$$ax + by + 8 = 0$$

$$\Rightarrow \qquad \qquad \frac{x}{-8} + \frac{y}{-8} = 1$$
So, the intercepts are  $\frac{-8}{a}$  and  $\frac{-8}{b}$ .  
and another given equation of line is  $2x - 3y + 6 = 0$ .  

$$\Rightarrow \qquad \qquad \frac{x}{-3} + \frac{y}{2} = 1$$
So, the intercepts are  $-3$  and 2.  
According to the question,  

$$\frac{-8}{a} = 3$$
 and  $\frac{-8}{b} = -2$ 

$$\therefore \qquad \qquad a = -\frac{8}{3}, b = 4$$

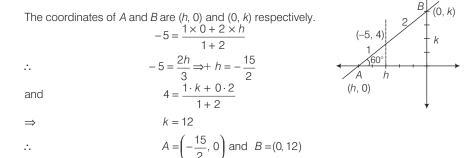
 ${f Q}$ .  ${f 10}$  If the intercept of a line between the coordinate axes is divided by the point (-5, 4) in the ratio 1 : 2, then find the equation of the line.

#### Thinking Process

The coordinates of a point which divides the join of  $(x_1, y_1)$  and  $(x_2, y_2)$  in the ratio  $m_1: m_2$  internally is  $\left(\frac{m_1x_2 + m_2x_1}{m_1 + m_2}, \frac{m_1y_2 + m_2y_1}{m_1 + m_2}\right)$ .

**Sol.** Let intercept of a line are (*h*, *k*).

....



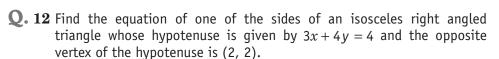
Hence, the equation of a line AB is

 ${f Q}_{f \cdot}$   ${f 11}$  Find the equation of a straight line on which length of perpendicular from the origin is four units and the line makes an angle of 120° with the positive direction of X-axis.

#### **Thinking Process**

The equation of the line having normal distance P from the origin and angle lpha which the normal makes with the positive direction of X-axis is  $x\cos\alpha + y\sin\alpha = p$ . Use this formula to solve the above problem.

**Sol.** Given that. OC = P = 4 units  $\angle BAX = 120^{\circ}$ B Let  $\angle COA = \alpha, \angle OCA = 90^{\circ}$  $\angle BAX = \angle COA + \angle OCA$  [exterior angle property] ÷  $120^\circ = \alpha + 90^\circ$  $\Rightarrow$ *:*..  $\alpha = 30^{\circ}$ Now, the equation of required line is  $x\cos 30^\circ + y\sin 30^\circ = 4$  $x \cdot \frac{\sqrt{3}}{2} + y \cdot \frac{1}{2} = 4$  $\Rightarrow$  $\sqrt{3}x + y = 8$ ⇒



**Sol.** Let slope of line AC be m and slope of line BC is  $\frac{-3}{4}$  and let angle between line AC and BC be  $\theta$ .

$$\therefore \quad \tan \theta = \left| \frac{m + \frac{3}{4}}{1 - \frac{3m}{4}} \right| \Rightarrow \tan 45^\circ = \pm \left[ \frac{m + \frac{3}{4}}{1 - \frac{3m}{4}} \right]$$
Taking positive sign, 
$$1 = \frac{m + \frac{3}{4}}{1 - \frac{3m}{4}}$$

$$\Rightarrow \qquad m + \frac{3}{4} = 1 - \frac{3m}{4}$$

$$\Rightarrow \qquad m + \frac{3m}{4} = 1 - \frac{3}{4}$$

$$\Rightarrow \qquad \frac{7m}{4} = \frac{1}{4} \Rightarrow m = \frac{1}{7}$$

⇒

$$B \xrightarrow{45^{\circ}} 45^{\circ} 45^{\circ} C$$

120

- X

Taking negative sign,

 $1 = -\left(\frac{m + \frac{3}{4}}{1 - \frac{3m}{4}}\right) \implies 1 - \frac{3m}{4} = -m - \frac{3}{4}$  $m - \frac{3m}{4} = -1 - \frac{3}{4}$ ⇒  $\frac{m}{4} = \frac{-7}{4} \Longrightarrow m = -7$ ⇒ :. Equation of side AC having slope  $\left(\frac{1}{7}\right)$  is  $y - 2 = \frac{1}{7}(x - 2)$ 7y - 14 = x - 2⇒ x - 7y + 12 = 0 $\Rightarrow$ and equation of side AB having slope (-7) is y - 2 = -7(x - 2)y - 2 = -7x + 14 $\Rightarrow$ 7x + y - 16 = 0 $\Rightarrow$ 

#### Long Answer Type Questions

**Q.** 13 If the equation of the base of an equilateral triangle is x + y = 2 and the vertex is (2, -1), then find the length of the side of the triangle.

#### **•** Thinking Process

Find the length of perpendicular (p) from (2, -1) to the line and use  $p = l \sin 60^\circ$ , where lis the length of the side of the triangle.

Sol. Given that, equilateral  $\triangle ABC$  having equation of base is x + y = 2.

 $\sin 60^\circ = \frac{AD}{AB}$ In  $\triangle ABD$ .

$$AD = AB\sin 60^\circ = AB\frac{\sqrt{3}}{2}$$
$$AD = AB\frac{\sqrt{3}}{2}$$

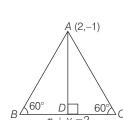
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Now, the length of perpendicular from (2, -1) to the line x + y = 2 is given by

$$AD = \left| \frac{2 + (-1) - 2}{\sqrt{1^2 + 1^2}} \right| = \frac{1}{\sqrt{2}}$$
$$\frac{1}{\sqrt{2}} = AB \frac{\sqrt{3}}{2}$$
$$AB = \sqrt{\frac{2}{3}}$$

From Eq. (i),



...(i)

- Q. 14 A variable line passes through a fixed point P. The algebraic sum of the perpendiculars drawn from the points (2, 0), (0, 2) and (1, 1) on the line is zero. Find the coordinates of the point P.
  - Thinking Process

Let the slope of the line be m. Then, the equation of the line passing through the fixed point  $P(x_1, y_1)$  is  $y - y_1 = m(x - x_1)$ . Taking the algebraic sum of perpendicular distances equal to zero, we get  $y_1 - 1 = m(x_1 - 1)$ . Thus,  $(x_1, y_1)$  is (1, 1).

**Sol.** Let slope of the line be *m* and the coordinates of fixed point *P* are  $(x_1, y_1)$ .  $\therefore$  Equation of line is  $y - y_1 = m(x - x_1)$  ....(i) Since, the given points are A(2, 0), B(0, 2) and C(1, 1). Now, perpendicular distance from *A*, is  $\frac{0 - y_1 - m(2 - x_1)}{\sqrt{1 + m^2}}$ Perpendicular distance from *B*, is  $\frac{2 - y_1 - m(0 - x_1)}{\sqrt{1 + m^2}}$ Perpendicular distance from *C*, is  $\frac{1 - y_1 - m(1 - x_1)}{\sqrt{1 + m^2}}$ Now,  $\frac{-y_1 - 2m + mx_1 + 2 - y_1 + mx_1 + 1 - y_1 - m + mx_1}{\sqrt{1 + m^2}} = 0$   $\Rightarrow \qquad -3y_1 - 3m + 3mx_1 + 3 = 0$   $\Rightarrow \qquad -y_1 - m + mx_1 + 1 = 0$ Since, (1, 1) lies on this line. So, the point *P* is (1, 1).

**Q.** 15 In what direction should a line be drawn through the point (1, 2), so that its point of intersection with the line x + y = 4 is at a distance  $\frac{\sqrt{6}}{3}$  from the given point?

**Sol.** Let slope of the line be *m*. As, the line passes through the point *A* (1, 2). Equation of line is y = 2 = m(x = 1)

$$\therefore \text{ Equation of line is } y - 2 = m(x - 1)$$

$$mx - y + 2 - m = 0 \qquad \dots(i)$$
and
$$x + y - 4 = 0$$

$$\frac{x}{(4 - 2 + m)} = \frac{y}{2 - m + 4m} = \frac{1}{1 + m}$$

$$\Rightarrow \qquad \frac{x}{2 + m} = \frac{y}{3m + 2} = \frac{1}{1 + m}$$

$$\Rightarrow \qquad x = \frac{2 + m}{1 + m}$$

$$y = \frac{3m + 2}{1 + m}$$
So, the point of intersection is  $B\left(\frac{m + 2}{m + 1}, \frac{3m + 2}{m + 1}\right)$ .

	$(m+2)^2$ $(2m+2)^2$
Now,	$AB^{2} = \left(\frac{m+2}{m+1} - 1\right)^{2} + \left(\frac{3m+2}{m+1} - 2\right)^{2}$
÷	$AB = \frac{\sqrt{6}}{3}$
÷	$\left(\frac{m+2-m-1}{m+1}\right)^2 + \left(\frac{3m+2-2m-2}{m+1}\right)^2 = \frac{6}{9}$
$\Rightarrow$	$\left(\frac{1}{m+1}\right)^2 + \left(\frac{m}{m+1}\right)^2 = \frac{6}{9}$
$\Rightarrow$	$\frac{1+m^2}{(1+m)^2} = \frac{6}{9}$
$\Rightarrow$	$\frac{1+m^2}{1+m^2+2m} = \frac{6}{9}$
$\Rightarrow$	$9 + 9m^2 = 6 + 6m^2 + 12m$
$\Rightarrow$	$3m^2 - 12m + 3 = 0$
$\Rightarrow$	$m^2 - 4m + 1 = 0$
÷	$m = \frac{4 \pm \sqrt{16 - 4}}{2} = 2 \pm \sqrt{3}$
	$=2 \pm \sqrt{3}$ = 2 + $\sqrt{3}$ or 2 - $\sqrt{3}$
.: <b>.</b>	$\theta = 75^{\circ} \text{ or } 15^{\circ}$

- **Q.** 16 A straight line moves so that the sum of the reciprocals of its intercepts made on axes is constant. Show that the line passes through a fixed point.
  - **Thinking Process**

If a line is  $\frac{x}{a} + \frac{y}{b} = 1$ , where  $\frac{1}{a} + \frac{1}{b} = constant = \frac{1}{k}(say)$ . This implies that  $\frac{k}{a} + \frac{k}{b} = 1 \Rightarrow$  line passes through the fixed point (k, k).

**Sol.** Since, the intercept form of a line is 
$$\frac{x}{a} + \frac{y}{b} = 1$$
.  
Given that,  
 $\frac{1}{a} + \frac{1}{b} = \text{constant}$   $= \frac{1}{k}$   
 $\therefore$   $\frac{1}{a} + \frac{1}{b} = \frac{1}{k}$   
 $\Rightarrow$   $\frac{k}{a} + \frac{k}{b} = 1$   
So,  $(k, k)$  lies on  $\frac{x}{a} + \frac{y}{b} = 1$ .

Hence, the line passes through the fixed point.

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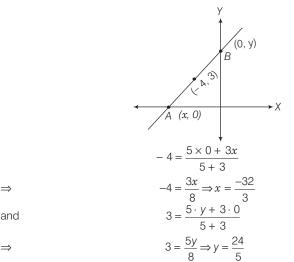
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**Q.** 17 Find the equation of the line which passes through the point (-4, 3) and the portion of the line intercepted between the axes is divided internally in the ratio 5 : 3 by this point.

#### **Thinking Process**

If the point (h, k) divides the join of A ( $x_1, y_1$ ) and B( $x_2, y_2$ ) internally, in the ratio  $m_1: m_2$ . Then, first of all find the coordinates of A and B using section formula for internal division i.e.,  $h = \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}$ ,  $k = \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2}$ . Then, find the equation of required line.

**Sol.** Since, the line intersects X and Y-axes respectively at A(x, 0) and B(0, y).



Since, the intercept on the X and Y-axes respectively are  $a = \frac{-32}{3}$  and  $b = \frac{24}{5}$ .

 $\therefore$  Equation of required line is

	$\frac{x}{-32/3} + \frac{y}{24/5} = 1$
$\Rightarrow$	$\frac{-3x}{32} + \frac{5y}{24} = 1$
$\Rightarrow$	-9x + 20y = 96
$\Rightarrow$	9x - 20y + 96 = 0

- **Q.** 18 Find the equations of the lines through the point of intersection of the lines x y + 1 = 0 and 2x 3y + 5 = 0 and whose distance from the point (3, 2) is  $\frac{7}{5}$ .
- Sol.
   Given equation of lines
   x y + 1 = 0 ...(i)

   and
   2x 3y + 5 = 0 ...(ii)

   From Eq. (i),
   x = y 1

Now, put the value of x in Eq. (ii), we get 2(y - 1) - 3y + 5 = 02y - 2 - 3y + 5 = 0 $\Rightarrow$  $3 - y = 0 \Longrightarrow y = 3$  $\Rightarrow$ y = 3 put in Eq. (i), we get x = 2Since, the point of intersection is (2, 3). Let slope of the required line be *m*. y - 3 = m(x - 2): Equation of line is mx - y + 3 - 2m = 0 $\Rightarrow$ ...(iii) Since, the distance from (3, 2) to line (iii) is  $\frac{7}{r}$ .  $\frac{7}{5} = \left| \frac{3m - 2 + 3 - 2m}{\sqrt{1 + m^2}} \right|$ *:*..  $\frac{49}{25} = \frac{(m+1)^2}{1+m^2}$ ⇒  $49 + 49m^2 = 25(m^2 + 2m + 1)$  $\Rightarrow$  $49 + 49m^2 = 25m^2 + 50m + 25$ ⇒  $24m^2 - 50m + 24 = 0$  $\Rightarrow$  $12m^2 - 25m + 12 = 0$  $\Rightarrow$  $m = \frac{25 \pm \sqrt{625 - 4 \cdot 12 \cdot 12}}{24}$  $= \frac{25 \pm \sqrt{49}}{24} = \frac{25 \pm 7}{24} = \frac{32}{24} \text{ or } \frac{18}{24} = \frac{4}{3} \text{ or } \frac{3}{4}$ *.*..  $y - 3 = \frac{4}{2}(x - 2)$ : First equation of a line is 3y - 9 = 4x - 8 $\Rightarrow$  $\Rightarrow \qquad 4x - 3y + 1 = 0$ and second equation of line is  $y - 3 = \frac{3}{4}(x - 2)$ 4y - 12 = 3x - 6 $\Rightarrow$ 3x - 4y + 6 = 0 $\Rightarrow$ 

Q. 19 If the sum of the distance of a moving point in a plane from the axes is 1, then find the locus of the point.

#### **Thinking Process**

Given that |x| + |y| = 1, which gives four sides of a square.

**Sol.** Let the coordinates of moving point P be (x, y). Given that, the sum of distances of this point in a plane from the axes is 1.

So, these equations give us locus of the point which is a square.

 $\begin{array}{c|c} B & x & P(x, y) \\ \hline & y \\ \hline & 0 & A \end{array} X$ 

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- **Q. 20**  $P_1$  and  $P_2$  are points on either of the two lines  $y \sqrt{3}|x| = 2$  at a distance of 5 units from their point of intersection. Find the coordinates of the foot of perpendiculars drawn from  $P_1$ ,  $P_2$  on the bisector of the angle between the given lines.
  - **Thinking Process**

Lines are  $y = \sqrt{3}x + 2$  and  $y = -\sqrt{3}x + 2$  according as  $x \ge 0$  or x < 0. Y-axis is the bisector of the angles between the lines. P<sub>1</sub>, P<sub>2</sub> are the points on these lines at a distance of 5 units from the point of intersection of these lines which have a point on Y-axis as common foot of perpendiculars drawn from these points. The y-coordinate of the foot of the perpendiculars is given by  $2 + 5 \cos 30^\circ$ .

Sol.	Given equation of lines are	$y - \sqrt{3}x = 2$	$[\because x \ge 0]$
	and	$y + \sqrt{3}x = 2$	$[:: x \leq 0]$
	÷	$y = \sqrt{3}x + 2$	(i)
	and	$y = -\sqrt{3}x + 2$	(ii)
	$\Rightarrow$	$\sqrt{3}x + 2 = -\sqrt{3}x + 2$	
	$\Rightarrow$	$2\sqrt{3}x = 0 \Longrightarrow x = 0$	
	On putting $x = 0$ in Eq. (i), we	get	
		<i>y</i> = 2	
		Y D	

(0.2)

5

60

С

30° 30°

C

60°

Α

X′ **←** 

 $P_1$ 

x

So, the point of intersection of line (i) and (ii) is (0, 2).  
Here,  

$$DC = 2$$
  
 $\ln \Delta DEC$ ,  
 $\frac{CD}{CE} = \cos 30^{\circ}$   
 $\therefore$   
 $CD = 5 \cos 30^{\circ}$   
 $= 5 \cdot \frac{\sqrt{3}}{2}$   
 $\Rightarrow$   
 $OD = OC + CD = 2 + 5\frac{\sqrt{3}}{2}$   
So, the coordinates of the foot of perpendiculars are  $\left(0, 2 + \frac{5\sqrt{3}}{2}\right)$ 

**Q.** 21 If *p* is the length of perpendicular from the origin on the line  $\frac{x}{a} + \frac{y}{b} = 1$ and  $a^2$ ,  $p^2$  and  $b^2$  are in AP, the show that  $a^4 + b^4 = 0$ .

Sol. Given equation of line is,

$$\frac{x}{a} + \frac{y}{b} = 1 \qquad \dots (i)$$

Perpendicular length from the origin on the line (i) is given by p i.e.,  $p = \frac{1}{\sqrt{\frac{1}{1-} + \frac{1}{2}}} = \frac{ab}{\sqrt{a^2 + b^2}}$ 

$$\therefore \qquad \qquad p^2 = \frac{a^2 b^2}{a^2 + b^2}$$

Given that,  $a^2$ ,  $p^2$  and  $b^2$  are in AP.

$$2p^{2} = a^{2} + b^{2}$$

$$\Rightarrow \qquad \frac{2a^{2}b^{2}}{a^{2} + b^{2}} = a^{2} + b^{2}$$

$$\Rightarrow \qquad 2a^{2}b^{2} = (a^{2} + b^{2})^{2}$$

$$\Rightarrow \qquad 2a^{2} + b^{2} = a^{4} + b^{4} + 2a^{2}b^{2}$$

$$\Rightarrow \qquad a^4 + b^4 = 0$$

#### **Objective Type Questions**

 $\mathbf{Q}$ . **22** A line cutting off intercept –3 from the Y-axis and the tangent at angle to the X-axis is  $\frac{3}{5}$ , its equation is (a) 5y - 3x + 15 = 0(b) 3y - 5x + 15 = 0(c) 5y - 3x - 15 = 0(d) None of the above c = -3 and  $m = \frac{3}{5}$ **Sol.** (*a*) Given that, : Equation of the line is y = mx + c $y = \frac{3}{5}x - 3$ 5y = 3x - 15 $\Rightarrow$ 5y - 3x + 15 = 0 $\Rightarrow$  ${f Q}_{f a}$   ${f 23}$  Slope of a line which cuts off intercepts of equal lengths on the axes is (d)  $\sqrt{3}$ (a) -1 (b) 0 (c) 2  $\frac{x}{a} + \frac{y}{a} = 1$ x + y = a**Sol.** (*a*) Let equation of line be  $\Rightarrow$ y = -x + a $\Rightarrow$ Required slope = -1*.*..

(d) x - y = 1

**Q.** 24 The equation of the straight line passing through the point (3, 2) and perpendicular to the line y = x is

(a) x - y = 5 (b) x + y = 5 (c) x + y = 1

- **Sol.** (b) Since, line passes through the point (3, 2) and perpendicular to the line y = x.
  - ∴ Slope (m) = -1 [since, line is perpendicular to the line y = x] ∴ Equation of line which passes through (3, 2) is

	y - 2 = -1(x - 3)
$\Rightarrow$	y - 2 = -x + 3
$\Rightarrow$	x + y = 5

**Q. 25** The equation of the line passing through the point (1, 2) and perpendicular to the line x + y + 1 = 0 is

(a) $y - x + 1 = 0$	(b) $y - x - 1 = 0$
(c) $y - x + 2 = 0$	(d) $y - x - 2 = 0$

**Sol.** (b) Given point is (1, 2) and slope of the required line is 1.  $\therefore x + y + 1 = 0 \Rightarrow y = -x - 1 \Rightarrow m_1 = -11$   $\therefore$  slope of the line  $= \frac{-1}{-1} = 1$   $\therefore$  Equation of required line is y - 2 = 1(x - 1)  $\Rightarrow \qquad y - 2 = x - 1$  $\Rightarrow \qquad y - x - 1 = 0$ 

**Q.** 26 The tangent of angle between the lines whose intercepts on the axes are a, -b and b, -a respectively, is

$$\tan \theta = \frac{a}{1+\frac{a}{b} \cdot \frac{b}{a}} = \frac{ab}{2} = \frac{b^2}{2ab}$$

**Q.** 27 If the line  $\frac{x}{a} + \frac{y}{b} = 1$  passes through the points (2, -3) and (4, -5), then (*a*, *b*) is (c) (1, -1) (d) (-1, -1) (a) (1, 1) (b) (-1, 1) **Sol.** (d) Given, line is  $\frac{x}{a} + \frac{y}{b} = 1$ ...(i) Since, the points (2, -3) and (4, -5) lies on this line.  $\frac{2}{a} - \frac{3}{b} = 1$  $\frac{4}{a} - \frac{5}{b} = 1$ *:*.. ...(ii) and ...(iii) On multiplying by 2 in Eq. (ii) and then subtracting Eq. (iii) from Eq. (ii), we get  $-\frac{6}{b} + \frac{5}{b} = 1$  $\frac{-1}{b} = 1$  $\Rightarrow$ b = -1*:*.. On putting b = -1 in Eq. (ii), we get  $\frac{2}{a} + 3 = 1$  $\frac{2}{a} = -2 \Rightarrow a = -1$  $\Rightarrow$ (a, b) = (-1, -1)*.*...

**Q.** 28 The distance of the point of intersection of the lines 2x - 3y + 5 = 0 and 3x + 4y = 0 from the line 5x - 2y = 0 is

5	5
(a) $\frac{130}{17\sqrt{29}}$	(b) $\frac{13}{7\sqrt{29}}$
(c) $\frac{130}{7}$	(d) None of these

#### Thinking Process

First of all find the point of intersection of the given first two lines, then get the perpendicular distance from this point to the third line. Using formula i.e., distance of a point  $(x_1, y_1)$  from the line ax + by + c = 0 is  $d = \frac{|ax_1 + by_1 + c|}{\sqrt{a^2 + b^2}}$ .

**Sol.** (*a*) Given equation of lines

and

2x - 3y + 5 = 0...(i) 3x + 4y = 0...(ii) From Eq. (ii), put the value of  $x = \frac{-4y}{3}$  in Eq. (i), we get (-4v)

$$2\left(\frac{-4y}{3}\right) - 3y + 5 = 0$$

$$\Rightarrow \qquad -8y - 9y + 15 = 0$$

$$\Rightarrow \qquad y = \frac{15}{17}$$

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From Eq. (ii),  $3x + 4 \cdot \frac{15}{17} = 0$   $\Rightarrow \qquad x = \frac{-60}{17 \cdot 3} = \frac{-20}{17}$ So, the point of intersection is  $\left(\frac{-20}{17}, \frac{15}{17}\right)$ .  $\therefore$  Required distance from the line 5x - 2y = 0 is,  $d = \frac{\left|-5 \times \frac{20}{17} - 2\left(\frac{15}{17}\right)\right|}{\sqrt{25 + 4}} = \frac{\left|\frac{-100}{17} - \frac{30}{17}\right|}{\sqrt{29}} = \frac{130}{17\sqrt{29}}$   $\left[ \because \text{ distance of a point } p(x_1, y_1) \text{ from the line } ax + by + c = 0 \text{ is } d = \frac{|ax_1 + by_1 + c|}{\sqrt{a^2 + b^2}} \right]$ 

- **Q.** 29 The equation of the lines which pass through the point (3, -2) and are inclined at 60° to the line  $\sqrt{3}x + y = 1$  is
  - (a) y + 2 = 0,  $\sqrt{3}x y 2 3\sqrt{3} = 0$ (b) x - 2 = 0,  $\sqrt{3}x - y + 2 + 3\sqrt{3} = 0$ (c)  $\sqrt{3}x - y - 2 - 3\sqrt{3} = 0$ (d) None of the above

**Sol.** (a) So, the given point A is 
$$(3, -2)$$
.  
So, the equation of line  $\sqrt{3}x + y = 1$ .  
 $\Rightarrow \qquad y = -\sqrt{3} x + 1$   
 $\therefore \qquad \text{Slope, } m_1 = -\sqrt{3}$   
Let slope of the required line be  $m_2$ .  
 $\therefore \qquad \tan \theta = \left|\frac{-\sqrt{3} - m_2}{1 - \sqrt{3}m_2}\right| \qquad [\because \tan \theta = \left|\frac{m_1 - m_2}{1 + m_1 m_2}\right|$   
 $\Rightarrow \qquad \tan 60^\circ = \pm \left(\frac{-\sqrt{3} - m_2}{1 - \sqrt{3}m_2}\right) \qquad ...(i)$   
 $\Rightarrow \qquad \sqrt{3} = \left(\frac{-\sqrt{3} - m_2}{1 - \sqrt{3}m_2}\right) \qquad [\text{taking positive sign}]$   
 $\Rightarrow \qquad \sqrt{3} - 3m_2 = -\sqrt{3} - m_2$   
 $\Rightarrow \qquad \sqrt{3} - 3m_2 = -\sqrt{3} - m_2$   
 $\Rightarrow \qquad \sqrt{3} - 3m_2 = -\sqrt{3} - m_2$   
 $\Rightarrow \qquad 0 = \sqrt{3} - 3m_2 = \sqrt{3} - m_2$   
 $\Rightarrow \qquad \sqrt{3} - 3m_2 = \sqrt{3} - m_2$   
 $\Rightarrow \qquad 0 = \sqrt{3}x - y - 2 - 3\sqrt{3} = 0$   
 $\Rightarrow \qquad \sqrt{3}x - y - 2 - 3\sqrt{3} = 0$   
 $\Rightarrow \qquad \sqrt{3}x - y - 2 - 3\sqrt{3} = 0$   
 $\therefore \text{ The equation of line is } y + 2 = 0 (x - 3)$   
 $\Rightarrow \qquad y + 2 = 0$   
 $\therefore \text{ The equation of line is } y + 2 = 0 (x - 3)$   
 $\Rightarrow \qquad y + 2 = 0$   
 $\Rightarrow \qquad (...(i))$   
So, the required equation of lines are  $\sqrt{3}x - y - 2 - 3\sqrt{3} = 0$  and  $y + 2 = 0$ .

<b>Q.</b> 30	The equations of the l	ines passing through the point (1, 0) and	1 at a
	distance $\frac{\sqrt{3}}{2}$ from the o	rigin, are	
	(a) $\sqrt{3}x + y - \sqrt{3} = 0$ , $\sqrt{3}x$ (b) $\sqrt{3}x + y + \sqrt{3} = 0$ , $\sqrt{3}x$ (c) $x + \sqrt{3}y - \sqrt{3} = 0$ , $x - (d)$ None of the above	$\begin{aligned} z - y - \sqrt{3} &= 0\\ x - y + \sqrt{3} &= 0 \end{aligned}$	
<b>Sol.</b> (a)	Let slope of the line be <i>m</i> . ∵ Equation of line passing		
	$\rightarrow$	y - 0 = m (x - 1) $y - mx + m = 0$	(i)
	$\Rightarrow$ Since, the distance from or		(i)
		_ 2	
	Then,	$\frac{\sqrt{3}}{2} = \frac{0 - 0 + m}{\sqrt{1 + m^2}}$	
	⇒	$\frac{\sqrt{3}}{2} = \frac{m}{\sqrt{1+m^2}}$	
	$\Rightarrow$	$\frac{3}{4} = \frac{m^2}{1+m^2}$	
	⇒ 3+	$+ 3m^2 = 4m^2$	
	$\Rightarrow$	$m^2 = 3$	
	$\Rightarrow$	$m = \pm \sqrt{3}$	
	So, the first equation of line		
	$\Rightarrow$	$y = \sqrt{3}(x - 1)$ $\sqrt{3}x - y - \sqrt{3} = 0$	
	and the second equation of	,,	
		$y = -\sqrt{3}(x - 1)$ $\sqrt{3}x + y - \sqrt{3} = 0$	
	$\Rightarrow$	$\sqrt{3x} + y - \sqrt{3} = 0$	
<b>O.</b> 31	The distance between t	he lines $y = mx + c_1$ and $y = mx + c_2$ is	
	(a) $\frac{c_1 - c_2}{\sqrt{m^2 + 1}}$	(b) $\frac{ c_1 - c_2 }{\sqrt{1 + m^2}}$	
	(c) $\frac{c_2 - c_1}{\sqrt{1 + m^2}}$	(d) 0	
Sol. (b)	Given, equation of the lines	sare	
		$y = mx + c_1$	(i)
	and	$y = mx + c_2$	(ii)
	Distance between them is	s given by	

$$d = \frac{|c_1 - c_2|}{\sqrt{1 + m^2}}$$

**Q. 32** The coordinates of the foot of perpendiculars from the point (2, 3) on the line y = 3x + 4 is given by

(a) 
$$\left(\frac{37}{10}, \frac{-1}{10}\right)$$
 (b)  $\left(-\frac{1}{10}, \frac{37}{10}\right)$  (c)  $\left(\frac{10}{37}, -10\right)$  (d)  $\left(\frac{2}{3}, -\frac{1}{3}\right)$   
Sol. (b) Given, equation of the line is  
 $y = 3x + 4$  ...(i)  
 $\therefore$  Slope of this line,  $m_1 = 3$   
So, the slope of line  $OP$  is  $-\frac{1}{3}$ . [ $\therefore OP \perp AB$ ]  
 $A = \frac{1}{y=3x+4} P$   
 $B$   
 $\therefore$  Equation of line  $OP$  is  
 $y - 3 = -\frac{1}{3}(x-2)$   
 $\Rightarrow 3y - 9 = -x + 2$   
 $\Rightarrow x + 3y - 11 = 0$  ...(ii)  
Using the value of y from Eq. (i) in Eq. (ii), we get  
 $x + 3(3x + 4) - 11 = 0$   
 $\Rightarrow x + 9x + 12 - 11 = 0$   
 $\Rightarrow 10x + 1 = 0 \Rightarrow x = -\frac{1}{10}$   
Put  $x = -\frac{1}{10}$  in Eq. (i), we get  
 $y = -\frac{3}{10} + 4 = -\frac{3+40}{10} = \frac{37}{10}$   
So, the foot of perpendicular is  $\left(-\frac{1}{10}, \frac{37}{10}\right)$   
Q. 33 If the coordinates of the middle point of the portion of a line

**Q. 33** If the coordinates of the middle point of the portion of a line intercepted between the coordinate axes is (3, 2), then the equation of the line will be

(a) 
$$2x + 3y = 12$$
 (b)  $3x + 2y = 12$  (c)  $4x - 3y = 6$  (d)  $5x - 2y = 10$   
**Sol.** (a) Since, the coordinates of the middle point are P(3, 2).  
 $\therefore$   $3 = \frac{1 \cdot 0 + 1 \cdot a}{1 + 1}$   
 $\Rightarrow$   $3 = \frac{a}{2} \Rightarrow a = 6$   
Similarly,  $b = 4$   
 $\therefore$  Equation of the line is  $\frac{x}{6} + \frac{y}{4} = 1$   
 $\Rightarrow$   $2x + 3y = 12$ 

- ${f Q}.~34$  Equation of the line passing through (1, 2) and parallel to the line y = 3x - 1 is
  - (a) y + 2 = x + 1(b) y + 2 = 3(x + 1)(c) y - 2 = 3(x - 1)(d) y - 2 = x - 1
- **Sol.** (c) Since, the line passes through (1, 2) and parallel to the line y = 3x 1. So, slope of the required line m = 3. [: slope of y = 3x - 1 is 3] Hence, the equation of line is

$$y - 2 = 3(x - 1)$$

Q. 35 Equations of diagonals of the square formed by the lines x = 0, y = 0, x = 1 and y = 1 are

(a) $y = x, y + x = 1$	(b) $y = x, x + y = 2$
(c) $2y = x, y + x = \frac{1}{3}$	(d) $y = 2x, y + 2x = 1$

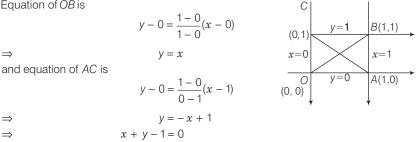
**Sol.** (a) Equation of OB is

 $\Rightarrow$ 

 $\Rightarrow$ 

 $\Rightarrow$ 

and



 $\mathbf{Q}$ . 36 For specifying a straight line, how many geometrical parameters should be known?

**Sol.** (b) Equation of straight lines are

y = mx + c, parameter = 2 ...(i)

$$\frac{x}{a} + \frac{y}{b} = 1$$
, parameter = 2 ...(ii)

$$y - y_1 = m(x - x_1)$$
, parameter = 2 ...(iii)

$$x\cos w + y\sin w = p$$
, parameter = 2 ...(iv)

It is clear that from Eqs. (i), (ii), (iii) and (iv), for specifying a straight line clearly two parameters should be known.

#### $\mathbf{Q}$ . 37 The point (4, 1) undergoes the following two successive transformations

- (i) Reflection about the line y = x
- (ii) Translation through a distance 2 units along the positive X-axis.

Then, the final coordinates of the point are

(a) (4, 3)	(b) (3, 4)
(c) (1, 4)	$(d)\left(\frac{7}{2},\frac{7}{2}\right)$

**Sol.** (b) Let the reflection of A(4, 1) in y = x is B(h, k). Now, mid-point of AB is  $\left(\frac{4+h}{2}, \frac{1+k}{2}\right)$  which lies on y = x.  $\frac{4+h}{2} = \frac{1+k}{2} \Longrightarrow h-k = -3$ i.e., ...(i) So, the slope of line y = x is 1. Slope of  $AB = \frac{h-4}{k-1}$ *:*..  $1 \cdot \left(\frac{h-4}{k-1}\right) = -1$  $\Rightarrow$ h - 4 = 1 - k $\Rightarrow$ h + k = 5 $\Rightarrow$ ...(ii) h - k = -3and  $2h = 2 \implies h = 1$ On putting h = 1 in Eq. (ii), we get k = 4So, the point is (1, 4). Hence, after translation the point is (1 + 2, 4) or (3, 4). **Q.** 38 A point equidistant from the lines 4x + 3y + 10 = 0, 5x - 12y + 26 = 0and 7x + 24y - 50 = 0 is (a)(1, -1)(b)(1, 1)(c) (0, 0) (d) (0, 1) **Sol.** (c) The given equation of lines are 4x + 3y + 10 = 0...(i) 5x - 12y + 26 = 0 $\Rightarrow$ ...(ii) 7x + 24y - 50 = 0 $\Rightarrow$ ...(iii) Let the point (h, k) which is equidistant from these lines. Distance from line (i) =  $\frac{|4h + 3k + 10|}{\sqrt{16 + 9}}$ Distance from line (ii) =  $\frac{|5h - 12k + 26|}{\sqrt{25 + 144}}$ Distance from the line (iii) =  $\frac{|7h + 24k - 50|}{\sqrt{7^2 + 24^2}}$ So, the point (h, k) is equidistant from lines (i), (ii) and (iii)  $\frac{4h+3k+10}{\sqrt{16+9}} = \frac{5h-12\,k+26}{\sqrt{25+144}} = \frac{7\,h+24k-50}{\sqrt{49+576}}$ *.*..  $\frac{|4h+3k+10|}{5} = \frac{|5h-12k+26|}{13} = \frac{|7h+24k-50|}{25}$  $\Rightarrow$ Clearly, if h = 0, k = 0, then  $\frac{10}{5} = \frac{26}{13} = \frac{50}{25} = 2$ Hence, the required point is (0, 0).

**Q. 39** A line passes through (2, 2) and is perpendicular to the line 3x + y = 3. Its y-intercept is (a)  $\frac{1}{3}$ (b)  $\frac{2}{3}$ (d)  $\frac{4}{3}$ (c) 1 Thinking Process First of all find the equation of required line using the formulae. i.e.,  $y - y_1 = m(x - x_1)$ then put x = 0 to get y-intercept. **Sol.** (d) Given line is y = 3 - 3x. Then, slope of the required line =  $\frac{1}{2}$ : Equation of the required line is  $y - 2 = \frac{1}{3}(x - 2)$ 3y - 6 = x - 2 $\Rightarrow$ x - 3y + 4 = 0 $\Rightarrow$ put x = 0, For y-intercept, 0 - 3y + 4 = 0 $y = \frac{4}{3}$ ⇒

**Q.** 40 The ratio in which the line 3x + 4y + 2 = 0 divides the distance between the lines 3x + 4y + 5 = 0 and 3x + 4y - 5 = 0 is (a) 1:2 (b) 3:7 (c) 2:3 (d) 2:5

**Sol.** (b) Let point  $A(x_1, y_1)$  lies on the line 3x + 4y + 5 = 0, then  $3x_1 + 4y_1 + 5 = 0$ 

$$3x + 4y + 5 = 0$$

$$A$$

$$P$$

$$3x + 4y + 2 = 0$$

$$3x + 4y - 5 = 0$$

Now, perpendicular distance from A to the line

$$\Rightarrow \qquad \frac{|3x_1 + 4y_1 + 2|}{\sqrt{9 + 16}} = \frac{|-5 - 2|}{\sqrt{9 + 16}} = \frac{-7}{5}$$

Let point  $B(x_2, y_2)$  lies on the line 3x + 4y - 5 = 0 *i.e.*,  $3x_2 + 4y_2 - 5 = 0$ . Now, perpendicular distance from *B* to the line 3x + 4y + 2 = 0,

3x + 4y + 2 = 0

$$\frac{|3x_2 + 4y_2 + 2|}{\sqrt{9 + 16}} = \frac{|+5-2|}{\sqrt{9 + 16}} = \frac{3}{5}$$

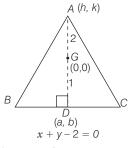
Hence, the required ratio is  $\frac{3}{5} : \frac{7}{5} i.e., 3:7$ .

## **Q. 41** One vertex of the equilateral triangle with centroid at the origin and one side as x + y - 2 = 0 is

**Thinking Process** 

Let ABC be the equilateral triangle with vertex A(h, k) and D ( $\alpha$ ,  $\beta$ ) be the point on BC. Then,  $\frac{2\alpha + h}{3} = 0 = \frac{2\beta + k}{3}$ . Also,  $\alpha + \beta - 2 = 0$  and  $\left(\frac{k - 0}{h - 0}\right) \cdot (-1) = -1$ .

**Sol.** (*c*) Let ABC be the equilateral triangle with vertex A(h, k). Let the coordinates of *D* are  $(\alpha, \beta)$ .



We know that, 2 : 1 from	m the vertex A.	
÷.	$0 = \frac{2\alpha + h}{3} \text{ and } 0 = \frac{2\beta + k}{3}$	
$\Rightarrow$	$2\alpha = -h$	
and	$2\beta = -k$	(i)
Also, $D(\alpha, \beta)$ lies on the	e line x + y - 2 = 0.	
	$\alpha + \beta - 2 = 0$	(ii)
	$AD \perp BC$	
Since, the slope of line	$e BC i.e., m_{BC} = -1$	
and slope of the line A	AG i.e., $m_{AG} = \frac{k-0}{h-0} = \frac{k}{h}$	
$\Rightarrow$	$(-1)\cdot\left(\frac{k}{h}\right) = -1$	
$\Rightarrow$	h = k	(iii)
From Eqs. (i) and (iii),		
	$2\alpha = -h$ and $2\beta = -h$	
	$\alpha = \beta$	
From Eq. (ii),	$2\alpha - 2 = 0 \implies \alpha = 1$	
If $\alpha = 1$ , then $\beta = 1$		
From Eq. (i), $h = -2$ , k	s = -2	
So, the vertex A is (-2	2, -2).	

#### Fillers

- **Q.** 42 If *a*, *b* and *c* are in AP, then the straight lines ax + by + c = 0 will always pass through ........
  - **Thinking Process**

If a, b and c are in AP, then 2b = a + c. Use this property to solve the above problem.

- **Sol.** Given line is ax + by + c = 0 ...(i) Since, *a*, *b* and *c* are in AP, then  $b = \frac{a+c}{2}$   $\Rightarrow \qquad a-2b+c=0$  ...(ii) On comparing Eqs.(i) and (ii), we get x = 1, y = 2 [using value of *b* in Eq. (i)] So, (1, -2) lies on the line.
- **Q. 43** The line which cuts off equal intercept from the axes and pass through the point (1, -2) is .........
- Sol. Let equation of line is

 $\frac{x}{a} + \frac{y}{a} = 1$ ...(i) Since, this line passes through (1, -2).  $\frac{1}{a} - \frac{2}{a} = 1$  $\Rightarrow \qquad 1 - 2 = a \Rightarrow a = -1$  $\therefore$  Required equation of the line is  $\frac{-x - y = 1}{x + y + 1 = 0}$ 

**Q.** 44 Equation of the line through thes point (3, 2) and making an angle of 45° with the line x - 2y = 3 are .......

**Sol.** Since, the given point P(3, 2) and line is x - 2y = 3. Slope of this line is  $m_1 = \frac{1}{2}$ 

Let the slope of the required line is m

Then,

e is m.  

$$\tan \theta = \left| \frac{m - \frac{1}{2}}{1 + \frac{1}{2}m} \right|$$

$$1 = \pm \left( \frac{m - \frac{1}{2}}{1 + \frac{m}{2}} \right)$$

 $[:: tan 45^{\circ} = 1] \dots (i)$ 

 $\Rightarrow$ 

Taking positive sign,

$$1 + \frac{m}{2} = m - \frac{1}{2}$$

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$$\Rightarrow \qquad \qquad m - \frac{m}{2} = 1 + \frac{1}{2}$$
$$\Rightarrow \qquad \qquad \frac{m}{2} = \frac{3}{2} \Rightarrow m = 3$$

Taking negative sign,

$$1 = -\left(\frac{m - \frac{1}{2}}{1 + \frac{m}{2}}\right)$$

$$\Rightarrow \qquad 1 + \frac{m}{2} = -m + \frac{1}{2}$$

$$\Rightarrow \qquad m + \frac{m}{2} = \frac{1}{2} - 1$$

$$\Rightarrow \qquad \frac{3m}{2} = \frac{-1}{2} \Rightarrow m = \frac{-1}{3}$$

:. First equation of the line is

 $\Rightarrow$ 

$$y - 2 = 3 (x - 3)$$
  
 $3x - y - 7 = 0$ 

and second equation of the line is

**Q. 45** The points (3, 4) and (2, -6) are situated on the ...... of the line 3x - 4y - 8 = 0.

**Sol.** Given line is 
$$3x - 4y - 8 = 0$$
 ...(i)  
For point (3, 4),  $9 - 4 \cdot 4 - 8$   
 $\Rightarrow$   $9 - 16 - 8$   
 $\Rightarrow$   $9 - 24$   
 $\Rightarrow$   $-15 < 0$  ...(i)  
For point (2, -6),  $6 + 24 - 8$   
 $22 > 0$  ...(ii)

Since, the value are of opposite sign.

Hence, the points (3, 4) and (2, -6) lies on opposite side to the line.

- **Q. 46** A point moves so that square of its distance from the point (3, -2) is numerically equal to its distance from the line 5x 12y = 3. The equation of its locus is .......
- **Sol.** Let the coordinaters of the point are (h, k),

 $\therefore$  Distance between (3, -2) and (h, k),

$$d_1^2 = (3-h)^2 + (-2-k)^2 \qquad \dots (i)$$

Now, distance of the point (*h*, *k*) from the line 5x - 12y = 3 is,

$$d_2 = \left| \frac{5h - 12k - 3}{\sqrt{25 + 144}} \right| = \left| \frac{5h - 12k - 3}{13} \right| \qquad \dots (ii)$$

 $d_1^2 = d_2$ Given that,  $(3-h)^{2} + (2+k)^{2} = \frac{5h-12k-3}{13}$  $9-6h+h^{2}+4+4k+k^{2} = \frac{5h-12k-3}{13}$  $\Rightarrow$  $\Rightarrow$  $h^{2} + k^{2} - 6h + 4k + 13 = \frac{5h - 12k - 3}{13}$  $\Rightarrow$  $13h^2 + 13k^2 - 78h + 52k + 169 = 5h - 12k - 3$ ⇒  $13h^2 + 13k^2 - 83h + 64k + 172 = 0$  $\Rightarrow$ : Locus of this point is  $13x^2 + 13y^2 - 83x + 64y + 172 = 0$ 

**Q.** 47 Locus of the mid-points of the portion of the line  $x\sin\theta + y\cos\theta = p$  intercepted between the axes is ......

**Sol.** Given equation of the line is  

$$x\sin\theta + y\cos\theta = p \qquad \dots(i)$$
Let the mid-point of *AB* are  $\left(\frac{a}{2}, \frac{b}{2}\right)$ 
Since, the point (a, 0) lies on the line (i), then  
 $a\sin\theta + 0 = p$   
 $\Rightarrow \qquad a\sin\theta = p \Rightarrow a = \frac{p}{\sin\theta}$   
and the point (0, b) also lies on the line, then  
 $0 + b\cos\theta = p$   
 $\Rightarrow \qquad b\cos\theta = p \Rightarrow b = \frac{p}{\cos\theta}$   
Now, mid-point of  $AB = \left(\frac{a}{2}, \frac{b}{2}\right) \operatorname{or} \left(\frac{p}{2\sin\theta}, \frac{p}{2\cos\theta}\right)$   
 $\therefore \qquad \frac{p}{2\sin\theta} = h \Rightarrow \sin\theta = \frac{p}{2h}$   
and  $\frac{p}{2\cos\theta} = k \Rightarrow \cos\theta = \frac{p}{2k}$   
 $\therefore \qquad \sin^2\theta + \cos^2\theta = \frac{p^2}{4h^2} + \frac{p^2}{4k^2}$   
 $\Rightarrow \qquad 1 = \frac{p^2}{4} \left(\frac{1}{h^2} + \frac{1}{k^2}\right)$   
Locus of the mid-point is  
 $4 = p^2 \left(\frac{1}{x^2} + \frac{1}{y^2}\right)$ 

$$4 = p^2 \left( \frac{1}{x^2} + \frac{1}{y^2} \right)$$
$$\Rightarrow \qquad 4x^2 y^2 = p^2 (x^2 + y^2)$$

#### **True/False**

#### ${f Q}_{f a}$ ${f 48}$ If the vertices of a triangle have integral coordinates, then the triangle cannot be equilateral.

#### Sol. True

We know that, if the vertices of a triangle have integral coordinates, then the triangle cannot be equilateral. Hence, the given statement is true.

Since, in equilatteral triangle, we get tan  $60^\circ = \sqrt{3}$  = Slope of the line, so with integral coordinates as vertices, the triangle cannot be equilateral.

#### **Q. 49** The points A(-2, 1), B(0, 5) and C(-1, 2) are collinear.

#### Sol. False

Given points are A (-2, 1), B (0, 5) and C(1, 2).Now,slope of 
$$AB = \frac{5-1}{0+2} = 2$$
Slope of $BC = \frac{2-5}{-1-0} = 3$ Slope of $AC = \frac{2-1}{-1+2} = 1$ 

Since, the slopes are different.

Hence, A, B and C are not collinear. So, statement is false.

**Q. 50** Equation of the line passing through the point  $(a \cos^3 \theta, a \sin^3 \theta)$ the line  $x \sec \theta + y \csc \theta = a$  is perpendicular to and  $x\cos\theta - y\sin\theta = a\sin2\theta$ .

2 ...

#### Sol. False

 $\Rightarrow$ 

Given point  $p(a\cos^3\theta, a\sin^3\theta)$  and the line is  $x \sec \theta + y \csc \theta = a$ 

Slope of this line  $= \frac{-\sec\theta}{\csc\theta} = -\tan\theta$ ÷ slope of required line  $=\frac{1}{\tan\theta}=\cot\theta$ and

... Equation of the required line is

$$y - a\sin^3\theta = \cot\theta (x - a\cos^3\theta)$$
$$y\sin\theta - a\sin^4\theta = x\cos\theta - a\cos^4\theta$$

$$\Rightarrow \qquad x\cos\theta - y\sin\theta = a\cos^4\theta - a\sin^4\theta$$

$$\Rightarrow \qquad x\cos\theta - y\sin\theta = a[(\cos^2\theta + \sin^2\theta)(\cos^2\theta - \sin^2\theta)]$$

 $x\cos\theta - y\sin\theta = a\cos^2\theta$  $\Rightarrow$ 

Hence, the given statement is false.

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- **Q.** 51 The straight line 5x + 4y = 0 passes through the point of intersection of the straight lines x + 2y - 10 = 0 and 2x + y + 5 = 0.
- Sol. True Given that, x + 2y - 10 = 0...(i) and 2x + y + 5 = 0...(ii) From Eq. (i), put the value of x = 10 - 2y in Eq. (ii), we get 20 - 4y + y + 5 = 020 - 3y + 5 = 0⇒  $y = \frac{25}{3}$  $\Rightarrow$  $x + \frac{50}{3} - 10 = 0$ [using Eq. (i)] *:*..  $\Rightarrow \qquad x + \frac{20}{3} = 0 \Rightarrow x = \frac{-20}{3}$ So, the point of intersection is  $\left(-\frac{20}{3}, \frac{25}{3}\right)$ . If the line 5x + 4y = 0 passes through the point  $\left(-\frac{20}{3}, \frac{25}{3}\right)$ , then this point should lie on this

$$5\left(\frac{-20}{3}\right) + \frac{4(25)}{3} = \frac{-100}{3} + \frac{100}{3} = 0$$

So, this point lies on the given line. Hence, the statement is true.

 ${f Q}_{f s}$   ${f 52}$  The vertex of an equilateral triangle is (2, 3) and the equation of the opposite side is x + y = 2. Then, the other two sides are  $y - 3 = (2 \pm \sqrt{3})(x - 2).$ 

**Sol.** *True*  
Let *ABC* be an equilateral triangle with vertex *A*(2, 3), and equation of *BC* is 
$$x + y = 2$$
. *i.e.*, slope  $= -1$ .  
Let slope of line *AB* is *m*.  
Since, the angle between line *AB* and *BC* is 60°.  
 $\therefore$   $\tan 60^\circ = \left| \frac{m+1}{1-m} \right|$   
 $\Rightarrow \sqrt{3} = \pm \left( \frac{m+1}{1-m} \right)$  [taking positive sign]  
 $\Rightarrow \sqrt{3} - \sqrt{3} m = m + 1$   
 $\Rightarrow \sqrt{3} - 1 = m + \sqrt{3} m$   
 $\Rightarrow \sqrt{3} - 1 = m(1 + \sqrt{3})$   
 $\therefore \qquad m = \frac{(\sqrt{3} - 1)(\sqrt{3} - 1)}{(\sqrt{3} + 1)(\sqrt{3} - 1)}$   
 $= \frac{3 + 1 - 2\sqrt{3}}{3 - 1} = \frac{4 - 2\sqrt{3}}{2} = 2 - \sqrt{3}$ 

Similarly, slope of  $AB = 2 + \sqrt{3}$ : Equation of other two side is

$$y - 3 = (2 \pm \sqrt{3})(x - 2)$$

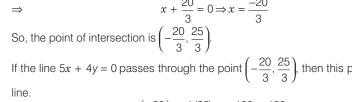
Hence, the statement is true.

[taking negative sign]

A (2, 3) в∠60 60%

x+y=2

C



- **Q. 53** The equation of the line joining the point (3, 5) to the point of intersection of the lines 4x + y 1 = 0 and 7x 3y 35 = 0 is equidistant from the points (0, 0) and (8, 34).
  - **Thinking Process**

Equation of a line passing through the points  $(x_1, y_1)$  and  $(x_2, y_2)$  is  $y-y_1=\frac{y_2-y_1}{x_2-x_1}(x-x_1)$ .

#### Sol. True

Given equation of lines are

$$4x + y - 1 = 0$$
and
$$7x - 3y - 35 = 0$$
From Eq. (i), on putting  $y = 1 - 4x$  in Eq. (ii), we get
$$7x - 3 + 12x - 35 = 0$$

$$\Rightarrow \qquad 19x - 38 = 0 \Rightarrow x = 2$$
On putting  $x = 2$  in Eq. (i), we get
$$8 + y - 1 = 0 \Rightarrow y = -7$$
Now, the equation of a line passing through (3, 5) and (2, -7) is
$$y - 5 = \frac{-7 - 5}{2 - 3}(x - 3)$$

$$\Rightarrow \qquad y - 5 = 12(x - 3)$$

$$\Rightarrow \qquad 12x - y - 31 = 0$$
Distance from (0, 0) to the line (iii),
$$d_1 = \frac{|-31|}{\sqrt{144 + 1}} = \frac{31}{\sqrt{145}}$$

:. Distance from (8, 34) to the line (iii),

$$d_2 = \frac{|96 - 34 - 31|}{\sqrt{145}} = \frac{31}{\sqrt{145}}$$
$$d_1 = d_2$$

Hence, the statement is true.

- **Q.** 54 The line  $\frac{x}{a} + \frac{y}{b} = 1$  moves in such a way that  $\frac{1}{a^2} + \frac{1}{b^2} = \frac{1}{c^2}$ , where *c* is a constant. The locus of the foot of the perpendicular from the origin on the given line is  $x^2 + y^2 = c^2$ .
- Sol. True

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Given that, equation of line is

$$\frac{x}{a} + \frac{y}{b} = 1 \qquad \dots (i)$$

Equation of line passing through origin and perpendicular to line (i) is

$$\frac{x}{b} - \frac{y}{a} = 0 \qquad \dots (ii)$$

Now, foot of perpendicular is the point of intersection of lines (i) and (ii). To find its locus we have to eliminate the variable *a* and *b*.

On squaring and adding Eqs. (i) and (ii), we get  $r^2 v^2 2\pi v r^2 v^2$ 

$$\frac{x^{2}}{a^{2}} + \frac{y^{2}}{b^{2}} + \frac{2xy}{ab} + \frac{x^{2}}{b^{2}} + \frac{y^{2}}{a^{2}} - \frac{2xy}{ab} = 1$$

$$\Rightarrow \qquad x^{2} \left(\frac{1}{a^{2}} + \frac{1}{b^{2}}\right) + y^{2} \left(\frac{1}{a^{2}} + \frac{1}{b^{2}}\right) = 1$$

$$\Rightarrow \qquad \frac{x^{2}}{c^{2}} + \frac{y^{2}}{c^{2}} = 1$$

$$\Rightarrow \qquad x^{2} + y^{2} = c^{2} \qquad \left[ \because \frac{1}{a^{2}} + \frac{1}{b^{2}} = \frac{1}{c^{2}} \right]$$

Hence, the statement is true.

## **Q.** 55 The lines ax + 2y + 1 = 0, bx + 3y + 1 = 0 and cx + 4y + 1 = 0 are concurrent, if a, b and c are in GP.

#### **Thinking Process**

First of all find the intersection point of first two line. Then, if the lines are concurrent then this point should lies on the third line.

#### Sol. False

Given lines are

$$ax + 2y + 1 = 0 \qquad \dots(i)$$
  
and 
$$bx + 3y + 1 = 0 \qquad \dots(i)$$
  
From Eq. (i), on putting  $y = \frac{-ax - 1}{2}$  in Eq. (ii), we get  
$$bx - \frac{3}{2}(ax + 1) + 1 = 0$$
  
$$\Rightarrow \qquad 2bx - 3ax - 3 + 2 = 0$$
  
$$\Rightarrow \qquad x (2b - 3a) = 1 \Rightarrow x = \frac{1}{2b - 3a}$$
  
Now, using  $x = \frac{1}{2b - 3a}$  in Eq. (i), we get  
$$\frac{a}{2b - 3a} + 2y + 1 = 0$$
  
$$\Rightarrow \qquad 2y = -\left[\frac{a + 2b - 3a}{2b - 3a}\right]$$
  
$$\Rightarrow \qquad 2y = -\left[\frac{a + 2b - 3a}{2b - 3a}\right]$$
  
$$\Rightarrow \qquad 2y = \frac{-(2b - 2a)}{2b - 3a}$$
  
$$\Rightarrow \qquad y = \frac{(a - b)}{2b - 3a}$$
  
So, the point of intersection is  $\left(\frac{1}{2b - 3a}, \frac{a - b}{2b - 3a}\right)$ .  
Since, this point lies on  $cx + 4y + 1 = 0$ , then  
$$\frac{c}{2b - 3a} + \frac{4(a - b)}{2b - 3a} + 1 = 0$$
  
$$\Rightarrow \qquad c + 4a - 4b + 2b - 3a = 0$$
  
$$\Rightarrow \qquad -2b + a + c = 0 \Rightarrow 2b = a + c$$
  
Hence, the given statement is false.

**Q. 56** Line joining the points (3, -4) and (-2, 6) is perpendicular to the line joining the points (-3, 6) and (9, -18).

**Sol.** *False* Given points are A(3, -4), B(-2, 6), P(-3, 6) and Q(9, -18). Now, slope of  $AB = \frac{6+4}{-2-3} = -2$ and slope of  $PQ = \frac{-18-6}{9+3} = -2$ 

So, line AB is parallel to line PQ.

#### **Matching The Columns**

**Q. 57** Match the following.

	Column I		Column II
(i)	The coordinates of the points <i>P</i> and <i>Q</i> on the line $x + 5y = 13$ which are at a distance of 2 units from the line 12x - 5y + 26 = 0 are	(a)	(3, 1), (–7, 11)
(ii)	The coordinates of the point on the line $x + y = 4$ , which are at a unit distance from the line $4x + 3y - 10 = 0$ are	(b)	$\left(-\frac{1}{3},\frac{11}{3}\right),\left(\frac{4}{3},\frac{7}{3}\right)$
(iii)	The coordinates of the point on the line joining $A(-2, 5)$ and $B(3, 1)$ such that $AP = PQ = QB$ are	(c)	$\left(1,\frac{12}{5}\right),\left(-3,\frac{16}{5}\right)$

**Sol.** (i) Let the coordinate of point  $P(x_1, y_1)$  on the line x + 5y = 13i.e.,

$$P(13 - 5y_1, y_1).$$
  

$$\therefore \text{ Distance of } P \text{ from the line } 12x - 5y + 26 = 0,$$

$$2 = \left| \frac{12(13 - 5y_1) - 5y_1 + 26}{\sqrt{144 + 25}} \right|$$

$$\Rightarrow \qquad 2 = \pm \frac{156 - 60y_1 - 5y_1 + 26}{13}$$

$$\Rightarrow \qquad -65y_1 = -156 \qquad \text{[taking positive sign]}$$

$$\Rightarrow \qquad y_1 = \frac{156}{65} = \frac{12}{5}$$

$$\therefore \qquad x_1 = 13 - 5y_1$$

$$= 13 - 12 = 1$$
So, the coordinate of is  $P\left(1, \frac{12}{5}\right).$ 

$$\text{Similarly, the coordinates of } Q \text{ are } \left(-3, \frac{16}{5}\right).$$

$$\text{[taking negative sign]}$$

(ii) Let coordinates of the point on the line x + y = 4 be  $(4 - y_1, y_1)$ . Distance from the line 4x + 3y - 10 = 0.

$$1 = \left| \frac{4(4 - y_1) + 3y_1 - 10}{\sqrt{16 + 9}} \right|$$

$$\Rightarrow \qquad 1 = \pm \frac{16 - 4y_1 + 3y_1 - 10}{5} \qquad \text{[taking negative sign]}$$

$$\Rightarrow \qquad 5 = 6 - y_1$$

$$\Rightarrow \qquad y_1 = 1 \qquad \text{if } y_1 = 1, \text{ then } x_1 = 3 \qquad \text{So, the point is (3, 1).}$$
Similarly, taking negative sign the point is (-7, 11).
(iii) Given point A (-2, 5) and B (3, 1).
$$(-2, 5) \qquad (3, 1) \qquad (-2, 5) \qquad (-2, 5$$

**Q. 58** The value of the  $\lambda$ , if the lines  $(2 + 3y + 4) + \lambda(6x - y + 12) = 0$  are

	Column I		Column II
(i)	parallel to Y-axis is	(a)	$\lambda = -\frac{3}{4}$
(ii)	perpendicular to $7x + y - 4 = 0$ is	(b)	$\lambda = -\frac{1}{3}$
(iii)	passes through (1, 2) is	(c)	$\lambda = -\frac{17}{41}$
(i∨)	parallel to X-axis is	(d)	$\lambda = 3$

Sol. (i) Given equation of the line is

$$(2x + 3y + 4) + \lambda (6x - y + 12) = 0 \qquad \dots(i)$$
  
If line is parallel to Y-axis *i.e.,* it is perpendicular to X-axis  
$$\therefore \qquad \text{Slope} = m = \tan 90^\circ = \infty$$

#### NCERT Exemplar (Class XI) Solutions

	From line (i), $x(2 + 6\lambda) +$ and slope	$y(3 - \lambda) + 4 + 12\lambda = 0$ $= \frac{-(2 + 6\lambda)}{3 - \lambda}$	
	⇒	$\frac{-2-6\lambda}{3-\lambda} = \infty$	
	⇒	$\frac{-2-6\lambda}{3-\lambda} = \frac{1}{0} \Longrightarrow \lambda = 3$	
(ii) If the line (i) is perpendicular to the line $7x + y - 4 = 0$ or $y = -7x + 4$			
	÷	$\frac{-(2 + 6\lambda)}{(3 - \lambda)}(-7) = -1$	
	$\Rightarrow$	$14 + 42\lambda = -3 + \lambda$	
	$\Rightarrow$	$41\lambda = -17$	
	$\Rightarrow$	$\lambda = -\frac{17}{41}$	
(iii)	If the line (i) passes throu	ugh the point (1, 2).	
	Then, (2 + 6	$+ 4) + \lambda(6 - 2 + 12) = 0$	
	⇒	$12 + 16\lambda = 0 \Longrightarrow \lambda = -\frac{3}{4}$	
(iv)	If the line is parallel to X-axis the slope $= 0$ .		
	Then,	$\frac{-(2+6\lambda)}{3-\lambda}=0$	
	$\Rightarrow$	$-(2 + 6\lambda) = 0 \implies \lambda = -\frac{1}{3}$	
	So, the correct matches a	are (i) $\rightarrow$ (d), (ii) $\rightarrow$ (c), (iii) $\rightarrow$ (a), (iv) $\rightarrow$ (b).	

## **Q. 59** The equation of the line through the intersection of the lines 2x - 3y = 0 and 4x - 5y = 2 and

	Column I		Column II
(i)	through the point (2, 1) is	(a)	2x - y = 4
(ii)	perpendicular to the line $x + 2y + 1 = 0$	(b)	x + y - 5 = 0
(iii)	parallel to the line $3x - 4y + 5 = 0$ is	(c)	x - y - 1 = 0
(i∨)	equally inclined to the axes is	(d)	3x - 4y - 1 = 0

#### **Sol.** Given equation of the lines are

and  
From Eq. (i), put 
$$x = \frac{3y}{2}$$
 in Eq. (ii), we get  
 $4 \cdot \frac{(3y)}{2} - 5y = 2$   
 $\Rightarrow$   
Now, put  $y = 2$  in Eq. (i), we get  
 $x = 3$ 

So, the intersection points are (3, 2).

 $\Rightarrow$  $\Rightarrow$ 

 $\Rightarrow$ 

 $\Rightarrow$ 

 $\Rightarrow$ 

(i) The equation of the line passes through the point (3, 2) and (2, 1), is

$$y - 2 = \frac{1 - 2}{2 - 3}(x - y) - 2 = (x - 3)$$
$$x - y - 1 = 0$$

(ii) If the required line is perpendicular to the line x + 2y + 1 = 0

- $\therefore$  Slope of the required line = 2
- : Equation of the line is

$$y - 2 = 2(x - 3)$$
  
 $2x - y - 4 = 0$ 

(iii) If the required line is parallel to the line 3x - 4y + 5 = 0, then the slope of the required line =  $\frac{3}{4}$ 

3)

:. Equation of the required line is

$$y - 2 = \frac{3}{4}(x - 3)$$

$$\Rightarrow \qquad 4y - 8 = 3x - 9$$

$$\Rightarrow \qquad 3x - 4y - 1 = 0$$

(iv) If the line is equally inclined to the X-axis, then

 $m = \pm \tan 45^\circ = \pm 1$ 

: Equation of the line is

$$y - 2 = -1(x - 3)$$
 [taking negative v  
 $y - 2 = -x + 3$ 

alue]

x + y - 5 = 0So, the correct matches are  $(a) \rightarrow (iii)$ ,  $(b) \rightarrow (i)$ ,  $(c) \rightarrow (iv)$ ,  $(d) \rightarrow (ii)$ .