

Areas Related to Circles

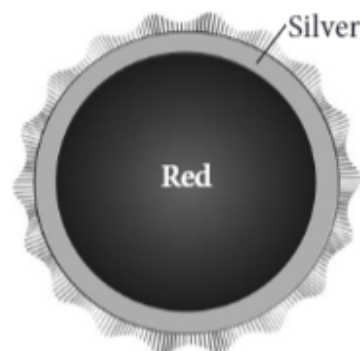
CASE STUDY / PASSAGE BASED QUESTIONS

1

Choosing Representative of the Students

Principle of a school decided to give badges to students who are chosen for the post of Head boy, Head girl, Prefect and Vice Prefect. Badges are circular in shape with two colour area, red and silver, as shown in figure. The diameter of the region representing red colour is 22 cm and silver colour is filled in 10.5 cm wide ring.

Based on the above information, answer the following questions.



- (i) The radius of circle representing the red region is
 (a) 9 cm (b) 10 cm (c) 11 cm (d) 12 cm
- (ii) Find the area of the red region.
 (a) 380.28 cm^2 (b) 382.28 cm^2 (c) 384.28 cm^2 (d) 378.28 cm^2
- (iii) Find the radius of the circle formed by combining the red and silver region.
 (a) 20.5 cm (b) 21.5 cm (c) 22.5 cm (d) 23.5 cm
- (iv) Find the area of the silver region.
 (a) 172.50 cm^2 (b) 1062.50 cm^2 (c) 1172.50 cm^2 (d) 1072.50 cm^2
- (v) Area of the circular path formed by two concentric circles of radii r_1 and r_2 ($r_1 > r_2$) =
 (a) $\pi(r_1^2 + r_2^2)$ sq. units (b) $\pi(r_1^2 - r_2^2)$ sq. units
 (c) $2\pi(r_1 - r_2)$ sq. units (d) $2\pi(r_1 + r_2)$ sq. units

2

Area of Button

While doing dusting a maid found a button whose upper face is of black colour, as shown in the figure. The diameter of each of the smaller identical circles is $\frac{1}{4}$ of the diameter of the larger circle whose radius is 16 cm.

Based on the above information, answer the following questions.



- (i) The area of each of the smaller circle is
 (a) 40.28 cm^2 (b) 46.39 cm^2 (c) 50.28 cm^2 (d) 52.3 cm^2

Syllabus

Motivate the area of a circle; area of sectors and segments of a circle. Problems based on areas and perimeter / circumference of the above said plane figures. (In calculating area of segment of a circle, problems should be restricted to central angle of 60° and 90° only. Plane figures involving triangles, simple quadrilaterals and circle should be taken.)

- (ii) The area of the larger circle is
 (a) 804.57 cm^2 (b) 704.57 cm^2 (c) 855.57 cm^2 (d) 990.57 cm^2
- (iii) The area of the black colour region is
 (a) 600.45 cm^2 (b) 603.45 cm^2 (c) 610.45 cm^2 (d) 623.45 cm^2
- (iv) The area of quadrant of a smaller circle is
 (a) 11.57 cm^2 (b) 13.68 cm^2 (c) 12 cm^2 (d) 12.57 cm^2
- (v) If two concentric circles are of radii 2 cm and 5 cm, then the area between them is
 (a) 60 cm^2 (b) 63 cm^2 (c) 66 cm^2 (d) 68 cm^2

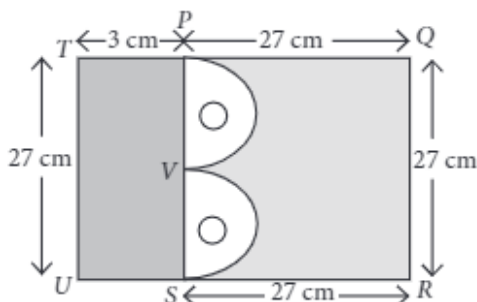
3

Layout of a House

Mr Ramanand purchased a plot $QRUT$ to build his house. He leave space of two congruent semicircles for gardening and a rectangular area of breadth 3 cm for car parking.

Based on the above information, answer the following questions.

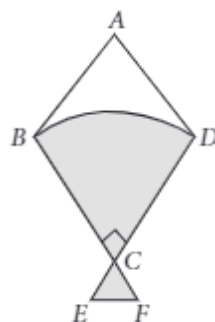
- (i) Area of square $PQRS$ is
 (a) 700 cm^2 (b) 729 cm^2 (c) 732 cm^2 (d) 735 cm^2
- (ii) Area of rectangle left for car parking is
 (a) 64 cm^2 (b) 76 cm^2 (c) 81 cm^2 (d) 100 cm^2
- (iii) Radius of semi-circle is
 (a) 6.75 cm (b) 7 cm (c) 7.75 cm (d) 8.75 cm
- (iv) Area of a semi-circle is
 (a) 61.59 cm^2 (b) 66.29 cm^2 (c) 70.36 cm^2 (d) 71.59 cm^2
- (v) Find the area of the shaded region.
 (a) 660.82 cm^2 (b) 666.82 cm^2 (c) 669.89 cm^2 (d) 700 cm^2



4

Kite Flying Competition

Makar Sankranti is a fun and delightful occasion. Like many other festivals, the kite flying competition also has a historical and cultural significance attached to it. The following figure shows a kite in which BCD is the shape of quadrant of a circle of radius 42 cm, $ABCD$ is a square and $\triangle CEF$ is an isosceles right angled triangle whose equal sides are 7 cm long.



Based on the above information, answer the following questions.

(i) Find the area of the square.

- (a) 1700 cm^2 (b) 1764 cm^2 (c) 1800 cm^2 (d) 1864 cm^2

(ii) Area of quadrant BCD is

- (a) 1290 cm^2 (b) 1380 cm^2 (c) 1386 cm^2 (d) 1390 cm^2

(iii) Find the area of $\triangle CEF$.

- (a) 24.5 cm^2 (b) 25 cm^2 (c) 25.5 cm^2 (d) 26 cm^2

(iv) Area of the shaded portion is

- (a) 1377 cm^2 (b) 1390 cm^2 (c) 1400 cm^2 (d) 1410.5 cm^2

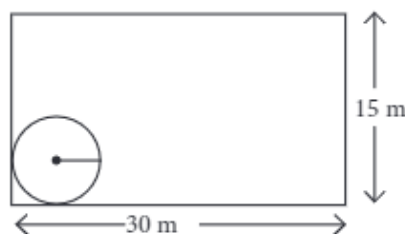
(v) Area of the unshaded portion is

- (a) 370 cm^2 (b) 378 cm^2 (c) 380 cm^2 (d) 384 cm^2

5

Rain Water Harvesting

A farmer has a rectangular field of length 30 m and breadth 15 m. By the farmer a pit of diameter 7 m is dug 12 m deep for rain water harvesting. The earth taken out is spread in the field.



Based on the above information, answer the following questions.

(i) Find the volume of the earth taken out.

- (a) 460 m^3 (b) 462 m^3 (c) 465 m^3 (d) 468 m^3

(ii) The area of the rectangular field is

- (a) 420 m^2 (b) 430 m^2 (c) 440 m^2 (d) 450 m^2

(iii) Find the area of the top of the pit.

- (a) 38.5 m^2 (b) 40.5 m^2 (c) 41.5 m^2 (d) None of these

(iv) The area of the remaining field is

- (a) 402.3 m^2 (b) 405 m^2 (c) 410 m^2 (d) 411.5 m^2

(v) Find the level rise in the field.

- (a) 0.5 m (b) 3 m (c) 1.12 m (d) 2.12 m

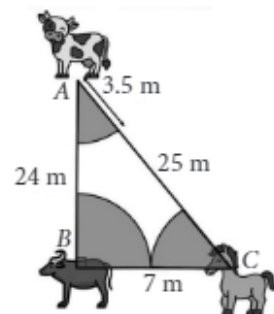
6

Grazing Management for Animals

Gayatri have a triangular shaped grass field. At the three corners of the field, a cow, a buffalo and a horse are tied separately to the pegs by means of ropes of 3.5 m each to graze in the field, as shown in the figure. Sides of the triangular field are 25 m, 24 m and 7 m. Based on the above information, answer the following questions.

(i) Area of triangular field is

- (a) 82 m^2 (b) 84 m^2 (c) 86 m^2 (d) 88 m^2



(ii) Area of the region grazed by the cow is

- (a) $\frac{\angle A}{360^\circ} \times \pi \times (3.5)^2$ (b) $\frac{\angle B}{360^\circ} \times \pi \times (24)^2$ (c) $\frac{\angle C}{360^\circ} \times \pi \times (3.5)^2$ (d) None of these

(iii) Area of region grazed by the buffalo and the horse is

- (a) $\frac{(\angle A + \angle C)}{360^\circ} \times \pi \times (5.5)^2$ (b) $\frac{(\angle B + \angle C)}{360^\circ} \times \pi \times (5.6)^2$
(c) $\frac{(\angle A + \angle C)}{360^\circ} \times \pi \times (3.5)^2$ (d) $\frac{(\angle B + \angle C)}{360^\circ} \times \pi \times (3.5)^2$

(iv) Total area grazed by the cow, the buffalo and the horse is

- (a) 16.25 m² (b) 17.3 m² (c) 18.25 m² (d) 19.25 m²

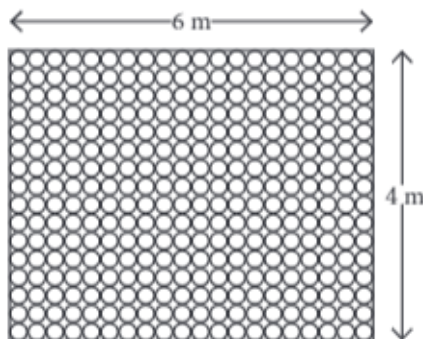
(v) Find the area of the field that cannot be grazed.

- (a) 60.75 m² (b) 64.75 m² (c) 68 m² (d) 69.75 m²

7

Design of a Floor

Shweta wants to change the design of the floor of her living room which is of dimensions 6 m × 4 m and it is covered with circular tiles of diameters 50 cm each, as shown in the figure.



Based on the above information, answer the following questions.

(i) Number of circular tiles along length of room is

- (a) 11 (b) 12 (c) 13 (d) 14

(ii) Total number of circular tiles equals to

- (a) 90 (b) 92 (c) 94 (d) 96

(iii) Area covered by each circular tile is

- (a) 1954.28 cm² (b) 1960.08 cm² (c) 1964.28 cm² (d) 1980 cm²

(iv) Area of rectangular floor is

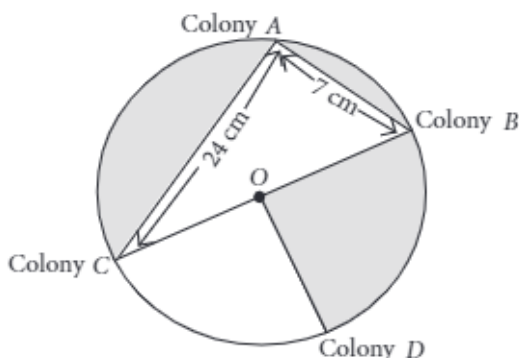
- (a) 240000 cm² (b) 204000 cm² (c) 420000 cm² (d) None of these

(v) Find the area of the floor that remains uncovered with tiles.

- (a) 3.6 m² (b) 4.6 m² (c) 5 m² (d) 5.142 m²

Identifying Polluted Region

To find the polluted region in different areas of Dwarka (a part of Delhi represented by the circle given below) a survey was conducted by the students of class X. It was found that the shaded region is the polluted region, where O is the centre of the circle.



Based on the above information, answer the following questions.

(i) Find the radius of the circle.

- (a) 12.5 cm (b) 13.5 cm (c) 15 cm (d) 16.5 cm

(ii) Find the area of the circle.

- (a) 481.7 cm^2 (b) 490 cm^2 (c) 491.07 cm^2 (d) 495.6 cm^2

(iii) If D lies at the middle of arc BC , then area of region COD is

- (a) 121 cm^2 (b) 122.76 cm^2 (c) 126 cm^2 (d) 129.8 cm^2

(iv) Area of the $\triangle BAC$ is

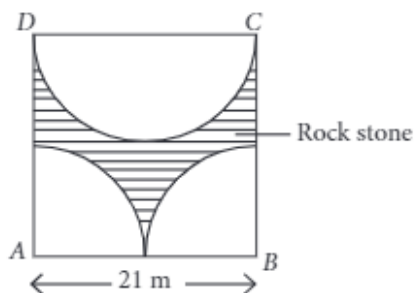
- (a) 77 cm^2 (b) 79 cm^2 (c) 81 cm^2 (d) 84 cm^2

(v) Find the area of the polluted region.

- (a) 280.31 cm^2 (b) 284.31 cm^2 (c) 285.31 cm^2 (d) 240.31 cm^2

Construction with Virtue

A builder of residential project have a vacant square land of side 21 m. He wants to make a temple in the shape of semi-circle and a park in the shape of two quadrants of a circle as shown in the figure.

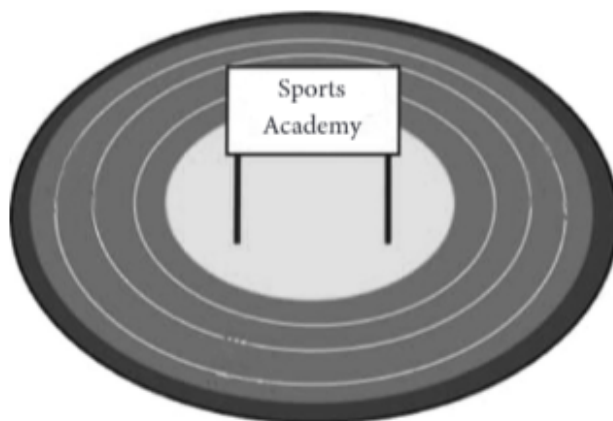


Based on the above information, answer the following questions.

- (i) Find the area of square.
 (a) 436 m^2 (b) 438 m^2 (c) 441 m^2 (d) 444 m^2
- (ii) Area of two quadrants, shown in figure, is
 (a) 170.25 m^2 (b) 173.25 m^2 (c) 175 m^2 (d) 178.25 m^2
- (iii) Find the area of semi-circular temple.
 (a) 163.25 m^2 (b) 168.25 m^2 (c) 173.25 m^2 (d) 178.25 m^2
- (iv) Find the area of unshaded region.
 (a) 340.5 m^2 (b) 346.5 m^2 (c) 350.5 m^2 (d) 355.65 m^2
- (v) Find the area of shaded region.
 (a) 88.5 m^2 (b) 90.5 m^2 (c) 92.5 m^2 (d) 94.5 m^2

Race Competition

There is a race competition between all students of a sports academy, so that the sports committee can choose better students for a marathon. The race track in the academy is in the form of a ring whose inner most circumference is 264 m and the outer most circumference is 308 m.

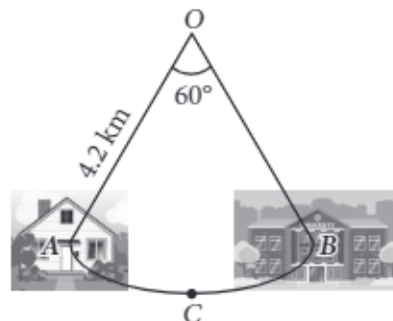


Based on the above information, answer the following questions.

- (i) Find the radius of the outer most circle.
 (a) 48 m (b) 49 m (c) 50 m (d) 51 m
- (ii) Find the radius of the inner most circle.
 (a) 38 m (b) 40 m (c) 42 m (d) 44 m
- (iii) Find the width of the track.
 (a) 7 m (b) 8 m (c) 9 m (d) 10 m
- (iv) Find the area of the race track.
 (a) 2010 m^2 (b) 2006 m^2 (c) 2000 m^2 (d) 2002 m^2
- (v) If the cost of painting on the race track is ₹ 6 per m^2 , then find the total cost for painting the whole race track.
 (a) ₹ 12000 (b) ₹ 12012 (c) ₹ 12550 (d) ₹ 12850

Analysing Distance and Expense

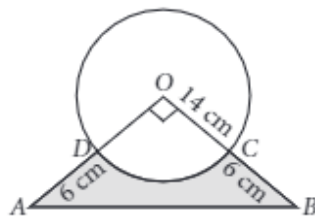
Kartik has his home located at A and his college located at B . Kartik drives his motorbike three days in a week and rides his bicycle in the remaining 3 days, to go to his college and back to home. AOB is a sector of a circle with centre O , central angle 60° and radius 4.2 km. Path AOB is the route for driving by motorbike and path ACB is for bicycle only.



- (i) Find the total distance travelled by Kartik through the motorbike in a week to go to college.
 - (a) 50.4 km
 - (b) 55 km
 - (c) 56.4 km
 - (d) 58 km
- (ii) Find the total distance travelled by Kartik through the bicycle in a week to go to college.
 - (a) 24.4 km
 - (b) 26.4 km
 - (c) 28 km
 - (d) 29.4 km
- (iii) Find the area of sector AOB .
 - (a) 7.88 km^2
 - (b) 8.24 km^2
 - (c) 9.24 km^2
 - (d) 10.14 km^2
- (iv) If the cost of fuel for the motorbike is ₹ 20 per km, then find the total cost of fuel used in a week in going college.
 - (a) ₹ 1008
 - (b) ₹ 1120
 - (c) ₹ 1200
 - (d) ₹ 1240
- (v) If the angle of sector changed from 60° to 90° , then find the total length of the available paths.
 - (a) 12 km
 - (b) 13 km
 - (c) 14 km
 - (d) 15 km

Prize Distribution

Director of a company select a round glass trophy for awarding their employees on annual function. Design of each trophy is made as shown in the figure, where its base $ABCD$ is golden plated from the front side at the rate of ₹ 6 per cm^2 .



- (i) Find the area of sector $ODCO$.
 - (a) 154 cm^2
 - (b) 155 cm^2
 - (c) 156 cm^2
 - (d) 157 cm^2
- (ii) Find the area of $\triangle AOB$.
 - (a) 150 cm^2
 - (b) 200 cm^2
 - (c) 250 cm^2
 - (d) 300 cm^2
- (iii) Find the total cost of golden plating.
 - (a) ₹ 276
 - (b) ₹ 280
 - (c) ₹ 284
 - (d) ₹ 200

(iv) Find the area of major sector formed in the given figure.

- (a) 400 cm^2 (b) 450 cm^2 (c) 462 cm^2 (d) 472 cm^2

(v) Find the length of arc DC .

- (a) 16 cm (b) 18 cm (c) 20 cm (d) 22 cm

13

Pendulum Clock

Kritika bought a pendulum clock for her living room. The clock contains a small pendulum of length 15 cm. The minute hand and hour hand of the clock are 9 cm and 6 cm long respectively.

Based on the above information, answer the following questions.



(i) Find the area swept by the minute hand in 10 minutes.

- (a) 24.24 cm^2 (b) 42.42 cm^2
(c) 44 cm^2 (d) 44.42 cm^2

(ii) If the pendulum covers a distance of 22 cm in one complete oscillation, then find the angle described by pendulum at the centre.

- (a) 40° (b) 42° (c) 45° (d) 48°

(iii) Find the angle described by hour hand in 10 minutes.

- (a) 5° (b) 10° (c) 15° (d) 20°

(iv) Find the area swept by the hour hand in 1 hour.

- (a) 7.68 cm^2 (b) 8.2 cm^2 (c) 8.86 cm^2 (d) 9.428 cm^2

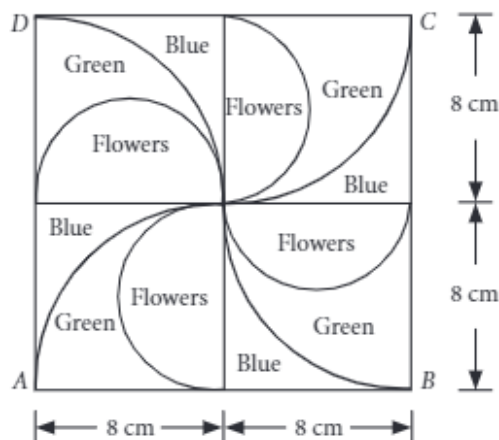
(v) Find the area swept by the hour hand between 11 a.m. and 5 p.m.

- (a) 56.568 cm^2 (b) 62 cm^2 (c) 70 cm^2 (d) 72 cm^2

14

Creating a Painting

Shiva made a painting on a square chart paper $ABCD$. The painting is made up of squares, semicircular arcs (painted with flowers) and arcs of quadrant of circles as shown below. He painted the same type of regions with same colours.



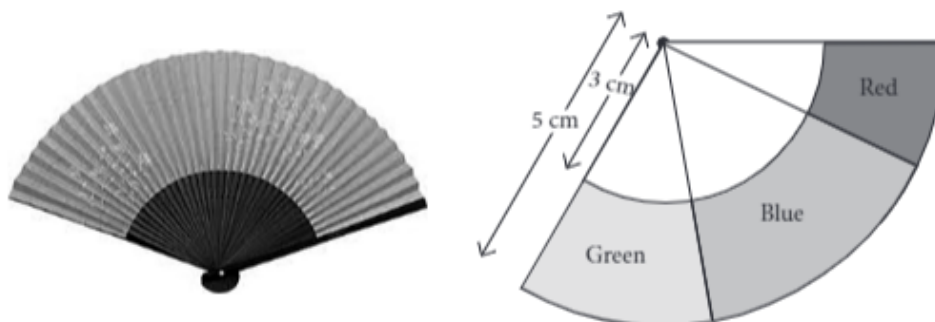
Based on the above information, answer the following questions.

- (i) Find the total area of the region which is painted with flowers.
 (a) 90.8 cm^2 (b) 100.57 cm^2 (c) 105.6 cm^2 (d) 111.20 cm^2
- (ii) Find the area of all the quadrants given in the figure.
 (a) 190 cm^2 (b) 198.14 cm^2 (c) 201.14 cm^2 (d) 222.14 cm^2
- (iii) Find the area of the region which is painted green
 (a) 100.57 cm^2 (b) 111.57 cm^2 (c) 120 cm^2 (d) 128.57 cm^2
- (iv) Find the area of the region which is painted blue.
 (a) 46.86 cm^2 (b) 48 cm^2 (c) 50.86 cm^2 (d) 54.86 cm^2
- (v) Find the total length of the boundary of the region which is painted green.
 (a) 128.57 cm (b) 132.56 cm (c) 145.57 cm (d) 150 cm

15

Japanese Folding Fan

Sara hold a japanese folding fan in her hand as shown in the figure. It is shaped like a sector of a circle and made of a thin material such as paper or feather. The inner and outer radii are 3 cm and 5 cm respectively. The fan has three colours *i.e.*, red, blue and green.



Based on the above information, answer the following questions.

- (i) If the region containing blue colour makes an angle of 80° at the centre, then find the area of the region having blue colour.
 (a) 9.17 cm^2 (b) 10.1 cm^2 (c) 11.17 cm^2 (d) 13.17 cm^2
- (ii) If the region containing green colour makes an angle of 60° at the centre, then find the area of the region having green colour.
 (a) 6.2 cm^2 (b) 8.38 cm^2 (c) 9.9 cm^2 (d) 11.12 cm^2
- (iii) If the region containing red colour makes an angle of 20° at the centre, then find the perimeter of the region containing red colour.
 (a) 2.9 cm (b) 4.2 cm (c) 5.4 cm (d) 6.79 cm
- (iv) Find the area of the region having radius 3 cm.
 (a) 12.57 cm^2 (b) 14.8 cm^2 (c) 20 cm^2 (d) 26.57 cm^2
- (v) The region given in the figure represents
 (a) minor sector (b) major sector (c) minor segment (d) major segment

HINTS & EXPLANATIONS

1. (i) (c): Radius of circle representing red region
 $= \frac{22}{2} = 11 \text{ cm}$ [$\because$ Diameter = 22 cm (Given)]

(ii) (a): Area of red region $= \pi r^2$
 $= \frac{22}{7} \times 11 \times 11 = 380.28 \text{ cm}^2$

(iii) (b): Radius of circle formed by combining red and silver region = Radius of red region
 + width of silver sign
 $= (11 + 10.5) \text{ cm} = 21.5 \text{ cm}$

(iv) (d): Area of silver region
 $= \text{Area of combined region} - \text{Area of red region}$
 $= \frac{22}{7} \times 21.5 \times 21.5 - 380.28$
 $= 1452.78 - 380.28 = 1072.50 \text{ cm}^2$

(v) (b): Area of circular path formed by two concentric circles $= \pi(r_1^2 - r_2^2)$ sq. units

2. Let r and R be the radii of each smaller circle and larger circle respectively.

We have, $d = \frac{1}{4}D$

$\Rightarrow r = \frac{1}{4}R \Rightarrow r = \frac{1}{4} \times 16 \Rightarrow r = 4 \text{ cm}$

(i) (c): Area of smaller circle $= \pi r^2$
 $= \frac{22}{7} \times 4 \times 4 = 50.28 \text{ cm}^2$

(ii) (a): Area of larger circle $= \pi R^2$
 $= \frac{22}{7} \times 16 \times 16 = \frac{5632}{7} = 804.57 \text{ cm}^2$

(iii) (b): Area of the black colour region = Area of larger circle - Area of 4 smaller circles
 $= 804.57 - 4 \times 50.28 = 603.45 \text{ cm}^2$

(iv) (d): Area of quadrant of a smaller circle
 $= \frac{1}{4} \times 50.28 = 12.57 \text{ cm}^2$

(v) (c): Area between two concentric circles
 $= \pi(R^2 - r^2) = \frac{22}{7}(5^2 - 2^2)$
 $= \frac{22}{7}(25 - 4) = \frac{22}{7} \times 21 = 66 \text{ cm}^2$

3. (i) (b): Side of square PQRS = 27 cm
 $\therefore$ Area of square PQRS $= 27 \times 27 = 729 \text{ cm}^2$

(ii) (c): Area of rectangle left for car parking is area of region PSUT $= 27 \times 3 = 81 \text{ cm}^2$

(iii) (a): Diameter of semi-circle $= PV = \frac{PS}{2} = \frac{27}{2}$
 $= 13.5 \text{ cm}$

$\therefore$ Radius of semi-circle $= \frac{13.5}{2} = 6.75 \text{ cm}$

(iv) (d): Area of a semi-circle $= \frac{1}{2} \pi r^2$
 $= \frac{1}{2} \times \frac{22}{7} \times 6.75 \times 6.75 = 71.59 \text{ cm}^2$

(v) (b): Area of shaded region = area of rectangular plot QRUT - area of two semi-circles
 $= 30 \times 27 - 2 \times 71.59 = 666.82 \text{ cm}^2$

4. (i) (b): Area of square ABCD $= 42 \times 42$
 $= 1764 \text{ cm}^2$

(ii) (c): Area of quadrant BCD
 $= \frac{1}{4} \times \frac{22}{7} \times 42 \times 42 = 1386 \text{ cm}^2$

(iii) (a): Area of $\triangle CEF = \frac{1}{2} \times CE \times CF$
 $= \frac{1}{2} \times 7 \times 7 = 24.5 \text{ cm}^2$

(iv) (d): Area of shaded region = Area of quadrant BCD
 + Area of $\triangle CEF$
 $= 1386 + 24.5 = 1410.5 \text{ cm}^2$

(v) (b): Area of the unshaded region = Area of square ABCD - Area of quadrant BCD
 $= 1764 - 1386 = 378 \text{ cm}^2$

5. (i) (b): Volume of the earth taken out

$= \pi \left(\frac{7}{2} \right)^2 \times 12 = \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times 12 = 462 \text{ m}^3$

(ii) (d): Area of the rectangular field
 $= 30 \times 15 = 450 \text{ m}^2$

(iii) (a): Area of top of the pit $= \pi \left(\frac{7}{2} \right)^2 = \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2}$
 $= \frac{77}{2} = 38.5 \text{ m}^2$

(iv) (d): Area of the remaining field = Area of rectangular field - area of top of pit
 $= 450 - 38.5 = 411.5 \text{ m}^2$

$$(v) (c): \text{The rise in the level of field} = \frac{462}{411.5} = 1.12 \text{ m}$$

6. (i) (b): Since $\triangle ABC$ is a right angled triangle.

$$\therefore \text{Area of triangle } ABC = \frac{1}{2} \times 7 \times 24 = 84 \text{ m}^2$$

(ii) (a): Area of region grazed by the cow

$$= \frac{\angle A}{360^\circ} \times \pi \times (3.5)^2$$

(iii) (d): Area of the region grazed by the buffalo and

$$\text{the horse} = \frac{\angle B}{360^\circ} \times \pi \times (3.5)^2 + \frac{\angle C}{360^\circ} \times \pi \times (3.5)^2$$

$$= \frac{(\angle B + \angle C)}{360^\circ} \times \pi \times (3.5)^2$$

(iv) (d): Total area grazed by the cow, the horse and the

$$\text{buffalo} = \frac{\angle A}{360^\circ} \times \pi \times (3.5)^2 + \frac{(\angle B + \angle C)}{360^\circ} \times \pi \times (3.5)^2$$

$$= \frac{(\angle A + \angle B + \angle C)}{360^\circ} \times \pi \times (3.5)^2$$

$$= \frac{22}{7} \times \frac{180^\circ}{360^\circ} \times 3.5 \times 3.5$$

($\because$ sum of interior angles of a triangle is 180°)

$$= \frac{77}{4} = 19.25 \text{ m}^2$$

(v) (b): Area of the field that cannot be grazed

$$= \text{Area of } \triangle ABC - \text{Area of region grazed by all the three animals}$$

$$= 84 - 19.25 = 64.75 \text{ m}^2$$

7. (i) (b): Number of circular tiles along length of

$$\text{room} = \frac{600}{50} = 12$$

(ii) (d): Number of circular tiles along breadth of

$$\text{room} = \frac{400}{50} = 8$$

$$\therefore \text{Total number of circular tiles} = 12 \times 8 = 96$$

(iii) (c): Area covered by each circular tile = $\pi(25)^2$

$$= \frac{22}{7} \times 25 \times 25 = 1964.28 \text{ cm}^2$$

(iv) (a): Area of rectangular floor = 600×400

$$= 240000 \text{ cm}^2$$

(v) (d): Area of the floor that remains uncovered with tiles = Area of rectangular floor

– Area of 96 circular tiles

$$= 240000 - 96 \times 1964.28$$

$$= 51429.12 \text{ cm}^2 = 5.142 \text{ m}^2$$

8. (i) (a): Since BOC is the diameter and $\angle BAC = 90^\circ$

$$\therefore BC^2 = AB^2 + AC^2$$

$$= 7^2 + 24^2 = 625$$

$$\Rightarrow BC = 25 \text{ cm}$$

$$\therefore \text{Radius of circle} = \frac{25}{2} \text{ cm} = 12.5 \text{ cm}$$

$$(ii) (c): \text{Area of circle} = \pi(12.5)^2 = \frac{22}{7} \times 12.5 \times 12.5$$

$$= 491.07 \text{ cm}^2$$

(iii) (b): Clearly, $\angle COD = 90^\circ$

[$\because \angle COB = 180^\circ$ and equal arcs subtends equal angles at the centre]

$$\text{Area of region } COD = \frac{90^\circ}{360^\circ} \times \pi r^2$$

$$= \frac{1}{4} (491.07) = 122.76 \text{ cm}^2$$

$$(iv) (d): \text{Area of } \triangle BAC = \frac{1}{2} \times AB \times AC$$

$$= \frac{1}{2} \times 7 \times 24 = 84 \text{ cm}^2$$

(v) (b): Area of the polluted region = Area of circle

– Area of sector COD – Area of $\triangle ABC$

$$= 491.07 - 122.76 - 84$$

$$= 284.31 \text{ cm}^2$$

9. (i) (c): Area of square $ABCD = 21 \times 21 = 441 \text{ m}^2$

(ii) (b): Area of two quadrants = $2 \left(\pi r^2 \times \frac{90^\circ}{360^\circ} \right)$

$$= \frac{22}{7} \times \frac{21}{2} \times \frac{21}{2} \times \frac{1}{2} = 173.25 \text{ m}^2$$

(iii) (c): Area of semi-circular temple = $\frac{1}{2} (\pi r^2)$

$$= \frac{1}{2} \times \frac{22}{7} \times \frac{21}{2} \times \frac{21}{2} = 173.25 \text{ m}^2$$

(iv) (b): Area of unshaded region = Area of semi-circle

+ Area of two quadrants

$$= 173.25 + 173.25 = 346.5 \text{ m}^2$$

(v) (d): Area of shaded region = Area of square

– (Area of two quadrants + Area of semi-circle)

$$= 441 - 346.5 = 94.5 \text{ m}^2$$

10. (i) (b): Let the radius of outer most circle be R .

Outer most circumference = 308 m [Given]

$$\Rightarrow 2\pi R = 308 \Rightarrow 2 \times \frac{22}{7} \times R = 308$$

$$\Rightarrow R = \frac{308 \times 7}{2 \times 22} = 49 \text{ m}$$

(ii) (c) : Let the radius of inner most circle be r
 Inner most circumference = 264 m [Given]
 $\Rightarrow 2\pi r = 264$
 $\Rightarrow 2 \times \frac{22}{7} \times r = 264 \Rightarrow r = \frac{264 \times 7}{2 \times 22} = 42 \text{ m}$

(iii) (a) : Width of the track = Radius of outer most track
 - Radius of inner most track = $49 - 42 = 7 \text{ m}$

(iv) (d) : Area of the race track = Area of outer circle
 - Area of inner circle
 $= \pi(R^2 - r^2) = \pi[(49)^2 - (42)^2]$
 $= \frac{22}{7}[2401 - 1764] = 2002 \text{ m}^2$

(v) (b) : Cost of painting the whole race track
 $= ₹ (6 \times 2002) = ₹ 12012.$

11. (i) (a) : In a week, Kartik drives his motorbike 3 days to go to college

$\therefore$ Total distance travelled by Kartik through motorbike = $2 \times 4.2 \times 6 = 50.4 \text{ km}$

(ii) (b) : In a week Kartik rides his bicycle 3 days to go to college.

$\therefore$ Total distance travelled by Kartik through bicycle
 $= \text{Length of arc } \widehat{ACB} \times 6$
 $= \frac{\theta}{360^\circ} \times 2\pi r \times 6 = \frac{60^\circ}{360^\circ} \times 2 \times \frac{22}{7} \times 4.2 \times 6 = 26.4 \text{ km}$

(iii) (c) : Area of sector $AOB = \frac{\theta}{360^\circ} \times \pi r^2$
 $= \frac{60^\circ}{360^\circ} \times \frac{22}{7} \times (4.2)^2 = 9.24 \text{ km}^2$

(iv) (a) : Total cost of fuel used for a week
 $= ₹ (20 \times 50.4) = ₹ 1008$

(v) (d) : Total length of available paths
 $= 4.2 + 4.2 + \frac{\theta}{360^\circ} \times 2\pi r$
 $= 8.4 + \frac{90^\circ}{360^\circ} \times 2 \times \frac{22}{7} \times 4.2 = 8.4 + 6.6 = 15 \text{ km}$

12. (i) (a) : Area of sector $ODCO = \frac{1}{4} \pi r^2$
 $= \frac{1}{4} \times \frac{22}{7} \times 14 \times 14 = 154 \text{ cm}^2$

(ii) (b) : Area of $\triangle AOB = \frac{1}{2} \times OA \times OB = \frac{1}{2} (20 \times 20)$
 $= 200 \text{ cm}^2$

(iii) (a) : Area of region which is golden plated
 $= \text{area of } \triangle OAB - \text{area of sector } ODCO$
 $= 200 - 154 = 46 \text{ cm}^2$
 $\therefore$ Total cost of golden plating = $₹ (6 \times 46) = ₹ 276$

(iv) (c) : Area of major sector = area of circle
 - area of minor sector
 $= \pi r^2 - \frac{1}{4} \pi r^2 = \frac{3\pi r^2}{4} = \frac{3}{4} \times \frac{22}{7} \times 14 \times 14 = 462 \text{ cm}^2$

(v) (d) : Length of arc $DC = \frac{90^\circ}{360^\circ} \times 2 \times \frac{22}{7} \times 14$
 $= 22 \text{ cm}$

13. (i) (b) : Angle made by minute hand in 60 minutes
 $= 360^\circ$

$\therefore$ Angle made by minute hand in 10 minutes
 $= \frac{360^\circ}{60} \times 10 = 60^\circ$

Length of minute hand = 9 cm

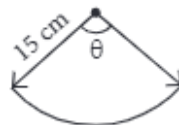
$\therefore$ Area swept by minute hand in 10 minutes
 $= \text{Area of sector having central angle } 60^\circ$

$= \pi r^2 \left(\frac{60^\circ}{360^\circ} \right) = \frac{22}{7} \times 9 \times 9 \times \frac{1}{6}$
 $= \frac{297}{7} = 42.42 \text{ cm}^2$

(ii) (b) : We have, $r = 15 \text{ cm}$
 and $l = \frac{1}{2} (22) = 11 \text{ cm}$

We know that $l = 2\pi r \left(\frac{\theta}{360^\circ} \right)$

$\Rightarrow \theta = \frac{11 \times 360^\circ}{2 \times \frac{22}{7} \times 15} = \frac{90^\circ \times 7}{15} = 6^\circ \times 7 = 42^\circ$



(iii) (a) : Angle made by hour hand in 12 hours = 360°
 $\therefore$ Angle made by hour hand in 10 minutes
 $= \left(\frac{360^\circ}{12} \times \frac{1}{6} \right) = 5^\circ$

(iv) (d) : Angle made by hour hand in 1 hour
 $= \frac{360^\circ}{12} = 30^\circ$

Also, $r = 6 \text{ cm}$

$\therefore$ Area swept by hour hand in 1 hour
 $= \text{Area of sector having central angle } 30^\circ$
 $= \pi r^2 \times \left(\frac{30^\circ}{360^\circ} \right) = \frac{22}{7} \times 6 \times 6 \times \frac{1}{12} = \frac{66}{7} = 9.428 \text{ cm}^2$

(v) (a) : Number of hours from 11 a.m. to 5 p.m. = 6
 Area swept by hour hand in 1 hour = 9.428 cm^2
 $\therefore$ Area swept by hour hand in 6 hours = 9.428×6
 $= 56.568 \text{ cm}^2$

14. (i) (b) : Region which is painted with flowers are 4 semi-circles of diameter 8 cm, i.e., 2 circles of radius 4 cm each.

$$\therefore \text{Total area of region which is painted with flowers} \\ = 2 \times \pi r^2 = 2 \times \frac{22}{7} \times 4 \times 4 = 100.57 \text{ cm}^2$$

(ii) (c) : In the figure, we have 4-quadrants of radius 8 cm

$$\therefore \text{Area of all quadrants} = 4 \times \frac{1}{4} \pi r^2 = \pi r^2 \\ = \frac{22}{7} \times 8 \times 8 = 201.14 \text{ cm}^2$$

(iii) (a) : Area of region which is painted green
= area of all quadrants – total area of region which are painted with flowers
 $= 201.14 - 100.57 = 100.57 \text{ cm}^2$

(iv) (d) : Area of region which is painted blue
= Area of whole chart paper – area of all quadrants
 $= 16 \times 16 - 201.14 = 256 - 201.14 = 54.86 \text{ cm}^2$

(v) (b) : Total length of boundary of region which is painted green = 4 [circumference of semi-circle of radius 4 cm each + length of arc of quadrant of radius 8 cm + radius of quadrant]

$$= 4 \left[\frac{1}{2} \times 2\pi(4) + \frac{1}{4} \times 2 \times \pi \times 8 + 8 \right] \\ = 4 \left[4\pi + 4\pi + 8 \right] = 4(8\pi + 8) = 4 \left(8 \times \frac{22}{7} + 8 \right) \\ = 4(33.14) = 132.56 \text{ cm}$$

15. (i) (c) : Area of the region containing blue colour
 $= \frac{22}{7} \times 5 \times 5 \times \frac{80^\circ}{360^\circ} - \frac{22}{7} \times 3 \times 3 \times \frac{80^\circ}{360^\circ}$

$$= \frac{22}{7} \times \frac{2}{9} \times [25 - 9] = \frac{44}{63} (16) = 11.17 \text{ cm}^2$$

(ii) (b) : Area of the region containing green colour

$$= \frac{22}{7} \times \frac{60^\circ}{360^\circ} [5 \times 5 - 3 \times 3] = \frac{22}{7} \times \frac{1}{6} \times 16 = 8.38 \text{ cm}^2$$

(iii) (d) : Perimeter of the region containing red colour
= 2 + 2 + length of arc of sector having radius 3 cm + length of arc of sector having radius 5 cm

$$= 4 + 2 \times \frac{22}{7} \times 3 \times \frac{20^\circ}{360^\circ} + 2 \times \frac{22}{7} \times 5 \times \frac{20^\circ}{360^\circ} \\ = 4 + \frac{44}{7} \times \frac{1}{18} \times 8 = 4 + \frac{176}{63} = 4 + 2.79 = 6.79 \text{ cm}$$

$$\text{(iv) (a) : Required area} = \frac{22}{7} \times 3 \times 3 \times \frac{160^\circ}{360^\circ} \\ = \frac{88}{7} = 12.57 \text{ cm}^2$$

(v) (a) : Angle of given sector = $80^\circ + 60^\circ + 20^\circ = 160^\circ$
Thus, the given region represents minor sector of a circle.