

# Applied Mathematics

## Class XI



**CENTRAL BOARD OF  
SECONDARY EDUCATION**

**Shiksha Sadan, 17, Institutional Area,  
Rouse Avenue, New Delhi-110 002**

*Dedicated to:*



**Sh. Pramod Kumar T.K.**

**(15th April 1971 to 25th May 2021)**

**Joint Secretary (Academics)  
Central Board of Secondary Education**

*You will always be in our memories...*

# Applied Mathematics

Class XI

Student Support Material



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## Applied Mathematics - Class XI

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## भारत का संविधान

### उद्देशिका

हम, भारत के लोग, भारत को एक सम्पूर्ण 'प्रभुत्व-संपन्न समाजवादी पंथनिरपेक्ष लोकतंत्रात्मक गणराज्य बनाने के लिए, तथा उसके समस्त नागरिकों को:

सामाजिक, आर्थिक और राजनैतिक न्याय,  
विचार, अभिव्यक्ति, विश्वास, धर्म

और उपासना की स्वतंत्रता,  
प्रतिष्ठा और अवसर की समता

प्राप्त कराने के लिए  
तथा उन सब में व्यक्ति की गरिमा

<sup>2</sup>और राष्ट्र की एकता और अखंडता  
सुनिश्चित करने वाली बंधुता बढ़ाने के लिए

दृढ़संकल्प होकर अपनी इस संविधान सभा में आज तारीख 26 नवम्बर, 1949 ई० को एतद्द्वारा इस संविधान को अंगीकृत, अधिनियमित और आत्मार्पित करते हैं।

1. संविधान ( बयालीसवां संशोधन ) अधिनियम, 1976 की धारा 2 द्वारा ( 3.1.1977 ) से "प्रभुत्व-संपन्न लोकतंत्रात्मक गणराज्य" के स्थान पर प्रतिस्थापित।
2. संविधान ( बयालीसवां संशोधन ) अधिनियम, 1976 की धारा 2 द्वारा ( 3.1.1977 ) से "राष्ट्र की एकता" के स्थान पर प्रतिस्थापित।

### भाग 4 क

### मूल कर्तव्य

**51 क. मूल कर्तव्य** - भारत के प्रत्येक नागरिक का यह कर्तव्य होगा कि वह -

- (क) संविधान का पालन करे और उसके आदर्शों, संस्थाओं, राष्ट्रध्वज और राष्ट्रगान का आदर करे;
- (ख) स्वतंत्रता के लिए हमारे राष्ट्रीय आंदोलन को प्रेरित करने वाले उच्च आदर्शों को हृदय में संजोए रखे और उनका पालन करे;
- (ग) भारत की प्रभुता, एकता और अखंडता की रक्षा करे और उसे अक्षुण्ण रखे;
- (घ) देश की रक्षा करे और आह्वान किए जाने पर राष्ट्र की सेवा करे;
- (ङ) भारत के सभी लोगों में समरसता और समान भ्रातृत्व की भावना का निर्माण करे जो धर्म, भाषा और प्रदेश या वर्ग पर आधारित सभी भेदभाव से परे हों, ऐसी प्रथाओं का त्याग करे जो स्त्रियों के सम्मान के विरुद्ध हैं;
- (च) हमारी सामासिक संस्कृति की गौरवशाली परंपरा का महत्त्व समझे और उसका परिरक्षण करे;
- (छ) प्राकृतिक पर्यावरण की जिसके अंतर्गत वन, झील, नदी, और वन्य जीव हैं, रक्षा करे और उसका संवर्धन करे तथा प्राणी मात्र के प्रति दयाभाव रखे;
- (ज) वैज्ञानिक दृष्टिकोण, मानववाद और ज्ञानार्जन तथा सुधार की भावना का विकास करे;
- (झ) सार्वजनिक संपत्ति को सुरक्षित रखे और हिंसा से दूर रहे;
- (ञ) व्यक्तिगत और सामूहिक गतिविधियों के सभी क्षेत्रों में उत्कर्ष की ओर बढ़ने का सतत प्रयास करे जिससे राष्ट्र निरंतर बढ़ते हुए प्रयत्न और उपलब्धि की नई उंचाइयों को छू ले;
- <sup>1</sup>(ट) यदि माता-पिता या संरक्षक हैं, छह वर्ष से चौदह वर्ष तक की आयु वाले अपने, यथास्थिति, बालक या प्रतिपाल्य के लिये शिक्षा के अवसर प्रदान करे।

1. संविधान ( छयासीवां संशोधन ) अधिनियम, 2002 की धारा 4 द्वारा प्रतिस्थापित।

# THE CONSTITUTION OF INDIA

## PREAMBLE

**WE, THE PEOPLE OF INDIA**, having solemnly resolved to constitute India into a <sup>1</sup>**[SOVEREIGN SOCIALIST SECULAR DEMOCRATIC REPUBLIC]** and to secure to all its citizens :

**JUSTICE**, social, economic and political;

**LIBERTY** of thought, expression, belief, faith and worship;

**EQUALITY** of status and of opportunity; and to promote among them all

**FRATERNITY** assuring the dignity of the individual and the<sup>2</sup> [unity and integrity of the Nation];

**IN OUR CONSTITUENT ASSEMBLY** this twenty-sixth day of November, 1949, do **HEREBY ADOPT, ENACT AND GIVE TO OURSELVES THIS CONSTITUTION.**

1. Subs, by the Constitution (Forty-Second Amendment) Act, 1976, sec. 2, for "Sovereign Democratic Republic" (w.e.f. 3.1.1977)
2. Subs, by the Constitution (Forty-Second Amendment) Act, 1976, sec. 2, for "unity of the Nation" (w.e.f. 3.1.1977)

# THE CONSTITUTION OF INDIA

## Chapter IV A

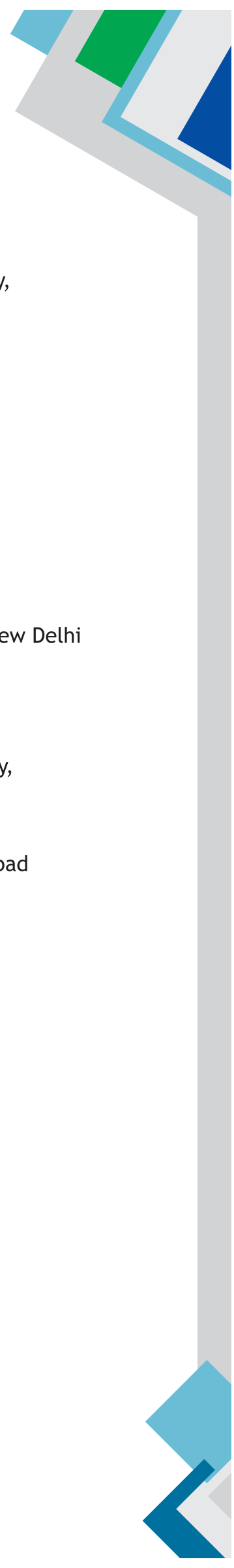
### FUNDAMENTAL DUTIES

#### ARTICLE 51A

**Fundamental Duties** - It shall be the duty of every citizen of India-

- (a) to abide by the Constitution and respect its ideals and institutions, the National Flag and the National Anthem;
- (b) to cherish and follow the noble ideals which inspired our national struggle for freedom;
- (c) to uphold and protect the sovereignty, unity and integrity of India;
- (d) to defend the country and render national service when called upon to do so;
- (e) to promote harmony and the spirit of common brotherhood amongst all the people of India transcending religious, linguistic and regional or sectional diversities; to renounce practices derogatory to the dignity of women;
- (f) to value and preserve the rich heritage of our composite culture;
- (g) to protect and improve the natural environment including forests, lakes, rivers, wild life and to have compassion for living creatures;
- (h) to develop the scientific temper, humanism and the spirit of inquiry and reform;
- (i) to safeguard public property and to abjure violence;
- (j) to strive towards excellence in all spheres of individual and collective activity so that the nation constantly rises to higher levels of endeavour and achievement;
- <sup>1</sup>(k) who is a parent or guardian to provide opportunities for education to his/her child or, as the case may be, ward between age of six and fourteen years.

1. Ins. by the constitution (Eighty - Sixth Amendment) Act, 2002 S.4 (w.e.f. 12.12.2002)



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## Note to the user

The technological, economic, and social changes of the last few decades have redefined the scope and relevance of important mathematical ideas in work and in everyday life. With exponential rise in applications of Mathematics influencing almost every aspect of human lives, it necessitates preparing mathematically skilled workforce who can make informed decisions in their professional and personal lives. India has rich and diverse landscape of learning contexts that requires effective mathematical solutions. Such mathematically illuminated contexts can contribute to the development of mathematics curriculum mapping the country's need and spirit. Moreover Mathematics skills are very much essential in all the fields be it art, literature or social sciences.

The present course in Applied Mathematics is application centric and problem driven. Key mathematical ideas are developed within and around the contexts that have potential applications in practical life. The course aims to develop new perspectives about what Mathematics is and how it can be used. The course is divided into different units each focusing on numerical, algebraic or statistical applications. The scope of the course ranges from mathematical applications in the field of financial and services (including Business and Economics), Pharmaceutical industry, Hospitality and Entertainment industry, Advertisement and Marketing sector, Healthcare Services including Counseling Services, Agricultural Sector, Government-aided programs such as resources distribution, Traffic Management Systems including Air Traffic Management, Infrastructure Development, Archeological Studies and studies on Historiography, real time data analysis and many more. Core mathematical ideas are presented keeping in mind these contexts.

The course aims to develop among learners the habit of mathematical thinking by reasoning quantitatively; constructing viable mathematical arguments; constructing new mathematical knowledge using problem solving and learning to model with Mathematics.

This student support material is divided into different units including a unit on use of spreadsheet for mathematical applications. Sequencing of units is done in a natural order starting from Quantification and Numerical Applications, Algebraic Thinking, Mathematical Reasoning, Calculus, Probability, Descriptive Statistics, Financial Mathematics and Coordinate Geometry.

Each unit begins with a starting position and divided into a number of sections having discrete exercises. Efforts are done to develop concepts around meaningful applications to foster inquisitiveness in learners. Teachers are encouraged to extend/adapt these examples to initiate investigations and stimulating discourse in the classrooms.

It may be kept in mind that this should not be considered as a text book and teachers should avoid teaching the content as given in this book. It only gives some directions to approach various topics. Teachers are advised to use multiple examples from sources such as newspapers, magazines and other online resources to help students reconcile different approaches of problem solving and refining mathematical arguments.

We hope that this book will provide students a real sense of application of Mathematics in different spheres of work and life. It is an invitation to reinvent mathematics and how it can empower us to make more logical and informed decisions in lives.

We look forward to the suggestions from teachers, students and all learning community to make this book more realistic for Indian classrooms.





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