# **Mathematics**

# (Chapter – 6) (Linear Inequalities) (Class – XI)

# Exercise 6.1

# **Question 1:**

Solve 24x < 100, when (i) x is a natural number

(ii) x is an integer

# Answer 1:

The given inequality is 24x < 100.

24x < 100

$$\Rightarrow \frac{24x}{24} < \frac{100}{24}$$
 [Dividing both sides by same positive number]  
$$\Rightarrow x < \frac{25}{6}$$

(i) It is evident that 1, 2, 3, and 4 are the only natural numbers less than  $\frac{25}{6}$  Thus,

when x is a natural number, the solutions of the given inequality are 1, 2, 3, and 4. Hence, in this case, the solution set is  $\{1, 2, 3, 4\}$ .

(ii) The integers less than  $\frac{25}{6}$  are ...-3, -2, -1, 0, 1, 2, 3, 4.

# Thus,

when x is an integer, the solutions of the given inequality are  $\dots -3$ , -2, -1, 0, 1, 2, 3, 4. Hence, in this case, the solution set is  $\{\dots -3, -2, -1, 0, 1, 2, 3, 4\}$ .

# **Question 2:**

Solve -12x > 30, when (i) x is a natural number (ii)

(ii) x is an integer

# Answer 2:

The given inequality is -12x > 30.

-12x > 30

$$\Rightarrow \frac{-12x}{-12} < \frac{30}{-12} \qquad \text{[Dividing both sides by same negative number]}\\ \Rightarrow x < -\frac{5}{2}$$

(i) There is no natural number less than  $\left(-\frac{5}{2}\right)$ .



Thus, when x is a natural number, there is no solution of the given inequality.

(ii) The integers less than  $\left(-\frac{5}{2}\right)$  are ..., -5, -4, -3.

Thus, when x is an integer, the solutions of the given inequality are  $\dots$ , -5, -4, -3. Hence, in this case, the solution set is  $\{\dots, -5, -4, -3\}$ .

# **Question 3:**

Solve 5x - 3 < 7, when

(i) x is an integer

(ii) x is a real number

# Answer 3:

The given inequality is 5x - 3 < 7. 5x - 3 < 7 $\Rightarrow$  5x-3+3<7+3  $\Rightarrow 5x < 10$  $\Rightarrow \frac{5x}{5} < \frac{10}{5}$  $\Rightarrow x < 2$ 

(i) The integers less than 2 are ..., -4, -3, -2, -1, 0, 1.

Thus, when x is an integer, the solutions of the given inequality are ...,

-4, -3, -2, -1, 0, 1.

Hence, in this case, the solution set is  $\{\dots, -4, -3, -2, -1, 0, 1\}$ .

(ii) When x is a real number, the solutions of the given inequality are given by x < 2, that is, all real numbers *x* which are less than 2.

Thus, the solution set of the given inequality is  $x \in (-\infty, 2)$ .

# **Question 4:**

Solve 3x + 8 > 2, when (i) x is an integer

(ii) x is a real number

### Answer 4:

The given inequality is 3x + 8 > 2.



3x+8>2  $\Rightarrow 3x+8-8>2-8$   $\Rightarrow 3x>-6$   $\Rightarrow \frac{3x}{3} > \frac{-6}{3}$  $\Rightarrow x > -2$ 

(i) The integers greater than -2 are -1, 0, 1, 2, ...

Thus, when x is an integer, the solutions of the given inequality are -1, 0, 1, 2 ...

Hence, in this case, the solution set is  $\{-1, 0, 1, 2, ...\}$ .

(ii) When x is a real number, the solutions of the given inequality are all the real numbers, which are greater than -2.

Thus, in this case, the solution set is  $(-2, \infty)$ .

### **Question 5:**

Solve the given inequality for real *x*: 4x + 3 < 5x + 7

#### Answer 5:

4x + 3 < 5x + 7  $\Rightarrow 4x + 3 - 7 < 5x + 7 - 7$   $\Rightarrow 4x - 4 < 5x$   $\Rightarrow 4x - 4 - 4x < 5x - 4x$  $\Rightarrow -4 < x$ 

Thus, all real numbers x, which are greater than -4, are the solutions of the given inequality.

Hence, the solution set of the given inequality is  $(-4, \infty)$ .

### **Question 6:**

Solve the given inequality for real *x*: 3x - 7 > 5x - 1

### Answer 6:

3x - 7 > 5x - 1  $\Rightarrow 3x - 7 + 7 > 5x - 1 + 7$   $\Rightarrow 3x > 5x + 6$   $\Rightarrow 3x - 5x > 5x + 6 - 5x$  $\Rightarrow - 2x > 6$ 



$$\Rightarrow \frac{-2x}{-2} < \frac{6}{-2}$$
$$\Rightarrow x < -3$$

Thus, all real numbers x, which are less than -3, are the solutions of the given inequality. Hence, the solution set of the given inequality is  $(-\infty, -3)$ .

### **Question 7:**

Solve the given inequality for real x:  $3(x - 1) \le 2(x - 3)$ 

### Answer 7:

 $3(x - 1) \le 2(x - 3)$   $\Rightarrow 3x - 3 \le 2x - 6$   $\Rightarrow 3x - 3 + 3 \le 2x - 6 + 3$   $\Rightarrow 3x \le 2x - 3$   $\Rightarrow 3x - 2x \le 2x - 3 - 2x$  $\Rightarrow x \le - 3$ 

Thus, all real numbers x, which are less than or equal to -3, are the solutions of the given inequality.

Hence, the solution set of the given inequality is  $(-\infty, -3]$ .

### **Question 8:**

Solve the given inequality for real  $x: 3(2 - x) \ge 2(1 - x)$ 

# Answer 8:

```
3(2 - x) \ge 2(1 - x)

\Rightarrow 6 - 3x \ge 2 - 2x

\Rightarrow 6 - 3x + 2x \ge 2 - 2x + 2x

\Rightarrow 6 - x \ge 2

\Rightarrow 6 - x - 6 \ge 2 - 6

\Rightarrow -x \ge -4

\Rightarrow x \le 4
```

Thus, all real numbers x, which are less than or equal to 4, are the solutions of the given inequality.

Hence, the solution set of the given inequality is  $(-\infty, 4]$ .



# **Question 9:**

Solve the given inequality for real *x*:

$$x + \frac{x}{2} + \frac{x}{3} < 11$$

### Answer 9:

$$x + \frac{x}{2} + \frac{x}{3} < 11$$

$$\Rightarrow x \left( 1 + \frac{1}{2} + \frac{1}{3} \right) < 11$$

$$\Rightarrow x \left( \frac{6 + 3 + 2}{6} \right) < 11$$

$$\Rightarrow \frac{11x}{6} < 11$$

$$\Rightarrow \frac{11x}{6} < 11$$

$$\Rightarrow \frac{11x}{6 \times 11} < \frac{11}{11}$$

$$\Rightarrow \frac{x}{6} < 1$$

$$\Rightarrow x < 6$$

Thus, all real numbers x, which are less than 6, are the solutions of the given inequality. Hence, the solution set of the given inequality is  $(-\infty, 6)$ .

### **Question 10:**

Solve the given inequality for real x:  $\frac{x}{3} > \frac{x}{2} + 1$ 

# Answer 10:

$$\frac{x}{3} > \frac{x}{2} + 1$$
$$\Rightarrow \frac{x}{3} - \frac{x}{2} > 1$$
$$\Rightarrow \frac{2x - 3x}{6} > 1$$
$$\Rightarrow -\frac{x}{6} > 1$$
$$\Rightarrow -x > 6$$
$$\Rightarrow x < -6$$

Thus, all real numbers x, which are less than -6, are the solutions of the given inequality. Hence, the solution set of the given inequality is  $(-\infty, -6)$ .



# **Question 11:**

Solve the given inequality for real *x*:

$$\frac{3(x-2)}{5} \le \frac{5(2-x)}{3}$$

### Answer 11:

$$\frac{3(x-2)}{5} \le \frac{5(2-x)}{3}$$
  

$$\Rightarrow 9(x-2) \le 25(2-x)$$
  

$$\Rightarrow 9x-18 \le 50-25x$$
  

$$\Rightarrow 9x-18+25x \le 50$$
  

$$\Rightarrow 34x-18 \le 50$$
  

$$\Rightarrow 34x \le 50+18$$
  

$$\Rightarrow 34x \le 68$$
  

$$\Rightarrow \frac{34x}{34} \le \frac{68}{34}$$
  

$$\Rightarrow x \le 2$$

Thus, all real numbers x, which are less than or equal to 2, are the solutions of the given inequality.

Hence, the solution set of the given inequality is  $(-\infty, 2]$ .

# **Question 12:**

Solve the given inequality for real *x*:  $\frac{1}{2}\left(\frac{3x}{5}+4\right) \ge \frac{1}{3}(x-6)$ 

# Answer 12:

$$\frac{1}{2}\left(\frac{3x}{5}+4\right) \ge \frac{1}{3}\left(x-6\right)$$
$$\Rightarrow 3\left(\frac{3x}{5}+4\right) \ge 2\left(x-6\right)$$
$$\Rightarrow \frac{9x}{5}+12 \ge 2x-12$$
$$\Rightarrow 12+12 \ge 2x-\frac{9x}{5}$$
$$\Rightarrow 24 \ge \frac{10x-9x}{5}$$
$$\Rightarrow 24 \ge \frac{x}{5}$$
$$\Rightarrow 120 \ge x$$

Thus, all real numbers x, which are less than or equal to 120, are the solutions of the given inequality.

Hence, the solution set of the given inequality is  $(-\infty, 120]$ .



### **Question 13:**

Solve the given inequality for real x: 2(2x + 3) - 10 < 6(x - 2)

### Answer 13:

2(2x+3)-10 < 6(x-2)  $\Rightarrow 4x+6-10 < 6x-12$   $\Rightarrow 4x-4 < 6x-12$   $\Rightarrow -4+12 < 6x-4x$   $\Rightarrow 8 < 2x$  $\Rightarrow 4 < x$ 

Thus, all real numbers x, which are greater than or equal to 4, are the solutions of the given inequality.

Hence, the solution set of the given inequality is  $[4, \infty)$ .

# **Question 14:**

Solve the given inequality for real x:  $37 - (3x + 5) \ge 9x - 8(x - 3)$ 

# Answer 14:

```
37 - (3x + 5) \ge 9x - 8(x - 3)

\Rightarrow 37 - 3x - 5 \ge 9x - 8x + 24

\Rightarrow 32 - 3x \ge x + 24

\Rightarrow 32 - 24 \ge x + 3x

\Rightarrow 8 \ge 4x

\Rightarrow 2 \ge x
```

Thus, all real numbers x, which are less than or equal to 2, are the solutions of the given inequality.

Hence, the solution set of the given inequality is  $(-\infty, 2]$ .

# **Question 15:**

Solve the given inequality for real *x*:  $\frac{x}{4} < \frac{(5x-2)}{3} - \frac{(7x-3)}{5}$ 



# Answer 15:

$$\frac{x}{4} < \frac{(5x-2)}{3} - \frac{(7x-3)}{5}$$

$$\Rightarrow \frac{x}{4} < \frac{5(5x-2) - 3(7x-3)}{15}$$

$$\Rightarrow \frac{x}{4} < \frac{25x - 10 - 21x + 9}{15}$$

$$\Rightarrow \frac{x}{4} < \frac{4x - 1}{15}$$

$$\Rightarrow 15x < 4(4x - 1)$$

$$\Rightarrow 15x < 16x - 4$$

$$\Rightarrow 4 < 16x - 15x$$

$$\Rightarrow 4 < x$$

Thus, all real numbers x, which are greater than 4, are the solutions of the given inequality. Hence, the solution set of the given inequality is  $(4, \infty)$ .

### **Question 16:**

Solve the given inequality for real x:

$$\frac{(2x-1)}{3} \ge \frac{(3x-2)}{4} - \frac{(2-x)}{5}$$

### Answer 16:

$$\frac{(2x-1)}{3} \ge \frac{(3x-2)}{4} - \frac{(2-x)}{5}$$
  

$$\Rightarrow \frac{(2x-1)}{3} \ge \frac{5(3x-2) - 4(2-x)}{20}$$
  

$$\Rightarrow \frac{(2x-1)}{3} \ge \frac{15x - 10 - 8 + 4x}{20}$$
  

$$\Rightarrow \frac{(2x-1)}{3} \ge \frac{19x - 18}{20}$$
  

$$\Rightarrow 20(2x-1) \ge 3(19x - 18)$$
  

$$\Rightarrow 40x - 20 \ge 57x - 54$$
  

$$\Rightarrow -20 + 54 \ge 57x - 40x$$
  

$$\Rightarrow 34 \ge 17x$$
  

$$\Rightarrow 2 \ge x$$

Thus, all real numbers x, which are less than or equal to 2, are the solutions of the given inequality.

Hence, the solution set of the given inequality is  $(-\infty, 2]$ .



### **Question 17:**

Solve the given inequality and show the graph of the solution on number line: 3x - 2 < 2x + 1

# Answer 17:

3x - 2 < 2x + 1  $\Rightarrow 3x - 2x < 1 + 2$  $\Rightarrow x < 3$ 

The graphical representation of the solutions of the given inequality is as follows.



### **Question 18:**

Solve the given inequality and show the graph of the solution on number line:  $5x - 3 \ge 3x - 5$ 

### Answer 18:

 $5x-3 \ge 3x-5$   $\Rightarrow 5x-3x \ge -5+3$   $\Rightarrow 2x \ge -2$   $\Rightarrow \frac{2x}{2} \ge \frac{-2}{2}$  $\Rightarrow x \ge -1$ 

The graphical representation of the solutions of the given inequality is as follows.





### **Question 19:**

Solve the given inequality and show the graph of the solution on number line:

3(1-x) < 2(x+4)

# Answer 19:

3(1-x) < 2(x+4)  $\Rightarrow 3-3x < 2x+8$   $\Rightarrow 3-8 < 2x+3x$   $\Rightarrow -5 < 5x$   $\Rightarrow \frac{-5}{5} < \frac{5x}{5}$  $\Rightarrow -1 < x$ 

The graphical representation of the solutions of the given inequality is as follows.



### **Question 20:**

Solve the given inequality and show the graph of the solution on number line:

$$\frac{x}{2} \ge \frac{(5x-2)}{3} - \frac{(7x-3)}{5}$$

Answer 20:

$$\frac{x}{2} \ge \frac{(5x-2)}{3} - \frac{(7x-3)}{5}$$

$$\Rightarrow \frac{x}{2} \ge \frac{5(5x-2) - 3(7x-3)}{15}$$

$$\Rightarrow \frac{x}{2} \ge \frac{25x - 10 - 21x + 9}{15}$$

$$\Rightarrow \frac{x}{2} \ge \frac{4x - 1}{15}$$

$$\Rightarrow 15x \ge 2(4x - 1)$$

$$\Rightarrow 15x \ge 8x - 2$$

$$\Rightarrow 15x - 8x \ge 8x - 2 - 8x$$

$$\Rightarrow 7x \ge -2$$

$$\Rightarrow x \ge -\frac{2}{7}$$

The graphical representation of the solutions of the given inequality is as follows.



### **Question 21:**

Ravi obtained 70 and 75 marks in first two unit test. Find the minimum marks he should get in the third test to have an average of at least 60 marks.

### Answer 21:

Let *x* be the marks obtained by Ravi in the third unit test.

Since the student should have an average of at least 60 marks,

$$\frac{70+75+x}{3} \ge 60$$
$$\Rightarrow 145+x \ge 180$$
$$\Rightarrow x \ge 180-145$$
$$\Rightarrow x \ge 35$$

Thus, the student must obtain a minimum of 35 marks to have an average of at least 60 marks.

### **Question 22:**

To receive Grade 'A' in a course, one must obtain an average of 90 marks or more in five examinations (each of 100 marks). If Sunita's marks in first four examinations are 87, 92, 94 and 95, find minimum marks that Sunita must obtain in fifth examination to get grade 'A' in the course.

# Answer 22:

Let x be the marks obtained by Sunita in the fifth examination.

In order to receive grade 'A' in the course, she must obtain an average of 90 marks or more in five examinations.

Therefore,

$$\frac{87 + 92 + 94 + 95 + x}{5} \ge 90$$
$$\Rightarrow \frac{368 + x}{5} \ge 90$$
$$\Rightarrow 368 + x \ge 450$$
$$\Rightarrow x \ge 450 - 368$$
$$\Rightarrow x \ge 82$$

Thus, Sunita must obtain greater than or equal to 82 marks in the fifth examination.



### **Question 23:**

Find all pairs of consecutive odd positive integers both of which are smaller than 10 such that their sum is more than 11.

# Answer 23:

Let x be the smaller of the two consecutive odd positive integers. Then, the other integer is x + 2.

Since both the integers are smaller than 10,

x + 2 < 10  $\Rightarrow x < 10 - 2$   $\Rightarrow x < 8 \dots (i)$ Also, the sum of the two integers is more than 11.  $\therefore x + (x + 2) > 11$   $\Rightarrow 2x + 2 > 11$   $\Rightarrow 2x > 11 - 2$   $\Rightarrow 2x > 9$   $\Rightarrow x > \frac{9}{2}$  $\Rightarrow x > 4.5 \qquad \dots (ii)$ 

From (i) and (ii), we obtain  $\therefore$  Since x is an odd number, x can take the values, 5 and 7. Thus, the required possible pairs are (5, 7) and (7, 9).

### **Question 24:**

Find all pairs of consecutive even positive integers, both of which are larger than 5 such that their sum is less than 23.

### Answer 24:

Let *x* be the smaller of the two consecutive even positive integers. Then, the other integer is x + 2. Since both the integers are larger than 5, x > 5 ......(1) Also, the sum of the two integers is less than 23. x + (x + 2) < 23



 $\Rightarrow 2x + 2 < 23$   $\Rightarrow 2x < 23 - 2$   $\Rightarrow 2x < 21$   $\Rightarrow x < \frac{21}{2}$  $\Rightarrow x < 10.5 \qquad \dots (2)$ 

From (1) and (2), we obtain 5 < x < 10.5. Since x is an even number, x can take the values, 6, 8, and 10. Thus, the required possible pairs are (6, 8), (8, 10), and (10, 12).

### **Question 25:**

The longest side of a triangle is 3 times the shortest side and the third side is 2 cm shorter than the longest side. If the perimeter of the triangle is at least 61 cm, find the minimum length of the shortest side.

### Answer 25:

Let the length of the shortest side of the triangle be x cm.

Then, length of the longest side = 3x cm

Length of the third side = (3x - 2) cm

Since the perimeter of the triangle is at least 61 cm,

 $x \operatorname{cm} + 3x \operatorname{cm} + (3x - 2) \operatorname{cm} \ge 61 \operatorname{cm}$  $\Rightarrow 7x - 2 \ge 61$  $\Rightarrow 7x \ge 61 + 2$  $\Rightarrow 7x \ge 63$  $\Rightarrow \frac{7x}{7} \ge \frac{63}{7}$  $\Rightarrow x \ge 9$ 

Thus, the minimum length of the shortest side is 9 cm.



### **Question 26:**

A man wants to cut three lengths from a single piece of board of length 91 cm. The second length is to be 3 cm longer than the shortest and the third length is to be twice as long as the shortest. What are the possible lengths of the shortest board if the third piece is to be at least 5 cm longer than the second?

[Hint: If x is the length of the shortest board, then x, (x + 3) and 2x are the lengths of the second and third piece, respectively. Thus,  $x = (x + 3) + 2x \le 91$  and  $2x \ge (x + 3) + 5$ ]

### Answer 26:

Let the length of the shortest piece be x cm. Then, length of the second piece and the third piece are (x + 3) cm and 2x cm respectively.

Since the three lengths are to be cut from a single piece of board of length 91 cm, x cm + (x + 3) cm + 2x cm  $\leq$  91 cm  $\Rightarrow 4x + 3 \leq$  91  $\Rightarrow 4x \leq$  91 - 3  $\Rightarrow 4x \leq$  88  $\Rightarrow \frac{4x}{4} \leq \frac{88}{4}$   $\Rightarrow x \leq 22$  ...(1) Also, the third piece is at least 5 cm longer than the second piece.  $\therefore 2x \geq (x + 3) + 5$   $\Rightarrow 2x \geq x + 8$  $\Rightarrow x \geq 8 \dots (2)$ 

From (1) and (2), we obtain

 $8 \le x \le 22$ 

Thus, the possible length of the shortest board is greater than or equal to 8 cm but less than or equal to 22 cm.



# **Mathematics**

(Chapter – 6) (Linear Inequalities) (Class – XI)

# Exercise 6.2

# **Question 1:**

Solve the given inequality graphically in two-dimensional plane: x + y < 5

# Answer 1:

The graphical representation of x + y = 5 is given as dotted line in the figure below. This line divides the *xy*-plane in two half planes, **I** and **II**.

Select a point (not on the line), which lies in one of the half planes, to determine whether the point satisfies the given inequality or not. We select the point as (0, 0).

It is observed that,

0 + 0 < 5 or, 0 < 5, which is true

Therefore, half plane **II** is not the solution region of the given inequality. Also, it is evident that any point on the line does not satisfy the given strict inequality.

Thus, the solution region of the given inequality is the shaded half plane  $\mathbf{I}$  excluding the points on the line.

This can be represented as follows.





# **Question 2:**

Solve the given inequality graphically in two-dimensional plane:  $2x + y \ge 6$ 

# Answer 2:

The graphical representation of 2x + y = 6 is given in the figure below. This line divides the *xy*-plane in two half planes, **I** and **II**.

Select a point (not on the line), which lies in one of the half planes, to determine whether the point satisfies the given inequality or not. We select the point as (0, 0).

It is observed that,  $2(0) + 0 \ge 6 \text{ or } 0 \ge 6$ , which is false Therefore, half plane **I** is not the solution region of the given inequality. Also, it is evident that any point on the line satisfies the given inequality.

Thus, the solution region of the given inequality is the shaded half plane **II** including the points on the line.

This can be represented as follows.





# **Question 3:**

Solve the given inequality graphically in two-dimensional plane:  $3x + 4y \le 12$ 

# Answer 3:

 $3x + 4y \le 12$ The graphical representation of 3x + 4y = 12 is given in the figure below. This line divides the *xy*-plane in two half planes, **I** and **II**.

Select a point (not on the line), which lies in one of the half planes, to determine whether the point satisfies the given inequality or not. We select the point as (0, 0).

It is observed that,

 $3(0) + 4(0) \le 12$  or  $0 \le 12$ , which is true

Therefore, half plane **II** is not the solution region of the given inequality. Also, it is evident that any point on the line satisfies the given inequality.

Thus, the solution region of the given inequality is the shaded half plane  $\mathbf{I}$  including the points on the line.

This can be represented as follows.





# **Question 4:**

Solve the given inequality graphically in two-dimensional plane:  $y + 8 \ge 2x$ 

### Answer 4:

The graphical representation of y + 8 = 2x is given in the figure below. This line divides the *xy*-plane in two half planes.

Select a point (not on the line), which lies in one of the half planes, to determine whether the point satisfies the given inequality or not. We select the point as (0, 0).

It is observed that,

 $0 + 8 \ge 2(0)$  or  $8 \ge 0$ , which is true

Therefore, lower half plane is not the solution region of the given inequality. Also, it is evident that any point on the line satisfies the given inequality.

Thus,

the solution region of the given inequality is the half plane containing the point (0, 0) including the line.





# **Question 5:**

Solve the given inequality graphically in two-dimensional plane:  $x - y \le 2$ 

# Answer 5:

The graphical representation of x - y = 2 is given in the figure below. This line divides the *xy*-plane in two half planes.

Select a point (not on the line), which lies in one of the half planes, to determine whether the point satisfies the given inequality or not. We select the point as (0, 0).

It is observed that,

 $0 - 0 \le 2$  or  $0 \le 2$ , which is true

Therefore, the lower half plane is not the solution region of the given inequality. Also, it is clear that any point on the line satisfies the given inequality.

Thus,

the solution region of the given inequality is the half plane containing the point (0, 0) including the line.





# **Question 6:**

Solve the given inequality graphically in two-dimensional plane: 2x - 3y > 6

### Answer 6:

The graphical representation of 2x - 3y = 6 is given as dotted line in the figure below. This line divides the *xy*-plane in two half planes.

Select a point (not on the line), which lies in one of the half planes, to determine whether the point satisfies the given inequality or not. We select the point as (0, 0).

It is observed that,

2(0) - 3(0) > 6 or 0 > 6, which is false

Therefore, the upper half plane is not the solution region of the given inequality. Also, it is clear that any point on the line does not satisfy the given inequality.

Thus, the solution region of the given inequality is the half plane that does not contain the point (0, 0) excluding the line.





# **Question 7:**

Solve the given inequality graphically in two-dimensional plane:  $-3x + 2y \ge -6$ 

# Answer 7:

The graphical representation of -3x + 2y = -6 is given in the figure below. This line divides the *xy*-plane in two half planes.

Select a point (not on the line), which lies in one of the half planes, to determine whether the point satisfies the given inequality or not. We select the point as (0, 0).

It is observed that,

 $-3(0) + 2(0) \ge -6$  or  $0 \ge -6$ , which is true

Therefore, the lower half plane is not the solution region of the given inequality. Also, it is evident that any point on the line satisfies the given inequality.

Thus,

the solution region of the given inequality is the half plane containing the point (0, 0) including the line.





### **Question 8:**

Solve the given inequality graphically in two-dimensional plane: 3y - 5x < 30

### Answer 8:

The graphical representation of 3y - 5x = 30 is given as dotted line in the figure below. This line divides the *xy*-plane in two half planes.

Select a point (not on the line), which lies in one of the half planes, to determine whether the point satisfies the given inequality or not. We select the point as (0, 0).

It is observed that,

3(0) - 5(0) < 30 or 0 < 30, which is true

Therefore, the upper half plane is not the solution region of the given inequality. Also, it is evident that any point on the line does not satisfy the given inequality.

Thus, the solution region of the given inequality is the half plane containing the point (0, 0) excluding the line.





### **Question 9:**

Solve the given inequality graphically in two-dimensional plane: y < -2

### Answer 9:

The graphical representation of y = -2 is given as dotted line in the figure below. This line divides the *xy*-plane in two half planes.

Select a point (not on the line), which lies in one of the half planes, to determine whether the point satisfies the given inequality or not. We select the point as (0, 0).

It is observed that,

0 < -2, which is false

Also, it is evident that any point on the line does not satisfy the given inequality.

Hence, every point below the line, y = -2 (excluding all the points on the line), determines the solution of the given inequality.





### **Question 10:**

Solve the given inequality graphically in two-dimensional plane: x > -3

### Answer 10:

The graphical representation of x = -3 is given as dotted line in the figure below. This line divides the *xy*-plane in two half planes.

Select a point (not on the line), which lies in one of the half planes, to determine whether the point satisfies the given inequality or not. We select the point as (0, 0).

It is observed that,

0 > -3, which is true

Also, it is evident that any point on the line does not satisfy the given inequality.

Hence, every point on the right side of the line, x = -3 (excluding all the points on the line), determines the solution of the given inequality.





# **Mathematics**

(Chapter – 6) (Linear Inequalities) (Class – XI)

# Exercise 6.3

# **Question 1:**

Solve the following system of inequalities graphically:  $x \ge 3$ ,  $y \ge 2$ .

### Answer 1:

 $x \ge 3$  .....(1)  $y \ge 2$  .....(2)

The graph of the lines, x = 3 and y = 2, are drawn in the figure below. Inequality (1) represents the region on the right hand side of the line, x = 3 (including the line x = 3), and inequality (2) represents the region above the line, y = 2 (including the line y = 2).





# **Question 2:**

Solve the following system of inequalities graphically:  $3x + 2y \le 12, x \ge 1, y \ge 2$ 

# Answer 2:

$3x + 2y \le 12 \dots$	(1)
<i>x</i> ≥ 1	(2)
<i>y</i> ≥ 2	(3)

The graphs of the lines, 3x + 2y = 12, x = 1, and y = 2, are drawn in the figure below.

Inequality (1) represents the region below the line, 3x + 2y = 12 (including the line 3x + 2y = 12). Inequality (2) represents the region on the right side of the line, x = 1 (including the line x = 1). Inequality (3) represents the region above the line, y = 2 (including the line y = 2).





# **Question 3:**

Solve the following system of inequalities graphically:  $2x + y \ge 6$ ,  $3x + 4y \le 12$ 

### Answer 3:

 $2x + y \ge 6$  .....(1)  $3x + 4y \le 12$  .....(2)

The graph of the lines, 2x + y = 6 and 3x + 4y = 12, are drawn in the figure below. Inequality (1) represents the region above the line, 2x + y = 6 (including the line 2x + y = 6), and inequality (2) represents the region below the line, 3x + 4y = 12 (including the line 3x + 4y = 12).





# **Question 4:**

Solve the following system of inequalities graphically:  $x + y \ge 4$ , 2x - y > 0

### Answer 4:

 $x + y \ge 4$  .....(1) 2x - y > 0 .....(2)

The graph of the lines, x + y = 4 and 2x - y = 0, are drawn in the figure below.

Inequality (1) represents the region above the line, x + y = 4 (including the line x + y = 4). It is observed that (1, 0) satisfies the inequality, 2x - y > 0. [2(1) - 0 = 2 > 0] Therefore, inequality (2) represents the half plane corresponding to the line, 2x - y = 0, containing the point (1, 0) [excluding the line 2x - y > 0].

Hence, the solution of the given system of linear inequalities is represented by the common shaded region including the points on line x + y = 4 and excluding the points on line 2x - y = 0 as follows.





# **Question 5:**

Solve the following system of inequalities graphically: 2x - y > 1, x - 2y < -1

# Answer 5:

2x - y > 1 .....(1) x - 2y < -1 .....(2)

The graph of the lines, 2x - y = 1 and x - 2y = -1, are drawn in the figure below.

Inequality (1) represents the region below the line, 2x - y = 1 (excluding the line 2x - y = 1), and inequality (2) represents the region above the line, x - 2y = -1 (excluding the line x - 2y = -1).





# **Question 6:**

Solve the following system of inequalities graphically:  $x + y \le 6$ ,  $x + y \ge 4$ 

# Answer 6:

 $x + y \le 6$  ..... (1)  $x + y \ge 4$  ..... (2)

The graph of the lines, x + y = 6 and x + y = 4, are drawn in the figure below.

Inequality (1) represents the region below the line, x + y = 6 (including the line x + y = 6), and inequality (2) represents the region above the line, x + y = 4 (including the line x + y = 4).





# **Question 7:**

Solve the following system of inequalities graphically:  $2x + y \ge 8$ ,  $x + 2y \ge 10$ 

# Answer 7:

2x + y = 8 .....(1) x + 2y = 10 .....(2)

The graph of the lines, 2x + y = 8 and x + 2y = 10, are drawn in the figure below.

Inequality (1) represents the region above the line, 2x + y = 8, and inequality (2) represents the region above the line, x + 2y = 10.





# **Question 8:**

Solve the following system of inequalities graphically:  $x + y \le 9$ , y > x,  $x \ge 0$ 

### Answer 8:

$X + y \leq 9$	(1)
y > x	(2)
$x \ge 0$	(3)

The graph of the lines, x + y = 9 and y = x, are drawn in the figure below.

Inequality (1) represents the region below the line, x + y = 9 (including the line x + y = 9). It is observed that (0, 1) satisfies the inequality, y > x. [1 > 0] Therefore, inequality (2) represents the half plane corresponding to the line, y = x, containing the point (0, 1) [excluding the line y = x]. Inequality (3) represents the region on the right hand side of the line, x = 0 or y-axis (including y-axis).

Hence, the solution of the given system of linear inequalities is represented by the common shaded region including the points on the lines, x + y = 9 and x = 0, and excluding the points on line y = x as follows.



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### **Question 9:**

Solve the following system of inequalities graphically:  $5x + 4y \le 20, x \ge 1, y \ge 2$ 

### Answer 9:

$5x + 4y \leq 20$	(1)
<i>x</i> ≥ 1	(2)
<i>y</i> ≥ 2	(3)

The graph of the lines, 5x + 4y = 20, x = 1, and y = 2, are drawn in the figure below.

Inequality (1) represents the region below the line, 5x + 4y = 20 (including the line 5x + 4y = 20). Inequality (2) represents the region on the right hand side of the line, x = 1 (including the line x = 1). Inequality (3) represents the region above the line, y = 2 (including the line y = 2).





### **Question 10:**

Solve the following system of inequalities graphically:  $3x + 4y \le 60$ ,  $x + 3y \le 30$ ,  $x \ge 0$ ,  $y \ge 0$ 

### Answer 10:

 $3x + 4y \le 60$  .....(1)  $x + 3y \le 30$  .....(2)

The graph of the lines, 3x + 4y = 60 and x + 3y = 30, are drawn in the figure below.

Inequality (1) represents the region below the line, 3x + 4y = 60 (including the line 3x + 4y = 60), and inequality (2) represents the region below the line, x + 3y = 30 (including the line x + 3y = 30).

Since  $x \ge 0$  and  $y \ge 0$ , every point in the common shaded region in the first quadrant including the points on the respective line and the axes represents the solution of the given system of linear inequalities.





# **Question 11:**

Solve the following system of inequalities graphically:  $2x + y \ge 4$ ,  $x + y \le 3$ ,  $2x - 3y \le 6$ 

### Answer 11:

 $2x + y \ge 4$  ......(1)  $x + y \le 3$  .....(2)  $2x - 3y \le 6$  .....(3)

The graph of the lines, 2x + y = 4, x + y = 3, and 2x - 3y = 6, are drawn in the figure below.

Inequality (1) represents the region above the line, 2x + y = 4 (including the line 2x + y = 4). Inequality (2) represents the region below the line, x + y = 3 (including the line x + y = 3). Inequality (3) represents the region above the line, 2x - 3y = 6 (including the line 2x - 3y = 6).





### **Question 12:**

Solve the following system of inequalities graphically:  $x - 2y \le 3$ ,  $3x + 4y \ge 12$ ,  $x \ge 0$ ,  $y \ge 1$ 

### Answer 12:

The graph of the lines, x - 2y = 3, 3x + 4y = 12, and y = 1, are drawn in the figure below.

Inequality (1) represents the region above the line, x - 2y = 3 (including the line x - 2y = 3). Inequality (2) represents the region above the line, 3x + 4y = 12 (including the line 3x + 4y = 12). Inequality (3) represents the region above the line, y = 1 (including the line y = 1). The inequality,  $x \ge 0$ , represents the region on the right of y-axis (including y - axis).




## **Question 13:**

Solve the following system of inequalities graphically:  $4x + 3y \le 60, y \ge 2x, x \ge 3, x, y \ge 0$ 

## Answer 13:

 $y \ge 2x$  (2)

 $x \ge 3 \tag{3}$ 

The graph of the lines, 4x + 3y = 60, y = 2x, and x = 3, are drawn in the figure below. Inequality (1) represents the region below the line, 4x + 3y = 60 (including the line 4x + 3y = 60). Inequality (2) represents the region above the line, y = 2x (including the line y = 2x). Inequality (3) represents the region on the right hand side of the line, x = 3 (including the line x = 3).

Hence, the solution of the given system of linear inequalities is represented by the common shaded region including the points on the respective lines as follows.





## **Question 14:**

Solve the following system of inequalities graphically:  $3x + 2y \le 150, x + 4y \le 80, x \le 15, y \ge 0, x \ge 0$ 

## Answer 14:

 $3x + 2y \le 150$  .....(1)  $x + 4y \le 80$  .....(2)

The graph of the lines, 3x + 2y = 150, x + 4y = 80, and x = 15, are drawn in the figure below.

Inequality (1) represents the region below the line, 3x + 2y = 150 (including the line 3x + 2y = 150). Inequality (2) represents the region below the line, x + 4y = 80 (including the line x + 4y = 80). Inequality (3) represents the region on the left hand side of the line, x = 15 (including the line x = 15).

Since  $x \ge 0$  and  $y \ge 0$ , every point in the common shaded region in the first quadrant including the points on the respective lines and the axes represents the solution of the given system of linear inequalities.





## **Question 15:**

Solve the following system of inequalities graphically:

 $x + 2y \le 10, x + y \ge 1, x - y \le 0, x \ge 0, y \ge 0$ 

## Answer 15:

 $x + 2y \le 10$  ......(1)

 $x - y \le 0$  (3)

The graph of the lines, x + 2y = 10, x + y = 1, and x - y = 0, are drawn in the figure below.

Inequality (1) represents the region below the line, x + 2y = 10 (including the line x + 2y = 10). Inequality (2) represents the region above the line, x + y = 1 (including the line x + y = 1). Inequality (3) represents the region above the line, x - y = 0 (including the line x - y = 0).

Since  $x \ge 0$  and  $y \ge 0$ , every point in the common shaded region in the first quadrant including the points on the respective lines and the axes represents the solution of the given system of linear inequalities.





# **Mathematics**

(Chapter – 6) (Linear Inequalities) (Class – XI)

## **Miscellaneous Exercise on Chapter 6**

## **Question 1:**

Solve the inequality  $2 \le 3x - 4 \le 5$ 

## Answer 1:

 $2 \le 3x - 4 \le 5$   $\Rightarrow 2 + 4 \le 3x - 4 + 4 \le 5 + 4$   $\Rightarrow 6 \le 3x \le 9$  $\Rightarrow 2 \le x \le 3$ 

Thus, all the real numbers, x, which are greater than or equal to 2 but less than or equal to 3, are the solutions of the given inequality. The solution set for the given inequality is [2, 3].

## **Question 2:**

Solve the inequality  $6 \le -3(2x - 4) < 12$ 

#### Answer 2:

 $6 \le -3(2x - 4) < 12$   $\Rightarrow 2 \le -(2x - 4) < 4$   $\Rightarrow -2 \ge 2x - 4 > -4$   $\Rightarrow 4 - 2 \ge 2x > 4 - 4$   $\Rightarrow 2 \ge 2x > 0$   $\Rightarrow 1 \ge x > 0$ Thus, the solution set for the given inequality is (0, 1].



## **Question 3:**

Solve the inequality  $-3 \le 4 - \frac{7x}{2} \le 18$ 

$$-3 \le 4 - \frac{1}{2} \le 1$$

## Answer 3:

$$-3 \le 4 - \frac{7x}{2} \le 18$$
  

$$\Rightarrow -3 - 4 \le -\frac{7x}{2} \le 18 - 4$$
  

$$\Rightarrow -7 \le -\frac{7x}{2} \le 14$$
  

$$\Rightarrow 7 \ge \frac{7x}{2} \ge -14$$
  

$$\Rightarrow 1 \ge \frac{x}{2} \ge -2$$
  

$$\Rightarrow 2 \ge x \ge -4$$

Thus, the solution set for the given inequality is [-4, 2].

## **Question 4:**

Solve the inequality \_\_\_\_\_

$$15 < \frac{3(x-2)}{5} \le 0$$

## Answer 4:

 $-15 < \frac{3(x-2)}{5} \le 0$  $\Rightarrow -75 < 3(x - 2) \le 0$  $\Rightarrow -25 < x - 2 \le 0$  $\Rightarrow -25 + 2 < x \leq 2$  $\Rightarrow -23 < x \leq 2$ 

Thus, the solution set for the given inequality is (-23, 2].



## **Question 5:**

Solve the inequality -12 < 4 - 4

$$-12 < 4 - \frac{3x}{-5} \le 2$$

## Answer 5:

$$-12 < 4 - \frac{3x}{-5} \le 2$$
$$\Rightarrow -12 - 4 < \frac{-3x}{-5} \le 2 - 3$$
$$\Rightarrow -16 < \frac{3x}{5} \le -2$$
$$\Rightarrow -80 < 3x \le -10$$
$$\Rightarrow \frac{-80}{3} < x \le \frac{-10}{3}$$

1.2

Thus, the solution set for the given inequality is.

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-80	ŝ.	-10
3	,	3

## **Question 6:**

Solve the inequality

$$7 \leq \frac{\left(3x+11\right)}{2} \leq 11$$

## Answer 6:

$$7 \le \frac{(3x+11)}{2} \le 11$$
  

$$\Rightarrow 14 \le 3x+11 \le 22$$
  

$$\Rightarrow 14-11 \le 3x \le 22-11$$
  

$$\Rightarrow 3 \le 3x \le 11$$
  

$$\Rightarrow 1 \le x \le \frac{11}{3}$$

Thus, the solution set for the given inequality is  $\left[1, \frac{11}{3}\right]$ 



## **Question 7:**

Solve the inequalities and represent the solution graphically on number line: 5x + 1 > -24, 5x - 1 < 24

#### Answer 7:

 $5x + 1 > -24 \implies 5x > -25$  $\Rightarrow x > -5 \dots (1)$  $5x - 1 < 24 \implies 5x < 25$  $\Rightarrow x < 5 \dots (2)$ From (1) and (2), it can be conclu

From (1) and (2), it can be concluded that the solution set for the given system of inequalities is (-5, 5). The solution of the given system of inequalities can be represented on number line as

$$\xrightarrow{-\infty} (-5,5) \xrightarrow{(-5,-5)} -7 -6 -5 -4 -3 -2 -1 \ 0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7 \ 8 \xrightarrow{\infty}$$

## **Question 8:**

Solve the inequalities and represent the solution graphically on number line:

2(x-1) < x + 5, 3(x + 2) > 2 - x

#### Answer 8:

 $2(x-1) < x + 5 \qquad \Rightarrow 2x - 2 < x + 5 \qquad \Rightarrow 2x - x < 5 + 2$  $\Rightarrow x < 7 \qquad (1)$  $3(x+2) > 2 - x \qquad \Rightarrow 3x + 6 > 2 - x \qquad \Rightarrow 3x + x > 2 - 6$  $\Rightarrow 4x > - 4$ 

 $\Rightarrow x > -1 \dots (2)$ 

From (1) and (2), it can be concluded that the solution set for the given system of inequalities is (-1, 7). The solution of the given system of inequalities can be represented on number line as

$$\overset{-\infty}{\bullet} \underbrace{(-1,7)}_{-7 -6 -5 -4 -3 -2 -1 \ 0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7 \ 8}^{(-1,7)} \bullet$$



#### **Question 9:**

Solve the following inequalities and represent the solution graphically on number line: 3x - 7 > 2(x - 6), 6 - x > 11 - 2x

## Answer 9:

 $3x - 7 > 2(x - 6) \implies 3x - 7 > 2x - 12 \implies 3x - 2x > -12 + 7$  $\Rightarrow x > -5$  ......(1)

$$6 - x > 11 - 2x \implies -x + 2x > 11 - 6$$

 $\Rightarrow x > 5 \dots (2)$ 

From (1) and (2), it can be concluded that the solution set for the given system of inequalities is  $(5, \infty)$ . The solution of the given system of inequalities can be represented on number line as

$$\overset{-\infty}{\bullet} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -7 & -6 & -5 & -4 & -3 & -2 & -1 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -7 & -7 & -7 & -7 & -7 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -7 & -7 & -7 & -7 & -7 \\ \end{array}}_{-7} \underbrace{\begin{array}{c} (5,\infty) \\ -7 & -7 & -7 & -7 & -7 & -7 \\ \end{array}}_$$

#### **Question 10:**

Solve the inequalities and represent the solution graphically on number line:  $5(2x - 7) - 3(2x + 3) \le 0, 2x + 19 \le 6x + 47$ 

#### Answer 10:

From (1) and (2), it can be concluded that the solution set for the given system of inequalities is [-7, 11]. The solution of the given system of inequalities can be represented on number line as





## **Question 11:**

A solution is to be kept between 68°F and 77°F. What is the range in temperature in degree Celsius (C) if the Celsius/Fahrenheit (F) conversion formula is given by

$$F = \frac{9}{8}C + 32?$$

## Answer 11:

Since the solution is to be kept between 68°F and 77°F, 68 < F < 77

Putting  $F = \frac{9}{5}C + 32$ , we obtain  $68 < \frac{9}{5}C + 32 < 77$   $\Rightarrow 68 - 32 < \frac{9}{5}C < 77 - 32$   $\Rightarrow 36 < \frac{9}{5}C < 45$   $\Rightarrow 36 \times \frac{5}{9} < C < 45 \times \frac{5}{9}$  $\Rightarrow 20 < C < 25$ 

Thus, the required range of temperature in degree Celsius is between 20°C and 25°C.



## **Question 12:**

A solution of 8% boric acid is to be diluted by adding a 2% boric acid solution to it. The resulting mixture is to be more than 4% but less than 6% boric acid. If we have 640 litres of the 8% solution, how many litres of the 2% solution will have to be added?

#### Answer 12:

Let *x* litres of 2% boric acid solution is required to be added.

Then, total mixture = (x + 640) litres

This resulting mixture is to be more than 4% but less than 6% boric acid.

 $\therefore 2\%x + 8\%$  of 640 > 4% of (x + 640) and 2% x + 8% of 640 < 6% of (x + 640)

2% x + 8% of 640 > 4% of (x + 640)

$$\Rightarrow \frac{2}{100} x + \frac{8}{100} (640) > \frac{4}{100} (x + 640)$$
  

$$\Rightarrow 2x + 5120 > 4x + 2560$$
  

$$\Rightarrow 5120 - 2560 > 4x - 2x$$
  

$$\Rightarrow 5120 - 2560 > 2x$$
  

$$\Rightarrow 2560 > 2x$$
  

$$\Rightarrow 1280 > x$$
  

$$2\% x + 8\% \text{ of } 640 < 6\% \text{ of } (x + 640)$$
  

$$\frac{2}{100} x + \frac{8}{100} (640) < \frac{6}{100} (x + 640)$$
  

$$\Rightarrow 2x + 5120 < 6x + 3840$$
  

$$\Rightarrow 5120 - 3840 < 6x - 2x$$
  

$$\Rightarrow 1280 < 4x$$
  

$$\Rightarrow 320 < x$$
  

$$\therefore 320 < x < 1280$$

Thus, the number of litres of 2% of boric acid solution that is to be added will have to be more than 320 litres but less than 1280 litres.



## **Question 13:**

How many litres of water will have to be added to 1125 litres of the 45% solution of acid so that the resulting mixture will contain more than 25% but less than 30% acid content?

#### Answer 13:

Let *x* litres of water is required to be added.

Then, total mixture = (x + 1125) litres

It is evident that the amount of acid contained in the resulting mixture is 45% of 1125 litres.

This resulting mixture will contain more than 25% but less than 30% acid content.

 $\therefore 30\%$  of (1125 + x) > 45% of 1125

And, 25% of (1125 + *x*) < 45% of 1125

30% of (1125 + *x*) > 45% of 1125

$$\Rightarrow \frac{30}{100} (1125 + x) > \frac{45}{100} \times 1125$$
  

$$\Rightarrow 30(1125 + x) > 45 \times 1125$$
  

$$\Rightarrow 30 \times 1125 + 30x > 45 \times 1125$$
  

$$\Rightarrow 30x > 45 \times 1125 - 30 \times 1125$$
  

$$\Rightarrow 30x > (45 - 30) \times 1125$$
  

$$\Rightarrow x > \frac{15 \times 1125}{30} = 562.5$$
  
25% of  $(1125 + x) < 45\%$  of  $1125$   

$$\Rightarrow \frac{25}{100} (1125 + x) < \frac{45}{100} \times 1125$$
  

$$\Rightarrow 25(1125 + x) > 45 \times 1125$$
  

$$\Rightarrow 25x > 1125 + 25x > 45 \times 1125$$
  

$$\Rightarrow 25x > 45 \times 1125 - 25 \times 1125$$
  

$$\Rightarrow 25x > (45 - 25) \times 1125$$
  

$$\Rightarrow x > \frac{20 \times 1125}{25} = 900$$

Thus, the required number of litres of water that is to be added will have to be more than 562.5 but less than 900.



## **Question 14:**

IQ of a person is given by the formula

$$IQ = \frac{MA}{CA} \times 100,$$

Where MA is mental age and CA is chronological age. If  $80 \le IQ \le 140$  for a group of 12 years old children, find the range of their mental age.

## Answer 14:

It is given that for a group of 12 years old children,  $80 \le IQ \le 140$  ......(i) For a group of 12 years old children, CA = 12 years  $IQ = \frac{MA}{12} \times 100$ Putting this value of IQ in (i), we obtain

$$80 \le \frac{MA}{12} \times 100 \le 140$$
$$\Rightarrow 80 \times \frac{12}{100} \le MA \le 140 \times \frac{12}{100}$$
$$\Rightarrow 9.6 \le MA \le 16.8$$

Thus, the range of mental age of the group of 12 years old children is  $9.6 \le MA \le 16.8$ 

