

# ANSWERS

## EXERCISE 7.1

1.  $-\frac{1}{2}\cos 2x$       2.  $\frac{1}{3}\sin 3x$       3.  $\frac{1}{2}e^{2x}$
4.  $\frac{1}{3a}(ax+b)^3$       5.  $-\frac{1}{2}\cos 2x - \frac{4}{3}e^{3x}$       6.  $\frac{4}{3}e^{3x} + x + C$
7.  $\frac{x^3}{3} - x + C$       8.  $\frac{ax^3}{3} + \frac{bx^2}{2} + cx + C$       9.  $\frac{2}{3}x^3 + e^x + C$
10.  $\frac{x^2}{2} + \log|x| - 2x + C$       11.  $\frac{x^2}{2} + 5x + \frac{4}{x} + C$
12.  $\frac{2}{7}x^{\frac{7}{2}} + 2x^{\frac{3}{2}} + 8\sqrt{x} + C$       13.  $\frac{x^3}{3} + x + C$
14.  $\frac{2}{3}x^{\frac{3}{2}} - \frac{2}{5}x^{\frac{5}{2}} + C$       15.  $\frac{6}{7}x^{\frac{7}{2}} + \frac{4}{5}x^{\frac{5}{2}} + 2x^{\frac{3}{2}} + C$
16.  $x^2 - 3\sin x + e^x + C$       17.  $\frac{2}{3}x^3 + 3\cos x + \frac{10}{3}x^{\frac{3}{2}} + C$
18.  $\tan x + \sec x + C$       19.  $\tan x - x + C$
20.  $2 \tan x - 3 \sec x + C$       21.  $C$
22.  $A$

## EXERCISE 7.2

1.  $\log(1+x^2) + C$       2.  $\frac{1}{3}(\log|x|)^3 + C$       3.  $\log|1+\log x| + C$
4.  $\cos(\cos x) + C$       5.  $-\frac{1}{4a}\cos 2(ax+b) + C$
6.  $\frac{2}{3a}(ax+b)^{\frac{3}{2}} + C$       7.  $\frac{2}{5}(x+2)^{\frac{5}{2}} - \frac{4}{3}(x+2)^{\frac{3}{2}} + C$

8.  $\frac{1}{6}(1+2x^2)^{\frac{3}{2}} + C$     9.  $\frac{4}{3}(x^2+x+1)^{\frac{3}{2}} + C$     10.  $2\log|\sqrt{x}-1| + C$
11.  $\frac{2}{3}\sqrt{x+4}(x-8) + C$
12.  $\frac{1}{7}(x^3-1)^{\frac{7}{3}} + \frac{1}{4}(x^3-1)^{\frac{4}{3}} + C$     13.  $-\frac{1}{18(2+3x^3)^2} + C$
14.  $\frac{(\log x)^{1-m}}{1-m} + C$     15.  $-\frac{1}{8}\log|9-4x^2| + C$     16.  $\frac{1}{2}e^{2x+3} + C$
17.  $-\frac{1}{2e^{x^2}} + C$     18.  $e^{\tan^{-1}x} + C$     19.  $\log(e^x + e^{-x}) + C$
20.  $\frac{1}{2}\log(e^{2x} + e^{-2x}) + C$     21.  $\frac{1}{2}\tan(2x-3) - x + C$
22.  $-\frac{1}{4}\tan(7-4x) + C$     23.  $\frac{1}{2}(\sin^{-1}x)^2 + C$
24.  $\frac{1}{2}\log|2\sin x + 3\cos x| + C$     25.  $\frac{1}{(1-\tan x)} + C$
26.  $2\sin\sqrt{x} + C$     27.  $\frac{1}{3}(\sin 2x)^{\frac{3}{2}} + C$     28.  $2\sqrt{1+\sin x} + C$
29.  $\frac{1}{2}(\log \sin x)^2 + C$     30.  $-\log|1+\cos x| + C$     31.  $\frac{1}{1+\cos x} + C$
32.  $\frac{x}{2} - \frac{1}{2}\log|\cos x + \sin x| + C$     33.  $\frac{x}{2} - \frac{1}{2}\log|\cos x - \sin x| + C$
34.  $2\sqrt{\tan x} + C$     35.  $\frac{1}{3}(1+\log x)^3 + C$     36.  $\frac{1}{3}(x+\log x)^3 + C$
37.  $-\frac{1}{4}\cos(\tan^{-1}x^4) + C$     38. D
39. B

## EXERCISE 7.3

1.  $\frac{x}{2} - \frac{1}{8} \sin(4x+10) + C$
2.  $-\frac{1}{14} \cos 7x + \frac{1}{2} \cos x + C$
3.  $\frac{1}{4} \left[ \frac{1}{12} \sin 12x + x + \frac{1}{8} \sin 8x + \frac{1}{4} \sin 4x \right] + C$
4.  $-\frac{1}{2} \cos(2x+1) + \frac{1}{6} \cos^3(2x+1) + C$
5.  $\frac{1}{6} \cos^6 x - \frac{1}{4} \cos^4 x + C$
6.  $\frac{1}{4} \left[ \frac{1}{6} \cos 6x - \frac{1}{4} \cos 4x - \frac{1}{2} \cos 2x \right] + C$
7.  $\frac{1}{2} \left[ \frac{1}{4} \sin 4x - \frac{1}{12} \sin 12x \right] + C$
8.  $2 \tan \frac{x}{2} - x + C$
9.  $x - \tan \frac{x}{2} + C$
10.  $\frac{3x}{8} - \frac{1}{4} \sin 2x + \frac{1}{32} \sin 4x + C$
11.  $\frac{3x}{8} + \frac{1}{8} \sin 4x + \frac{1}{64} \sin 8x + C$
12.  $x - \sin x + C$
13.  $2(\sin x + x \cos x) + C$
14.  $-\frac{1}{\cos x + \sin x} + C$
15.  $\frac{1}{6} \sec^3 2x - \frac{1}{2} \sec 2x + C$
16.  $\frac{1}{3} \tan^3 x - \tan x + x + C$
17.  $\sec x - \operatorname{cosec} x + C$
18.  $\tan x + C$
19.  $\log |\tan x| + \frac{1}{2} \tan^2 x + C$
20.  $\log |\cos x + \sin x| + C$
21.  $\frac{\pi x}{2} - \frac{x^2}{2} + C$
22.  $\frac{1}{\sin(a-b)} \log \left| \frac{\cos(x-a)}{\cos(x-b)} \right| + C$
23. A
24. B

## EXERCISE 7.4

1.  $\tan^{-1} x^3 + C$
2.  $\frac{1}{2} \log \left| 2x + \sqrt{1+4x^2} \right| + C$

3.  $\log \left| \frac{1}{2-x+\sqrt{x^2-4x+5}} \right| + C$       4.  $\frac{1}{5} \sin^{-1} \frac{5x}{3} + C$
5.  $\frac{3}{2\sqrt{2}} \tan^{-1} \sqrt{2} x^2 + C$       6.  $\frac{1}{6} \log \left| \frac{1+x^3}{1-x^3} \right| + C$
7.  $\sqrt{x^2-1} - \log |x+\sqrt{x^2-1}| + C$       8.  $\frac{1}{3} \log |x^3+\sqrt{x^6+a^6}| + C$
9.  $\log |\tan x + \sqrt{\tan^2 x + 4}| + C$       10.  $\log |x+1+\sqrt{x^2+2x+2}| + C$
11.  $\frac{1}{6} \tan^{-1} \left( \frac{3x+1}{2} \right) + C$       12.  $\sin^{-1} \left( \frac{x+3}{4} \right) + C$
13.  $\log \left| x - \frac{3}{2} + \sqrt{x^2-3x+2} \right| + C$       14.  $\sin^{-1} \left( \frac{2x-3}{\sqrt{41}} \right) + C$
15.  $\log \left| x - \frac{a+b}{2} + \sqrt{(x-a)(x-b)} \right| + C$
16.  $2\sqrt{2x^2+x-3} + C$       17.  $\sqrt{x^2-1} + 2 \log |x+\sqrt{x^2-1}| + C$
18.  $\frac{5}{6} \log |3x^2+2x+1| - \frac{11}{3\sqrt{2}} \tan^{-1} \left( \frac{3x+1}{\sqrt{2}} \right) + C$
19.  $6\sqrt{x^2-9x+20} + 34 \log \left| x - \frac{9}{2} + \sqrt{x^2-9x+20} \right| + C$
20.  $-\sqrt{4x-x^2} + 4 \sin^{-1} \left( \frac{x-2}{2} \right) + C$
21.  $\sqrt{x^2+2x+3} + \log |x+1+\sqrt{x^2+2x+3}| + C$
22.  $\frac{1}{2} \log |x^2-2x-5| + \frac{2}{\sqrt{6}} \log \left| \frac{x-1-\sqrt{6}}{x-1+\sqrt{6}} \right| + C$

$$23. 5\sqrt{x^2+4x+10} - 7\log|x+2+\sqrt{x^2+4x+10}| + C$$

$$24. B$$

$$25. B$$

### EXERCISE 7.5

$$1. \log \frac{(x+2)^2}{|x+1|} + C$$

$$2. \frac{1}{6} \log \left| \frac{x-3}{x+3} \right| + C$$

$$3. \log|x-1| - 5\log|x-2| + 4\log|x-3| + C$$

$$4. \frac{1}{2} \log|x-1| - 2\log|x-2| + \frac{3}{2} \log|x-3| + C$$

$$5. 4\log|x+2| - 2\log|x+1| + C$$

$$6. \frac{x}{2} + \log|x| - \frac{3}{4} \log|1-2x| + C$$

$$7. \frac{1}{2} \log|x-1| - \frac{1}{4} \log(x^2+1) + \frac{1}{2} \tan^{-1} x + C$$

$$8. \frac{2}{9} \log \left| \frac{x-1}{x+2} \right| - \frac{1}{3(x-1)} + C$$

$$9. \frac{1}{2} \log \left| \frac{x+1}{x-1} \right| - \frac{4}{x-1} + C$$

$$10. \frac{5}{2} \log|x+1| - \frac{1}{10} \log|x-1| - \frac{12}{5} \log|2x+3| + C$$

$$11. \frac{5}{3} \log|x+1| - \frac{5}{2} \log|x+2| + \frac{5}{6} \log|x-2| + C$$

$$12. \frac{x^2}{2} + \frac{1}{2} \log|x+1| + \frac{3}{2} \log|x-1| + C$$

$$13. -\log|x-1| + \frac{1}{2} \log(1+x^2) + \tan^{-1} x + C$$

$$14. 3\log|x+2| + \frac{7}{x+2} + C$$

$$15. \frac{1}{4} \log \left| \frac{x-1}{x+1} \right| - \frac{1}{2} \tan^{-1} x + C$$

$$16. \frac{1}{n} \log \left| \frac{x^n}{x^n+1} \right| + C$$

$$17. \log \left| \frac{2-\sin x}{1-\sin x} \right| + C$$

$$18. x + \frac{2}{\sqrt{3}} \tan^{-1} \frac{x}{\sqrt{3}} - 3 \tan^{-1} \frac{x}{2} + C$$

$$19. \frac{1}{2} \log \left( \frac{x^2+1}{x^2+3} \right) + C$$

$$20. \frac{1}{4} \log \left| \frac{x^4 - 1}{x^4} \right| + C$$

22. B

$$21. \log \left( \frac{e^x - 1}{e^x} \right) + C$$

23. A

### EXERCISE 7.6

$$1. -x \cos x + \sin x + C$$

$$3. e^x (x^2 - 2x + 2) + C$$

$$5. \frac{x^2}{2} \log 2x - \frac{x^2}{4} + C$$

$$7. \frac{1}{4} (2x^2 - 1) \sin^{-1} x + \frac{x\sqrt{1-x^2}}{4} + C$$

$$9. (2x^2 - 1) \frac{\cos^{-1} x}{4} - \frac{x}{4} \sqrt{1-x^2} + C$$

$$10. (\sin^{-1} x)^2 x + 2\sqrt{1-x^2} \sin^{-1} x - 2x + C$$

$$11. -\sqrt{1-x^2} \cos^{-1} x + x + C$$

$$13. x \tan^{-1} x - \frac{1}{2} \log(1+x^2) + C$$

$$15. \left( \frac{x^3}{3} + x \right) \log x - \frac{x^3}{9} - x + C$$

$$17. \frac{e^x}{1+x} + C$$

$$19. \frac{e^x}{x} + C$$

$$21. \frac{e^{2x}}{5} (2 \sin x - \cos x) + C$$

23. A

$$2. -\frac{x}{3} \cos 3x + \frac{1}{9} \sin 3x + C$$

$$4. \frac{x^2}{2} \log x - \frac{x^2}{4} + C$$

$$6. \frac{x^3}{3} \log x - \frac{x^3}{9} + C$$

$$8. \frac{x^2}{2} \tan^{-1} x - \frac{x}{2} + \frac{1}{2} \tan^{-1} x + C$$

$$12. x \tan x + \log |\cos x| + C$$

$$14. \frac{x^2}{2} (\log x)^2 - \frac{x^2}{2} \log x + \frac{x^2}{4} + C$$

$$16. e^x \sin x + C$$

$$18. e^x \tan \frac{x}{2} + C$$

$$20. \frac{e^x}{(x-1)^2} + C$$

$$22. 2x \tan^{-1} x - \log(1+x^2) + C$$

24. B

**EXERCISE 7.7**

1.  $\frac{1}{2}x\sqrt{4-x^2} + 2\sin^{-1}\frac{x}{2} + C$
2.  $\frac{1}{4}\sin^{-1}2x + \frac{1}{2}x\sqrt{1-4x^2} + C$
3.  $\frac{(x+2)}{2}\sqrt{x^2+4x+6} + \log\left|x+2+\sqrt{x^2+4x+6}\right| + C$
4.  $\frac{(x+2)}{2}\sqrt{x^2+4x+1} - \frac{3}{2}\log\left|x+2+\sqrt{x^2+4x+1}\right| + C$
5.  $\frac{5}{2}\sin^{-1}\left(\frac{x+2}{\sqrt{5}}\right) + \frac{x+2}{2}\sqrt{1-4x-x^2} + C$
6.  $\frac{(x+2)}{2}\sqrt{x^2+4x-5} - \frac{9}{2}\log\left|x+2+\sqrt{x^2+4x-5}\right| + C$
7.  $\frac{(2x-3)}{4}\sqrt{1+3x-x^2} + \frac{13}{8}\sin^{-1}\left(\frac{2x-3}{\sqrt{13}}\right) + C$
8.  $\frac{2x+3}{4}\sqrt{x^2+3x} - \frac{9}{8}\log\left|x+\frac{3}{2}+\sqrt{x^2+3x}\right| + C$
9.  $\frac{x}{6}\sqrt{x^2+9} + \frac{3}{2}\log\left|x+\sqrt{x^2+9}\right| + C$
10. A
11. D

**EXERCISE 7.8**

1.  $\frac{1}{2}(b^2 - a^2)$
2.  $\frac{35}{2}$
3.  $\frac{19}{3}$
4.  $\frac{27}{2}$
5.  $e - \frac{1}{e}$
6.  $\frac{15+e^8}{2}$

**EXERCISE 7.9**

1. 2
2.  $\log\frac{3}{2}$
3.  $\frac{64}{3}$
4.  $\frac{1}{2}$
5. 0
6.  $e^4(e-1)$

7.  $\frac{1}{2} \log 2$       8.  $\log \left( \frac{\sqrt{2}-1}{2-\sqrt{3}} \right)$       9.  $\frac{\pi}{2}$
10.  $\frac{\pi}{4}$       11.  $\frac{1}{2} \log \frac{3}{2}$       12.  $\frac{\pi}{4}$
13.  $\frac{1}{2} \log 2$       14.  $\frac{1}{5} \log 6 + \frac{3}{\sqrt{5}} \tan^{-1} \sqrt{5}$
15.  $\frac{1}{2} (e - 1)$       16.  $5 - \frac{5}{2} \left( 9 \log \frac{5}{4} - \log \frac{3}{2} \right)$
17.  $\frac{\pi^4}{1024} + \frac{\pi}{2} + 2$       18. 0      19.  $3 \log 2 + \frac{3\pi}{8}$
20.  $1 + \frac{4}{\pi} - \frac{2\sqrt{2}}{\pi}$       21. D      22. C

## EXERCISE 7.10

1.  $\frac{1}{2} \log 2$       2.  $\frac{64}{231}$       3.  $\frac{\pi}{2} - \log 2$
4.  $\frac{16\sqrt{2}}{15}(\sqrt{2}+1)$       5.  $\frac{\pi}{4}$       6.  $\frac{1}{\sqrt{17}} \log \frac{21+5\sqrt{17}}{4}$
7.  $\frac{\pi}{8}$       8.  $\frac{e^2(e^2-2)}{4}$       9. D
10. B

## EXERCISE 7.11

1.  $\frac{\pi}{4}$       2.  $\frac{\pi}{4}$       3.  $\frac{\pi}{4}$       4.  $\frac{\pi}{4}$
5. 29      6. 9      7.  $\frac{1}{(n+1)(n+2)}$
8.  $\frac{\pi}{8} \log 2$       9.  $\frac{16\sqrt{2}}{15}$       10.  $\frac{\pi}{2} \log \frac{1}{2}$       11.  $\frac{\pi}{2}$



12.  $\pi$                       13. 0                      14. 0                      15. 0  
 16.  $-\pi \log 2$             17.  $\frac{a}{2}$                     18. 5                      20. C  
 21. C

### MISCELLANEOUS EXERCISE ON CHAPTER 7

1.  $\frac{1}{2} \log \left| \frac{x^2}{1-x^2} \right| + C$                       2.  $\frac{2}{3(a-b)} \left[ (x+a)^{\frac{3}{2}} - (x+b)^{\frac{3}{2}} \right] + C$   
 3.  $-\frac{2}{a} \sqrt{\frac{(a-x)}{x}} + C$                       4.  $-\left(1 + \frac{1}{x^4}\right)^{\frac{1}{4}} + C$   
 5.  $2\sqrt{x} - 3x^{\frac{1}{3}} + 6x^{\frac{1}{6}} - 6 \log(1+x^{\frac{1}{6}}) + C$   
 6.  $-\frac{1}{2} \log|x+1| + \frac{1}{4} \log(x^2+9) + \frac{3}{2} \tan^{-1} \frac{x}{3} + C$   
 7.  $\sin a \log|\sin(x-a)| + x \cos a + C$     8.  $\frac{x^3}{3} + C$   
 9.  $\sin^{-1} \left( \frac{\sin x}{2} \right) + C$                       10.  $-\frac{1}{2} \sin 2x + C$   
 11.  $\frac{1}{\sin(a-b)} \log \left| \frac{\cos(x+b)}{\cos(x+a)} \right| + C$     12.  $\frac{1}{4} \sin^{-1}(x^4) + C$   
 13.  $\log \left( \frac{1+e^x}{2+e^x} \right) + C$                       14.  $\frac{1}{3} \tan^{-1} x - \frac{1}{6} \tan^{-1} \frac{x}{2} + C$   
 15.  $-\frac{1}{4} \cos^4 x + C$                       16.  $\frac{1}{4} \log(x^4+1) + C$   
 17.  $\frac{[f(ax+b)]^{n+1}}{a(n+1)} + C$                       18.  $\frac{-2}{\sin \alpha} \sqrt{\frac{\sin(x+\alpha)}{\sin x}} + C$   
 19.  $\frac{2(2x-1)}{\pi} \sin^{-1} \sqrt{x} + \frac{2\sqrt{x-x^2}}{\pi} - x + C$

$$20. -2\sqrt{1-x} + \cos^{-1}\sqrt{x} + \sqrt{x-x^2} + C$$

$$21. e^x \tan x + C$$

$$22. -2\log|x+1| - \frac{1}{x+1} + 3\log|x+2| + C$$

$$23. \frac{1}{2} \left[ x \cos^{-1} x - \sqrt{1-x^2} \right] + C$$

$$24. -\frac{1}{3} \left( 1 + \frac{1}{x^2} \right)^{\frac{3}{2}} \left[ \log \left( 1 + \frac{1}{x^2} \right) - \frac{2}{3} \right] + C$$

$$25. e^{\frac{\pi}{2}}$$

$$26. \frac{\pi}{8}$$

$$27. \frac{\pi}{6}$$

$$28. 2\sin^{-1} \frac{(\sqrt{3}-1)}{2}$$

$$29. \frac{4\sqrt{2}}{3}$$

$$30. \frac{1}{40} \log 9$$

$$31. \frac{\pi}{2} - 1$$

$$32. \frac{\pi}{2} (\pi - 2)$$

$$33. \frac{19}{2}$$

$$40. \frac{1}{3} \left( e^2 - \frac{1}{e} \right)$$

$$41. A$$

$$42. B$$

$$43. D$$

$$44. B$$

### EXERCISE 8.1

$$1. \frac{14}{3}$$

$$2. 16 - 4\sqrt{2}$$

$$3. \frac{32 - 8\sqrt{2}}{3}$$

$$4. 12\pi$$

$$5. 6\pi$$

$$6. \frac{\pi}{3}$$

$$7. \frac{a^2}{2} \left( \frac{\pi}{2} - 1 \right)$$

$$8. (4)^{\frac{2}{3}}$$

$$9. \frac{1}{3}$$

$$10. \frac{9}{8}$$

$$11. 8\sqrt{3}$$

$$12. A$$

$$13. B$$

**EXERCISE 8.2**

1.  $\frac{\sqrt{2}}{6} + \frac{9}{4} \sin^{-1} \frac{2\sqrt{2}}{3}$

2.  $\left( \frac{2\pi}{3} - \frac{\sqrt{3}}{2} \right)$

3.  $\frac{21}{2}$

4. 4

5. 8

6. B

7. B

**Miscellaneous Exercise on Chapter 8**

1. (i)  $\frac{7}{3}$

(ii) 624.8

2.  $\frac{1}{6}$

3.  $\frac{7}{3}$

4. 9

5. 4

6.  $\frac{8a^2}{3m^3}$

7. 27

8.  $\frac{3}{2}(\pi - 2)$

9.  $\frac{ab}{4}(\pi - 2)$

10.  $\frac{5}{6}$

11. 2

12.  $\frac{1}{3}$

13. 7

14.  $\frac{7}{2}$

15.  $\frac{9\pi}{8} - \frac{9}{4} \sin^{-1} \left( \frac{1}{3} \right) + \frac{1}{3\sqrt{2}}$

16. D

17. C

18. C

19. B

**EXERCISE 9.1**

1. Order 4; Degree not defined

2. Order 1; Degree 1

3. Order 2; Degree 1

4. Order 2; Degree not defined

5. Order 2; Degree 1

6. Order 3; Degree 2

7. Order 3; Degree 1

8. Order 1; Degree 1

9. Order 2; Degree 1

10. Order 2; Degree 1

11. D

12. A

**EXERCISE 9.2**

11. D

12. D

**EXERCISE 9.3**

1.  $y'' = 0$
2.  $xy y'' + x (y')^2 - y y' = 0$
3.  $y'' - y' - 6y = 0$
4.  $y'' - 4y' + 4y = 0$
5.  $y'' - 2y' + 2y = 0$
6.  $2xyy' + x^2 = y^2$
7.  $xy' - 2y = 0$
8.  $xyy'' + x(y')^2 - yy' = 0$
9.  $xyy'' + x(y')^2 - yy' = 0$
10.  $(x^2 - 9)(y')^2 + x^2 = 0$
11. B
12. C

**EXERCISE 9.4**

1.  $y = 2 \tan \frac{x}{2} - x + C$
2.  $y = 2 \sin (x + C)$
3.  $y = 1 + Ae^{-x}$
4.  $\tan x \tan y = C$
5.  $y = \log (e^x + e^{-x}) + C$
6.  $\tan^{-1} y = x + \frac{x^3}{3} + C$
7.  $y = e^{cx}$
8.  $x^{-4} + y^{-4} = C$
9.  $y = x \sin^{-1} x + \sqrt{1 - x^2} + C$
10.  $\tan y = C (1 - e^x)$
11.  $y = \frac{1}{4} \log [(x+1)^2 (x^2+1)^3] - \frac{1}{2} \tan^{-1} x + 1$
12.  $y = \frac{1}{2} \log \left( \frac{x^2-1}{x^2} \right) - \frac{1}{2} \log \frac{3}{4}$
13.  $\cos \left( \frac{y-2}{x} \right) = a$
14.  $y = \sec x$
15.  $2y - 1 = e^x (\sin x - \cos x)$
16.  $y - x + 2 = \log (x^2 (y + 2)^2)$
17.  $y^2 - x^2 = 4$
18.  $(x + 4)^2 = y + 3$
19.  $(63t + 27)^{\frac{1}{3}}$
20. 6.93%
21. Rs 1648
22.  $\frac{2 \log 2}{\log \left( \frac{11}{10} \right)}$
23. A

**EXERCISE 9.5**

1.  $(x-y)^2 = Cx e^{\frac{-y}{x}}$
2.  $y = x \log |x| + Cx$

3.  $\tan^{-1}\left(\frac{y}{x}\right) = \frac{1}{2} \log(x^2 + y^2) + C$       4.  $x^2 + y^2 = Cx$
5.  $\frac{1}{2\sqrt{2}} \log \left| \frac{x + \sqrt{2}y}{x - \sqrt{2}y} \right| = \log|x| + C$       6.  $y + \sqrt{x^2 + y^2} = Cx^2$
7.  $xy \cos \left| \frac{y}{x} \right| = C$       8.  $x \left[ 1 - \cos \left( \frac{y}{x} \right) \right] = C \sin \left( \frac{y}{x} \right)$
9.  $cy = \log \left| \frac{y}{x} \right| - 1$       10.  $ye^{\frac{x}{y}} + x = C$
11.  $\log(x^2 + y^2) + 2 \tan^{-1} \frac{y}{x} = \frac{\pi}{2} + \log 2$
12.  $y + 2x = 3x^2 y$       13.  $\cot \left( \frac{y}{x} \right) = \log|ex|$
14.  $\cos \left( \frac{y}{x} \right) = \log|ex|$       15.  $y = \frac{2x}{1 - \log|x|} \quad (x \neq 0, x \neq e)$
16. C      17. D

### EXERCISE 9.6

1.  $y = \frac{1}{5} (2 \sin x - \cos x) + C e^{-2x}$       2.  $y = e^{-2x} + C e^{-3x}$
3.  $xy = \frac{x^4}{4} + C$       4.  $y(\sec x + \tan x) = \sec x + \tan x - x + C$
5.  $y = (\tan x - 1) + C e^{-\tan x}$       6.  $y = \frac{x^2}{16} (4 \log|x| - 1) + C x^{-2}$
7.  $y \log x = \frac{-2}{x} (1 + \log|x|) + C$       8.  $y = (1+x)^{-1} \log|\sin x| + C(1+x^2)^{-1}$
9.  $y = \frac{1}{x} - \cot x + \frac{C}{x \sin x}$       10.  $(x + y + 1) = C e^y$
11.  $x = \frac{y^2}{3} + \frac{C}{y}$       12.  $x = 3y^2 + Cy$

13.  $y = \cos x - 2 \cos^2 x$

14.  $y(1 + x^2) = \tan^{-1} x - \frac{\pi}{4}$

15.  $y = 4 \sin^3 x - 2 \sin^2 x$

16.  $x + y + 1 = e^x$

17.  $y = 4 - x - 2e^x$

18. C

19. D

**Miscellaneous Exercise on Chapter 9**

1. (i) Order 2; Degree 1      (ii) Order 1; Degree 3

(iii) Order 4; Degree not defined

3.  $y' = \frac{2y^2 - x^2}{4xy}$

5.  $(x + yy')^2 = (x - y)^2 (1 + (y')^2)$

6.  $\sin^{-1} y + \sin^{-1} x = C$

8.  $\cos y = \frac{\sec x}{\sqrt{2}}$

9.  $\tan^{-1} y + \tan^{-1}(e^x) = \frac{\pi}{2}$

10.  $e^{\frac{x}{y}} = y + C$

11.  $\log |x - y| = x + y + 1$

12.  $ye^{2\sqrt{x}} = (2\sqrt{x} + C)$

13.  $y \sin x = 2x^2 - \frac{\pi^2}{2} \quad (\sin x \neq 0)$

14.  $y = \log \left| \frac{2x+1}{x+1} \right|, x \neq -1$

15. 31250

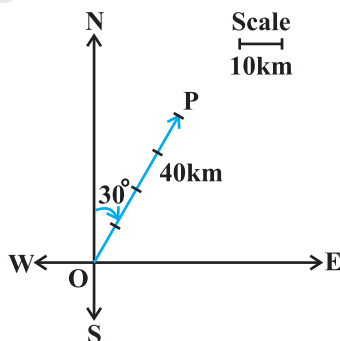
16. C

17. C

18. C

**EXERCISE 10.1**

1. In the adjoining figure, the vector
- $\overrightarrow{OP}$
- represents the required displacement.



2. (i) scalar (ii) vector (iii) scalar (iv) scalar (v) scalar  
(vi) vector
3. (i) scalar (ii) scalar (iii) vector (iv) vector (v) scalar
4. (i) Vectors  $\vec{a}$  and  $\vec{b}$  are coinitial  
(ii) Vectors  $\vec{b}$  and  $\vec{d}$  are equal  
(iii) Vectors  $\vec{a}$  and  $\vec{c}$  are collinear but not equal
5. (i) True (ii) False (iii) False (iv) False

### EXERCISE 10.2

1.  $|\vec{a}|=\sqrt{3}, |\vec{b}|=\sqrt{62}, |\vec{c}|=1$
2. An infinite number of possible answers.
3. An infinite number of possible answers.
4.  $x=2, y=3$
5.  $-7$  and  $6; -7\hat{i}$  and  $6\hat{j}$
6.  $-4\hat{j}-\hat{k}$
7.  $\frac{1}{\sqrt{6}}\hat{i}+\frac{1}{\sqrt{6}}\hat{j}+\frac{2}{\sqrt{6}}\hat{k}$
8.  $\frac{1}{\sqrt{3}}\hat{i}+\frac{1}{\sqrt{3}}\hat{j}+\frac{1}{\sqrt{3}}\hat{k}$
9.  $\frac{1}{\sqrt{2}}\hat{i}+\frac{1}{\sqrt{2}}\hat{k}$
10.  $\frac{40}{\sqrt{30}}\hat{i}-\frac{8}{\sqrt{30}}\hat{j}+\frac{16}{\sqrt{30}}\hat{k}$
12.  $\frac{1}{\sqrt{14}}, \frac{2}{\sqrt{14}}, \frac{3}{\sqrt{14}}$
13.  $-\frac{1}{3}, -\frac{2}{3}, \frac{2}{3}$
15. (i)  $-\frac{1}{3}\hat{i}+\frac{4}{3}\hat{j}+\frac{1}{3}\hat{k}$  (ii)  $-3\hat{i}+3\hat{k}$
16.  $3\hat{i}+2\hat{j}+\hat{k}$
18. (C)
19. (B), (C), (D)

### EXERCISE 10.3

1.  $\frac{\pi}{4}$
2.  $\cos^{-1}\left(\frac{5}{7}\right)$
3. 0
4.  $\frac{60}{\sqrt{114}}$
6.  $\frac{16\sqrt{2}}{3\sqrt{7}}, \frac{2\sqrt{2}}{3\sqrt{7}}$
7.  $6|\vec{a}|^2+11\vec{a}.\vec{b}-35|\vec{b}|^2$
8.  $|\vec{a}|=1, |\vec{b}|=1$
9.  $\sqrt{13}$
10. 8

12. Vector  $\vec{b}$  can be any vector
13.  $\frac{-3}{2}$
14. Take any two non-zero perpendicular vectors  $\vec{a}$  and  $\vec{b}$
15.  $\cos^{-1}\left(\frac{10}{\sqrt{102}}\right)$
18. (D)

### EXERCISE 10.4

1.  $19\sqrt{2}$
2.  $\pm\frac{2}{3}\hat{i} \mp \frac{2}{3}\hat{j} \mp \frac{1}{3}\hat{k}$
3.  $\frac{\pi}{3}; \frac{1}{2}, \frac{1}{\sqrt{2}}, \frac{1}{2}$
5.  $3, \frac{27}{2}$
6. Either  $|\vec{a}|=0$  or  $|\vec{b}|=0$
8. No; take any two nonzero collinear vectors
9.  $\frac{\sqrt{61}}{2}$
10.  $15\sqrt{2}$
11. (B)
12. (C)

### Miscellaneous Exercise on Chapter 10

1.  $\frac{\sqrt{3}}{2}\hat{i} + \frac{1}{2}\hat{j}$
2.  $x_2 - x_1, y_2 - y_1, z_2 - z_1; \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$
3.  $\frac{-5}{2}\hat{i} + \frac{3\sqrt{3}}{2}\hat{j}$
4. No; take  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  to represent the sides of a triangle.
5.  $\pm\frac{1}{\sqrt{3}}$
6.  $\frac{3}{2}\sqrt{10}\hat{i} + \frac{\sqrt{10}}{2}\hat{j}$
7.  $\frac{3}{\sqrt{22}}\hat{i} - \frac{3}{\sqrt{22}}\hat{j} + \frac{2}{\sqrt{22}}\hat{k}$
8. 2 : 3
9.  $3\vec{a} + 5\vec{b}$
10.  $\frac{1}{7}(3\hat{i} - 6\hat{j} + 2\hat{k}); 11\sqrt{5}$
12.  $\frac{1}{3}(160\hat{i} - 5\hat{j} + 70\hat{k})$
13.  $\lambda = 1$
16. (B)
17. (D)
18. (C)
19. (B)



## EXERCISE 11.1

1.  $0, \frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}$       2.  $\pm \frac{1}{\sqrt{3}}, \pm \frac{1}{\sqrt{3}}, \pm \frac{1}{\sqrt{3}}$       3.  $\frac{-9}{11}, \frac{6}{11}, \frac{-2}{11}$   
 5.  $\frac{-2}{\sqrt{17}}, \frac{-2}{\sqrt{17}}, \frac{3}{17}; \frac{-2}{\sqrt{17}}, \frac{-3}{\sqrt{17}}, \frac{-2}{\sqrt{17}}; \frac{4}{\sqrt{42}}, \frac{5}{\sqrt{42}}, \frac{-1}{\sqrt{42}}$

## EXERCISE 11.2

4.  $\vec{r} = \hat{i} + 2\hat{j} + 3\hat{k} + \lambda(3\hat{i} + 2\hat{j} - 2\hat{k})$ , where  $\lambda$  is a real number  
 5.  $\vec{r} = 2\hat{i} - \hat{j} + 4\hat{k} + \lambda(\hat{i} + 2\hat{j} - \hat{k})$  and cartesian form is  

$$\frac{x-2}{1} = \frac{y+1}{2} = \frac{z-4}{-1}$$
  
 6. 
$$\frac{x+2}{3} = \frac{y-4}{5} = \frac{z+5}{6}$$
  
 7.  $\vec{r} = (5\hat{i} - 4\hat{j} + 6\hat{k}) + \lambda(3\hat{i} + 7\hat{j} + 2\hat{k})$   
 8. Vector equation of the line:  $\vec{r} = \lambda(5\hat{i} - 2\hat{j} + 3\hat{k})$ ;  
 Cartesian equation of the line:  $\frac{x}{5} = \frac{y}{-2} = \frac{z}{3}$   
 9. Vector equation of the line:  $\vec{r} = 3\hat{i} - 2\hat{j} - 5\hat{k} + \lambda(11\hat{k})$   
 Cartesian equation of the line:  $\frac{x-3}{0} = \frac{y+2}{0} = \frac{z+5}{11}$   
 10. (i)  $\theta = \cos^{-1}\left(\frac{19}{21}\right)$       (ii)  $\theta = \cos^{-1}\left(\frac{8}{5\sqrt{3}}\right)$   
 11. (i)  $\theta = \cos^{-1}\left(\frac{26}{9\sqrt{38}}\right)$       (ii)  $\theta = \cos^{-1}\left(\frac{2}{3}\right)$   
 12.  $p = \frac{70}{11}$       14.  $\frac{3\sqrt{2}}{2}$       15.  $2\sqrt{29}$   
 16.  $\frac{3}{\sqrt{19}}$       17.  $\frac{8}{\sqrt{29}}$

## EXERCISE 11.3

1. (a) 0, 0, 1; 2 (b)  $\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}; \frac{1}{\sqrt{3}}$
- (c)  $\frac{2}{\sqrt{14}}, \frac{3}{\sqrt{14}}, \frac{-1}{\sqrt{14}}; \frac{5}{\sqrt{14}}$  (d) 0, 1, 0;  $\frac{8}{5}$
2.  $\vec{r} \cdot \left( \frac{3\hat{i} + 5\hat{j} - 6\hat{k}}{\sqrt{70}} \right) = 7$
3. (a)  $x + y - z = 2$  (b)  $2x + 3y - 4z = 1$   
 (c)  $(s - 2t)x + (3 - t)y + (2s + t)z = 15$
4. (a)  $\left( \frac{24}{29}, \frac{36}{29}, \frac{48}{29} \right)$  (b)  $\left( 0, \frac{18}{25}, \frac{24}{25} \right)$   
 (c)  $\left( \frac{1}{3}, \frac{1}{3}, \frac{1}{3} \right)$  (d)  $\left( 0, \frac{-8}{5}, 0 \right)$
5. (a)  $[\vec{r} - (\hat{i} - 2\hat{k})] \cdot (\hat{i} + \hat{j} - \hat{k}) = 0; x + y - z = 3$   
 (b)  $[\vec{r} - (\hat{i} + 4\hat{j} + 6\hat{k})] \cdot (\hat{i} - 2\hat{j} + \hat{k}) = 0; x - 2y + z + 1 = 0$
6. (a) The points are collinear. There will be infinite number of planes passing through the given points.  
 (b)  $2x + 3y - 3z = 5$
7.  $\frac{5}{2}, 5, -5$  8.  $y = 3$  9.  $7x - 5y + 4z - 8 = 0$
10.  $\vec{r} \cdot (38\hat{i} + 68\hat{j} + 3\hat{k}) = 153$  11.  $x - z + 2 = 0$
12.  $\cos^{-1} \frac{15}{\sqrt{731}}$
13. (a)  $\cos^{-1} \left( \frac{2}{5} \right)$  (b) The planes are perpendicular  
 (c) The planes are parallel (d) The planes are parallel  
 (e)  $45^\circ$
14. (a)  $\frac{3}{13}$  (b)  $\frac{13}{3}$   
 (c) 3 (d) 2

**Miscellaneous Exercise on Chapter 11**

3.  $90^\circ$                       4.  $\frac{x}{1} = \frac{y}{0} = \frac{z}{0}$                       5.  $0^\circ$
6.  $k = \frac{-10}{7}$                       7.  $\vec{r} = \hat{i} + 2\hat{j} + 3\hat{k} + \lambda(\hat{i} + 2\hat{j} - 5\hat{k})$
8.  $x + y + z = a + b + c$                       9. 9
10.  $\left(0, \frac{17}{2}, \frac{-13}{2}\right)$                       11.  $\left(\frac{17}{3}, 0, \frac{23}{3}\right)$                       12.  $(1, -2, 7)$
13.  $7x - 8y + 3z + 25 = 0$                       14.  $p = \frac{3}{2}$  or  $\frac{11}{6}$  or  $\frac{7}{3}$
15.  $y - 3z + 6 = 0$                       16.  $x + 2y - 3z - 14 = 0$
17.  $33x + 45y + 50z - 41 = 0$                       18. 13
19.  $\vec{r} = \hat{i} + 2\hat{j} + 3\hat{k} + \lambda(-3\hat{i} + 5\hat{j} + 4\hat{k})$
20.  $\vec{r} = \hat{i} + 2\hat{j} - 4\hat{k} + \lambda(2\hat{i} + 3\hat{j} + 6\hat{k})$                       22. D
23. B

**EXERCISE 12.1**

1. Maximum  $Z = 16$  at  $(0, 4)$
2. Minimum  $Z = -12$  at  $(4, 0)$
3. Maximum  $Z = \frac{235}{19}$  at  $\left(\frac{20}{19}, \frac{45}{19}\right)$
4. Minimum  $Z = 7$  at  $\left(\frac{3}{2}, \frac{1}{2}\right)$
5. Maximum  $Z = 18$  at  $(4, 3)$
6. Minimum  $Z = 6$  at all the points on the line segment joining the points  $(6, 0)$  and  $(0, 3)$ .
7. Minimum  $Z = 300$  at  $(60, 0)$ ;  
Maximum  $Z = 600$  at all the points on the line segment joining the points  $(120, 0)$  and  $(60, 30)$ .

8. Minimum  $Z = 100$  at all the points on the line segment joining the points  $(0, 50)$  and  $(20, 40)$ ;  
Maximum  $Z = 400$  at  $(0, 200)$
9.  $Z$  has no maximum value
10. No feasible region, hence no maximum value of  $Z$ .

### EXERCISE 12.2

1. Minimum cost = Rs 160 at all points lying on segment joining  $\frac{8}{3}, 0$  and  $2, \frac{1}{2}$ .
2. Maximum number of cakes = 30 of kind one and 10 cakes of another kind.
3. (i) 4 tennis rackets and 12 cricket bats  
(ii) Maximum profit = Rs 200
4. 3 packages of nuts and 3 packages of bolts; Maximum profit = Rs 73.50.
5. 30 packages of screws A and 20 packages of screws B; Maximum profit = Rs 410
6. 4 Pedestal lamps and 4 wooden shades; Maximum profit = Rs 32
7. 8 Souvenir of types A and 20 of Souvenir of type B; Maximum profit = Rs 160.
8. 200 units of desktop model and 50 units of portable model; Maximum profit = Rs 1150000.
9. Minimise  $Z = 4x + 6y$   
subject to  $3x + 6y \geq 80$ ,  $4x + 3y \geq 100$ ,  $x \geq 0$  and  $y \geq 0$ , where  $x$  and  $y$  denote the number of units of food  $F_1$  and food  $F_2$  respectively; Minimum cost = Rs 104
10. 100 kg of fertiliser  $F_1$  and 80 kg of fertiliser  $F_2$ ; Minimum cost = Rs 1000
11. (D)

### Miscellaneous Exercise on Chapter 12

1. 40 packets of food P and 15 packets of food Q; Maximum amount of vitamin A = 285 units.
2. 3 bags of brand P and 6 bags of brand Q; Minimum cost of the mixture = Rs 1950
3. Least cost of the mixture is Rs 112 (2 kg of Food X and 4 kg of food Y).

5. 40 tickets of executive class and 160 tickets of economy class; Maximum profit = Rs 136000.
6. From A : 10,50, 40 units; From B: 50,0,0 units to D, E and F respectively and minimum cost = Rs 510
7. From A: 500, 3000 and 3500 litres; From B: 4000, 0, 0 litres to D, E and F respectively; Minimum cost = Rs 4400
8. 40 bags of brand P and 100 bags of brand Q; Minimum amount of nitrogen = 470 kg.
9. 140 bags of brand P and 50 bags of brand Q; Maximum amount of nitrogen = 595 kg.
10. 800 dolls of type A and 400 dolls of type B; Maximum profit = Rs 16000

### EXERCISE 13.1

1.  $P(E|F) = \frac{2}{3}$ ,  $P(F|E) = \frac{1}{3}$
2.  $P(A|B) = \frac{16}{25}$
3. (i) 0.32 (ii) 0.64 (iii) 0.98
4.  $\frac{11}{26}$
5. (i)  $\frac{4}{11}$  (ii)  $\frac{4}{5}$  (iii)  $\frac{2}{3}$
6. (i)  $\frac{1}{2}$  (ii)  $\frac{3}{7}$  (iii)  $\frac{6}{7}$
7. (i) 1 (ii) 0
8.  $\frac{1}{6}$  9. 1 10. (a)  $\frac{1}{3}$ , (b)  $\frac{1}{9}$
11. (i)  $\frac{1}{2}, \frac{1}{3}$  (ii)  $\frac{1}{2}, \frac{2}{3}$  (iii)  $\frac{3}{4}, \frac{1}{4}$
12. (i)  $\frac{1}{2}$  (ii)  $\frac{1}{3}$  13.  $\frac{5}{9}$
14.  $\frac{1}{15}$  15. 0 16. C 17. D

**EXERCISE 13.2**

1.  $\frac{3}{25}$       2.  $\frac{25}{102}$       3.  $\frac{44}{91}$   
 4. A and B are independent      5. A and B are not independent  
 6. E and F are not independent  
 7. (i)  $p = \frac{1}{10}$       (ii)  $p = \frac{1}{5}$   
 8. (i) 0.12      (ii) 0.58      (iii) 0.3      (iv) 0.4  
 9.  $\frac{3}{8}$       10. A and B are not independent  
 11. (i) 0.18      (ii) 0.12      (iii) 0.72      (iv) 0.28  
 12.  $\frac{7}{8}$       13. (i)  $\frac{16}{81}$ , (ii)  $\frac{20}{81}$ , (iii)  $\frac{40}{81}$   
 14. (i)  $\frac{2}{3}$ , (ii)  $\frac{1}{2}$       15. (i), (ii)      16. (a)  $\frac{1}{5}$ , (b)  $\frac{1}{3}$ , (c)  $\frac{1}{2}$   
 17. D      18. B

**EXERCISE 13.3**

1.  $\frac{1}{2}$       2.  $\frac{2}{3}$       3.  $\frac{9}{13}$       4.  $\frac{12}{13}$   
 5.  $\frac{22}{133}$       6.  $\frac{4}{9}$       7.  $\frac{1}{52}$       8.  $\frac{1}{4}$   
 9.  $\frac{2}{9}$       10.  $\frac{8}{11}$       11.  $\frac{5}{34}$       12.  $\frac{11}{50}$   
 13. A      14. C

**EXERCISE 13.4**

1. (ii), (iii) and (iv)      2.  $X = 0, 1, 2$ ; yes      3.  $X = 6, 4, 2, 0$

4. (i)

|      |               |               |               |
|------|---------------|---------------|---------------|
| X    | 0             | 1             | 2             |
| P(X) | $\frac{1}{4}$ | $\frac{1}{2}$ | $\frac{1}{4}$ |

(ii)

|      |               |               |               |               |
|------|---------------|---------------|---------------|---------------|
| X    | 0             | 1             | 2             | 3             |
| P(X) | $\frac{1}{8}$ | $\frac{3}{8}$ | $\frac{3}{8}$ | $\frac{1}{8}$ |

(iii)

|      |                |               |               |               |                |
|------|----------------|---------------|---------------|---------------|----------------|
| X    | 0              | 1             | 2             | 3             | 4              |
| P(X) | $\frac{1}{16}$ | $\frac{1}{4}$ | $\frac{3}{8}$ | $\frac{1}{4}$ | $\frac{1}{16}$ |

5. (i)

|      |               |               |               |
|------|---------------|---------------|---------------|
| X    | 0             | 1             | 2             |
| P(X) | $\frac{4}{9}$ | $\frac{4}{9}$ | $\frac{1}{9}$ |

(ii)

|      |                 |                 |
|------|-----------------|-----------------|
| X    | 0               | 1               |
| P(X) | $\frac{25}{36}$ | $\frac{11}{36}$ |

6.

|      |                   |                   |                  |                  |                 |
|------|-------------------|-------------------|------------------|------------------|-----------------|
| X    | 0                 | 1                 | 2                | 3                | 4               |
| P(X) | $\frac{256}{625}$ | $\frac{256}{625}$ | $\frac{96}{625}$ | $\frac{16}{625}$ | $\frac{1}{625}$ |

7.

|      |                |                |                |
|------|----------------|----------------|----------------|
| X    | 0              | 1              | 2              |
| P(X) | $\frac{9}{16}$ | $\frac{6}{16}$ | $\frac{1}{16}$ |

8. (i)  $k = \frac{1}{10}$  (ii)  $P(X < 3) = \frac{3}{10}$  (iii)  $P(X > 6) = \frac{17}{100}$

(iv)  $P(0 < X < 3) = \frac{3}{10}$

9. (a)  $k = \frac{1}{6}$  (b)  $P(X < 2) = \frac{1}{2}$ ,  $P(X \leq 2) = 1$ ,  $P(X \geq 2) = \frac{1}{2}$

10. 1.5 11.  $\frac{1}{3}$  12.  $\frac{14}{3}$

13.  $\text{Var}(X) = 5.833$ ,  $\text{S.D} = 2.415$

14.

|      |                |                |                |                |                |                |                |                |
|------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
| X    | 14             | 15             | 16             | 17             | 18             | 19             | 20             | 21             |
| P(X) | $\frac{2}{15}$ | $\frac{1}{15}$ | $\frac{2}{15}$ | $\frac{3}{15}$ | $\frac{1}{15}$ | $\frac{2}{15}$ | $\frac{3}{15}$ | $\frac{1}{15}$ |

Mean = 17.53,  $\text{Var}(X) = 4.78$  and  $\text{S.D}(X) = 2.19$

15.  $E(X) = 0.7$  and  $\text{Var}(X) = 0.21$

16. B

17. D

### EXERCISE 13.5

1. (i)  $\frac{3}{32}$

(ii)  $\frac{7}{64}$

(iii)  $\frac{63}{64}$

2.  $\frac{25}{216}$

3.  $\left(\frac{29}{20}\right)\left(\frac{19}{20}\right)^9$

4. (i)  $\frac{1}{1024}$

(ii)  $\frac{45}{512}$

(iii)  $\frac{243}{1024}$

5. (i)  $(0.95)^5$

(ii)  $(0.95)^4 \times 1.2$

(iii)  $1 - (0.95)^4 \times 1.2$

(iv)  $1 - (0.95)^5$

6.  $\left(\frac{9}{10}\right)^4$

7.  $\left(\frac{1}{2}\right)^{20} [20C_{12} + {}^{20}C_{13} + \dots + {}^{20}C_{20}]$

9.  $\frac{11}{243}$

10. (a)  $1 - \left(\frac{99}{100}\right)^{50}$

(b)  $\frac{1}{2} \left(\frac{99}{100}\right)^{49}$

(c)  $1 - \frac{149}{100} \left(\frac{99}{100}\right)^{49}$

11.  $\frac{7}{12} \left(\frac{5}{6}\right)^5$

12.  $\frac{35}{18} \left(\frac{5}{6}\right)^4$

13.  $\frac{22 \times 9^3}{10^{11}}$

14. C

15. A

### Miscellaneous Exercise on Chapter 13

1. (i) 1

(ii) 0

2. (i)  $\frac{1}{3}$

(ii)  $\frac{1}{2}$

3.  $\frac{20}{21}$

4.  $1 - \sum_{r=7}^{10} {}^{10}C_r (0.9)^r (0.1)^{10-r}$

5. (i)  $\left(\frac{2}{5}\right)^6$

(ii)  $7\left(\frac{2}{5}\right)^4$

(iii)  $1 - \left(\frac{2}{5}\right)^6$

(iv)  $\frac{864}{3125}$



6.  $\frac{5^{10}}{2 \times 6^9}$

7.  $\frac{625}{23328}$

8.  $\frac{2}{7}$

9.  $\frac{31}{9} \left( \frac{2}{3} \right)^4$

10.  $n \geq 4$

11.  $\frac{-91}{54}$

12.  $\frac{1}{15}, \frac{2}{5}, \frac{8}{15}$

13.  $\frac{14}{29}$

14.  $\frac{3}{16}$

15. (i) 0.5      (ii) 0.05

16.  $\frac{16}{31}$

17. A

18. C

19. B

