

## Measures of Central Tendency (Mean, Median, Quartiles & Mode)

---

### Exercise 24A

#### Question 1.

Find the mean of the following set of numbers:

(i) 6, 9, 11, 12 and 7

(ii) 11, 14, 23, 26, 10, 12, 18 and 6

#### Solution:

(i)

$$\bar{x} = \frac{x_1 + x_2 + \dots + x_n}{n}$$

Here  $n = 5$

$$\therefore \bar{x} = \frac{6 + 9 + 11 + 12 + 7}{5} = \frac{45}{5} = 9$$

(ii)

$$\bar{x} = \frac{x_1 + x_2 + \dots + x_n}{n}$$

Here  $n = 8$

$$\therefore \bar{x} = \frac{11 + 14 + 23 + 26 + 10 + 12 + 18 + 6}{8} = \frac{120}{8} = 15$$

#### Question 2.

Marks obtained (in mathematics) by 9 student are given below:

60, 67, 52, 76, 50, 51, 74, 45 and 56

(a) find the arithmetic mean

(b) if marks of each student be increased by 4; what will be the new value of arithmetic mean.

**Solution:**

(a) Here  $n = 9$

$$\bar{x} = \frac{x_1 + x_2 + \dots + x_n}{n}$$

$$\therefore \bar{x} = \frac{60 + 67 + 52 + 76 + 50 + 51 + 74 + 45 + 56}{9} = \frac{531}{9} = 59$$

(b)

If marks of each student be increased by 4 then new arithmetic mean will be  $= 59 + 4 = 63$

**Question 3.**

Find the mean of the natural numbers from 3 to 12.

**Solution:**

Numbers between 3 to 12 are 3, 4, 5, 6, 7, 8, 9, 10, 11 and 12.

Here  $n = 10$

$$\bar{x} = \frac{x_1 + x_2 + \dots + x_n}{n}$$

$$\therefore \bar{x} = \frac{3 + 4 + 5 + 6 + 7 + 8 + 9 + 10 + 11 + 12}{10} = \frac{75}{10} = 7.5$$

**Question 4.**

(a) Find the mean of 7, 11, 6, 5, and 6

(b) If each number given in (a) is diminished by 2, find the new value of mean.

**Solution:**

(a) The mean of 7, 11, 6, 5 and 6

$$\bar{x} = \frac{7 + 11 + 6 + 5 + 6}{5} = \frac{35}{5} = 7$$

(b)

If we subtract 2 from each number, then the mean will be  $7 - 2 = 5$

**Question 5.**

If the mean of 6, 4, 7, 'a' and 10 is 8. Find the value of 'a'

**Solution:**

No. of terms = 5

Mean = 8

Sum of numbers =  $8 \times 5 = 40$  ..(i)

But, sum of numbers =  $6+4+7+a+10 = 27+a$  ..(ii)

From (i) and (ii)

$$27+a = 40$$

$$a = 13$$

**Question 6.**

The mean of the number 6, 'y', 7, 'x' and 14 is 8. Express 'y' in terms of 'x'.

**Solution:**

No. of terms = 5 and mean = 8

Sum of numbers =  $5 \times 8 = 40$  ..(i)

but sum of numbers =  $6+y+7+x+14 = 27+y+x$  ..(ii)

from (i) and (ii)

$$27 + y + x = 40$$

$$x + y = 13$$

$$y = 13 - x$$

**Question 7.**

The ages of 40 students are given in the following table:

| Age( in yrs) | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
|--------------|----|----|----|----|----|----|----|
| Frequency    | 2  | 4  | 6  | 9  | 8  | 7  | 4  |

Find the arithmetic mean.

**Solution:**

| Age in yrs<br>$x_i$ | Frequency<br>( $f_i$ ) | $f_i x_i$ |
|---------------------|------------------------|-----------|
| 12                  | 2                      | 24        |
| 13                  | 4                      | 52        |
| 14                  | 6                      | 84        |
| 15                  | 9                      | 135       |
| 16                  | 8                      | 128       |
| 17                  | 7                      | 119       |
| 18                  | 4                      | 72        |
| Total               | 40                     | 614       |

$$\bar{x} = \frac{\sum f_i x_i}{\sum f} = \frac{614}{40} = 15.35$$

**Question 8.**

If 69.5 is the mean of 72, 70, 'x', 62, 50, 71, 90, 64, 58 and 82, find the value of 'x'.

**Solution:**

No. of terms = 10

Mean = 69.5

Sum of the numbers =  $69.5 \times 10 = 695$  .....(i)

But sum of numbers =  $72+70+x+62+ 50+71+90+64+58+82$

=  $619 + x$  .....(ii)

from (i) and (ii)

$619 + x = 695$

$x = 76$

**Question 9.**

The following table gives the heights of plants in centimeter. If the mean height of plants is 60.95 cm; find the value of 'f'.

|               |    |    |    |    |    |    |    |
|---------------|----|----|----|----|----|----|----|
| Height (cm)   | 50 | 55 | 58 | 60 | 65 | 70 | 71 |
| No. of plants | 2  | 4  | 10 | f  | 5  | 4  | 3  |

**Solution:**

| Height (cm)<br>$x_i$ | No. of Plants<br>$f_i$ | $f_i x_i$  |
|----------------------|------------------------|------------|
| 50                   | 2                      | 100        |
| 55                   | 4                      | 220        |
| 58                   | 10                     | 580        |
| 60                   | f                      | 60f        |
| 65                   | 5                      | 325        |
| 70                   | 4                      | 280        |
| 71                   | 3                      | 213        |
| Total                | 28+f                   | 1718 + 60f |

Mean = 60.95

$$\therefore \frac{1718 + 60f}{28 + f} = 60.95$$

$$\Rightarrow 1718 + 60f = 60.95(28 + f)$$

$$\Rightarrow 1718 + 60f = 1706.6 + 60.95f$$

$$\Rightarrow (60.95 - 60)f = 1718.0 - 1706.6$$

$$\Rightarrow 0.95f = 11.4$$

$$\therefore f = \frac{11.4}{0.95} = 12$$

**Question 10.**

From the data given below, calculate the mean wage, correct to the nearest rupee.

| Category       | A  | B  | C  | D  | E  | F   |
|----------------|----|----|----|----|----|-----|
| Wages (Rs/day) | 50 | 60 | 70 | 80 | 90 | 100 |
| No. of workers | 2  | 4  | 8  | 12 | 10 | 6   |

(i) If the number of workers in each category is doubled, what would be the new mean wage?

(ii) If the wages per day in each category are increased by 60%; what is the new mean wage?

(iii) If the number of workers in each category is doubled and the wages per day per worker are reduced by 40%, what would be the new mean wage?

**Solution:**

| Wages (Rs/day) (x) | No. of Workers (f) | fx   |
|--------------------|--------------------|------|
| 50                 | 2                  | 100  |
| 60                 | 4                  | 240  |
| 70                 | 8                  | 560  |
| 80                 | 12                 | 960  |
| 90                 | 10                 | 900  |
| 100                | 6                  | 600  |
| Total              | 42                 | 3360 |

$$\bar{x} = \frac{\sum fx}{\sum f} = \frac{3360}{42} = 80$$

(i) Mean remains the same if the number of workers in each category is doubled.

Mean = 80

(ii) Mean will be increased by 60% if the wages per day per worker is increased by 60%

$$\text{New mean} = 80 \times \frac{160}{100} = 128$$

(iii) No change in the mean if the number of workers is doubled but if wages per worker is reduced by 40%, then

$$\text{New mean} = 80 \times \frac{60}{100} = 48$$

**Question 11.**

The contents of 100 match boxes were checked to determine the number of matches they contained.

|                |    |    |    |    |    |    |    |
|----------------|----|----|----|----|----|----|----|
| No. of matches | 35 | 36 | 37 | 38 | 39 | 40 | 41 |
| No. of boxes   | 6  | 10 | 18 | 25 | 21 | 12 | 8  |

(i) calculate, correct to one decimal place, the mean number of matches per box.

(ii) Determine how many extra matches would have to be added to the total contents of the 100 boxes to bring the mean up to exactly 39 matches.

**Solution:**

| No. of matches<br>(x) | No. of boxes<br>(f) | fx   |
|-----------------------|---------------------|------|
| 35                    | 6                   | 210  |
| 36                    | 10                  | 360  |
| 37                    | 18                  | 666  |
| 38                    | 25                  | 950  |
| 39                    | 21                  | 819  |
| 40                    | 12                  | 480  |
| 41                    | 8                   | 328  |
| Total                 | 100                 | 3813 |

$$(i) \bar{x} = \frac{\sum fx}{\sum f} = \frac{3813}{100} = 38.13$$

(ii) In the second case,

New mean = 39 matches

Total contents =  $39 \times 100 = 3900$

But total number of matches already given = 3813

Number of new matches to be added =  $3900 - 3813 = 87$

**Question 12.**

If the mean of the following distribution is 3, find the value of p.

|   |   |   |   |   |       |
|---|---|---|---|---|-------|
| x | 1 | 2 | 3 | 5 | p + 4 |
| f | 9 | 6 | 9 | 3 | 6     |

**Solution:**

We have,

| x     | f               | fx                    |
|-------|-----------------|-----------------------|
| 1     | 9               | 9                     |
| 2     | 6               | 12                    |
| 3     | 9               | 27                    |
| 5     | 3               | 15                    |
| p + 4 | 6               | 6p + 24               |
|       | $\Sigma f = 33$ | $\Sigma fx = 6p + 87$ |

$$\text{Now, Mean} = \frac{\Sigma fx}{\Sigma f}$$

$$\Rightarrow 3 = \frac{6p + 87}{33}$$

$$\Rightarrow 99 = 6p + 87$$

$$\Rightarrow 6p = 12$$

$$\Rightarrow p = 2$$

**Question 13.**

In the following table,  $\Sigma f = 200$  and mean = 73. Find the missing frequencies  $f_1$ , and  $f_2$ .

|   |    |       |       |     |     |     |
|---|----|-------|-------|-----|-----|-----|
| x | 0  | 50    | 100   | 150 | 200 | 250 |
| f | 46 | $f_1$ | $f_2$ | 25  | 10  | 5   |

**Solution:**

We have,

| x   | f                           | fx                                  |
|-----|-----------------------------|-------------------------------------|
| 0   | 46                          | 0                                   |
| 50  | $f_1$                       | $50f_1$                             |
| 100 | $f_2$                       | $100f_2$                            |
| 150 | 25                          | 3750                                |
| 200 | 10                          | 2000                                |
| 250 | 5                           | 1250                                |
|     | $\Sigma f = 86 + f_1 + f_2$ | $\Sigma fx = 7000 + 50f_1 + 100f_2$ |

Given,  $\Sigma f = 200$

$$\Rightarrow 86 + f_1 + f_2 = 200$$

$$\Rightarrow f_1 + f_2 = 114 \quad \dots(i)$$

$$\text{Mean} = \frac{\Sigma fx}{\Sigma f}$$

$$\Rightarrow 73 = \frac{7000 + 50f_1 + 100f_2}{200}$$

$$\Rightarrow 7000 + 50f_1 + 100f_2 = 14600$$

$$\Rightarrow 50f_1 + 100f_2 = 7600$$

$$\Rightarrow f_1 + 2f_2 = 152 \quad \dots(ii)$$

Subtracting (ii) from (i), we get

$$f_2 = 38$$

$$\Rightarrow f_1 = 114 - 38 = 76$$

Hence,  $f_1 = 76$  and  $f_2 = 38$

#### Question 14.

Find the arithmetic mean (correct to the nearest whole-number) by using step-deviation method.

| x | 5  | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 | 50 |
|---|----|----|----|----|----|----|----|----|----|----|
| f | 20 | 43 | 75 | 67 | 72 | 45 | 39 | 9  | 8  | 6  |



**Solution:**

Let the assumed mean  $A = 30$

| $x$      | $f$              | $d = x - A$ | $t = \frac{x - A}{i} = \frac{x - 30}{5}$ | $ft$               |
|----------|------------------|-------------|------------------------------------------|--------------------|
| 5        | 20               | -25         | -5                                       | -100               |
| 10       | 43               | -20         | -4                                       | -172               |
| 15       | 75               | -15         | -3                                       | -225               |
| 20       | 67               | -10         | -2                                       | -134               |
| 25       | 72               | -5          | -1                                       | -72                |
| $A = 30$ | 45               | 0           | 0                                        | 0                  |
| 35       | 39               | 5           | 1                                        | 39                 |
| 40       | 9                | 10          | 2                                        | 18                 |
| 45       | 8                | 15          | 3                                        | 24                 |
| 50       | 6                | 20          | 4                                        | 24                 |
|          | $\Sigma f = 384$ |             |                                          | $\Sigma ft = -598$ |

$$\begin{aligned}
 \therefore \text{Mean} &= A + \frac{\Sigma ft}{\Sigma f} \times i \\
 &= 30 + \frac{(-598)}{384} \times 5 \\
 &= 30 - \frac{299}{192} \times 5 \\
 &= 30 - \frac{1495}{192} \\
 &= \frac{5760 - 1495}{192} \\
 &= \frac{4265}{192} \\
 &= 22.21 \\
 &= 22
 \end{aligned}$$

**Question 15.**

Find the mean (correct to one place of decimal) by using short-cut method.

|     |    |    |    |    |    |    |    |
|-----|----|----|----|----|----|----|----|
| $x$ | 40 | 41 | 43 | 45 | 46 | 49 | 50 |
| $f$ | 14 | 28 | 38 | 50 | 40 | 20 | 10 |

**Solution:**

Let the assumed mean  $A = 45$

| $x$      | $f$              | $d = x - A$<br>$= x - 45$ | $fd$              |
|----------|------------------|---------------------------|-------------------|
| 40       | 14               | -5                        | -70               |
| 41       | 28               | -4                        | -112              |
| 43       | 38               | -2                        | -76               |
| $A = 45$ | 50               | 0                         | 0                 |
| 46       | 40               | 1                         | 40                |
| 49       | 20               | 4                         | 80                |
| 50       | 10               | 5                         | 50                |
|          | $\Sigma f = 200$ |                           | $\Sigma fd = -88$ |

$$\begin{aligned}\therefore \text{Mean} &= A + \frac{\Sigma fd}{\Sigma f} \\ &= 45 + \frac{(-88)}{200} \\ &= 45 - \frac{11}{25} \\ &= \frac{1125 - 11}{25} \\ &= \frac{1114}{25} \\ &= 44.6\end{aligned}$$

**Exercise 24B****Question 1.**

The following table gives the ages of 50 students of a class. Find the arithmetic mean of their ages.

| Age - Years     | 16 - 18 | 18 - 20 | 20 - 22 | 22 - 24 | 24 - 26 |
|-----------------|---------|---------|---------|---------|---------|
| No. of Students | 2       | 7       | 21      | 17      | 3       |

**Solution:**

| Age in years<br>C.I. | $x_i$ | Number of students ( $f_i$ ) | $x_i f_i$ |
|----------------------|-------|------------------------------|-----------|
| 16 - 18              | 17    | 2                            | 34        |
| 18 - 20              | 19    | 7                            | 133       |
| 20 - 22              | 21    | 21                           | 441       |
| 22 - 24              | 23    | 17                           | 391       |
| 24 - 26              | 25    | 3                            | 75        |
| Total                |       | 50                           | 1074      |

$$\bar{x} = \frac{\sum f_i x_i}{\sum f_i} = \frac{1074}{50} = 21.48$$

**Question 2.**

The following table gives the weekly wages of workers in a factory.

| Weekly Wages (Rs) | No. of Workers |
|-------------------|----------------|
| 50-55             | 5              |
| 55-60             | 20             |
| 60-65             | 10             |
| 65-70             | 10             |
| 70-75             | 9              |
| 75-80             | 6              |
| 80-85             | 12             |
| 85-90             | 8              |

Calculate the mean by using:

(i) Direct Method

(ii) Short - Cut Method

**Solution:**

(i) Direct Method

| Weekly Wages (Rs) | Mid-Value $x_i$ | No. of Workers ( $f_i$ ) | $f_i x_i$ |
|-------------------|-----------------|--------------------------|-----------|
| 50-55             | 52.5            | 5                        | 262.5     |
| 55-60             | 57.5            | 20                       | 1150.0    |
| 60-65             | 62.5            | 10                       | 625.0     |
| 65-70             | 67.5            | 10                       | 675.0     |
| 70-75             | 72.5            | 9                        | 652.5     |
| 75-80             | 77.5            | 6                        | 465.0     |
| 80-85             | 82.5            | 12                       | 990.0     |
| 85-90             | 87.5            | 8                        | 700.0     |
| Total             |                 | 80                       | 5520.00   |

$$\bar{x} = \frac{\sum f_i x_i}{\sum f_i} = \frac{5520}{80} = 69$$

(ii) Short - cut method

| Weekly wages (Rs) | No. of workers ( $f_i$ ) | Mid-value $x_i$ | $A = 72.5$<br>$d_i = x_i - A$ | $f_i d_i$ |
|-------------------|--------------------------|-----------------|-------------------------------|-----------|
| 50-55             | 5                        | 52.5            | -20                           | -100      |
| 55-60             | 20                       | 57.5            | -15                           | -300      |
| 60-65             | 10                       | 62.5            | -10                           | -100      |
| 65-70             | 10                       | 67.5            | -5                            | -50       |
| 70-75             | 9                        | $A=72.5$        | 0                             | 0         |
| 75-80             | 6                        | 77.5            | 5                             | 30        |
| 80-85             | 12                       | 82.5            | 10                            | 120       |
| 85-90             | 8                        | 87.5            | 15                            | 120       |
| Total             | 80                       |                 |                               | -280      |

$$\bar{x} = A + \frac{\sum f_i d_i}{\sum f_i} = 72.5 + \left( \frac{-280}{80} \right) = 72.5 - 3.5 = 69$$

**Question 3.**

The following are the marks obtained by 70 boys in a class test:

| Marks    | No. of boys |
|----------|-------------|
| 30 - 40  | 10          |
| 40 - 50  | 12          |
| 50 - 60  | 14          |
| 60 - 70  | 12          |
| 70 - 80  | 9           |
| 80 - 90  | 7           |
| 90 - 100 | 6           |

Calculate the mean by:

- (i) Short - cut method
- (ii) Step - deviation method

**Solution:**

(i) Short - cut method

| Marks    | No. of boys ( $f_i$ ) | Mid-value $x_i$ | $A = 65$<br>$d_i = x_i - A$ | $f_i d_i$ |
|----------|-----------------------|-----------------|-----------------------------|-----------|
| 30 - 40  | 10                    | 35              | -30                         | -300      |
| 40 - 50  | 12                    | 45              | -20                         | -240      |
| 50 - 60  | 14                    | 55              | -10                         | -140      |
| 60 - 70  | 12                    | $A = 65$        | 0                           | 0         |
| 70 - 80  | 9                     | 75              | 10                          | 90        |
| 80 - 90  | 7                     | 85              | 20                          | 140       |
| 90 - 100 | 6                     | 95              | 30                          | 180       |
| Total    | 70                    |                 |                             | -270      |

$$\bar{x} = A + \frac{\sum f_i d_i}{\sum f_i} = 65 + \left( \frac{-270}{70} \right) = 65 - 3.86 = 61.14$$

(ii) Step - deviation method

| Marks    | No. of boys ( $f_i$ ) | Mid-value $x_i$ | $A = 65$<br>$u_i = \frac{x_i - A}{h}$ | $f_i u_i$ |
|----------|-----------------------|-----------------|---------------------------------------|-----------|
| 30 - 40  | 10                    | 35              | -3                                    | -30       |
| 40 - 50  | 12                    | 45              | -2                                    | -24       |
| 50 - 60  | 14                    | 55              | -1                                    | -14       |
| 60 - 70  | 12                    | $A = 65$        | 0                                     | 0         |
| 70 - 80  | 9                     | 75              | 1                                     | 9         |
| 80 - 90  | 7                     | 85              | 2                                     | 14        |
| 90 - 100 | 6                     | 95              | 3                                     | 18        |
| Total    | 70                    |                 |                                       | -27       |

Here  $A = 65$  and  $h = 10$

$$\bar{x} = A + h \times \frac{\sum f_i u_i}{\sum f_i} = 65 + 10 \times \left( \frac{-27}{70} \right) = 65 - 3.86 = 61.14$$

**Question 4.**

Find mean by step - deviation method:

|       |       |       |       |       |       |        |         |
|-------|-------|-------|-------|-------|-------|--------|---------|
| C. I. | 63-70 | 70-77 | 77-84 | 84-91 | 91-98 | 98-105 | 105-112 |
| Freq  | 9     | 13    | 27    | 38    | 32    | 16     | 15      |

**Solution:**

| C. I.     | Frequency ( $f_i$ ) | Mid-value $x_i$ | $A = 87.50$<br>$u_i = \frac{x_i - A}{h}$ | $f_i u_i$ |
|-----------|---------------------|-----------------|------------------------------------------|-----------|
| 63 - 70   | 9                   | 66.50           | -3                                       | -27       |
| 70 - 77   | 13                  | 73.50           | -2                                       | -26       |
| 77 - 84   | 27                  | 80.50           | -1                                       | -27       |
| 84 - 91   | 38                  | $A = 87.50$     | 0                                        | 0         |
| 91 - 98   | 32                  | 94.50           | 1                                        | 32        |
| 98 - 105  | 16                  | 101.50          | 2                                        | 32        |
| 105 - 112 | 15                  | 108.50          | 3                                        | 45        |
| Total     | 150                 |                 |                                          | 29        |

Here  $A = 87.50$  and  $h = 7$ 

$$\bar{x} = A + h \times \frac{\sum f_i u_i}{\sum f_i} = 87.5 + 7 \times \frac{29}{150} = 87.5 + 1.35 = 88.85$$

**Question 5.**The mean of the following frequency distribution is  $21\frac{1}{7}$ . Find the value of 'f'.

|       |        |         |         |         |         |
|-------|--------|---------|---------|---------|---------|
| C. I. | 0 - 10 | 10 - 20 | 20 - 30 | 30 - 40 | 40 - 50 |
| freq  | 8      | 22      | 31      | f       | 2       |

**Solution:**

$$\bar{x} = 21\frac{1}{7} = \frac{148}{7}$$

| C. I. | frequency | Mid-value ( $x_i$ ) | $f_i x_i$  |
|-------|-----------|---------------------|------------|
| 0-10  | 8         | 5                   | 40         |
| 10-20 | 22        | 15                  | 330        |
| 20-30 | 31        | 25                  | 775        |
| 30-40 | $f$       | 35                  | $35f$      |
| 40-50 | 2         | 45                  | 90         |
| Total | $63+f$    |                     | $1235+35f$ |

$$\bar{x} = \frac{\sum f_i x_i}{\sum f_i} = \frac{1235 + 35f}{63 + f}$$

$$\Rightarrow \frac{148}{7} = \frac{1235 + 35f}{63 + f}$$

$$\Rightarrow 9324 + 148f = 8645 + 245f$$

$$\Rightarrow 245f - 148f = 9324 - 8645$$

$$\Rightarrow f = \frac{679}{97}$$

$$\Rightarrow f = 7$$

**Question 6.**

Using step-deviation method, calculate the mean marks of the following distribution.

| C.I       | 50-55 | 55-60 | 60-65 | 65-70 | 70-75 | 75-80 | 80-85 | 85-90 |
|-----------|-------|-------|-------|-------|-------|-------|-------|-------|
| Frequency | 5     | 20    | 10    | 10    | 9     | 6     | 12    | 8     |



**Solution:**

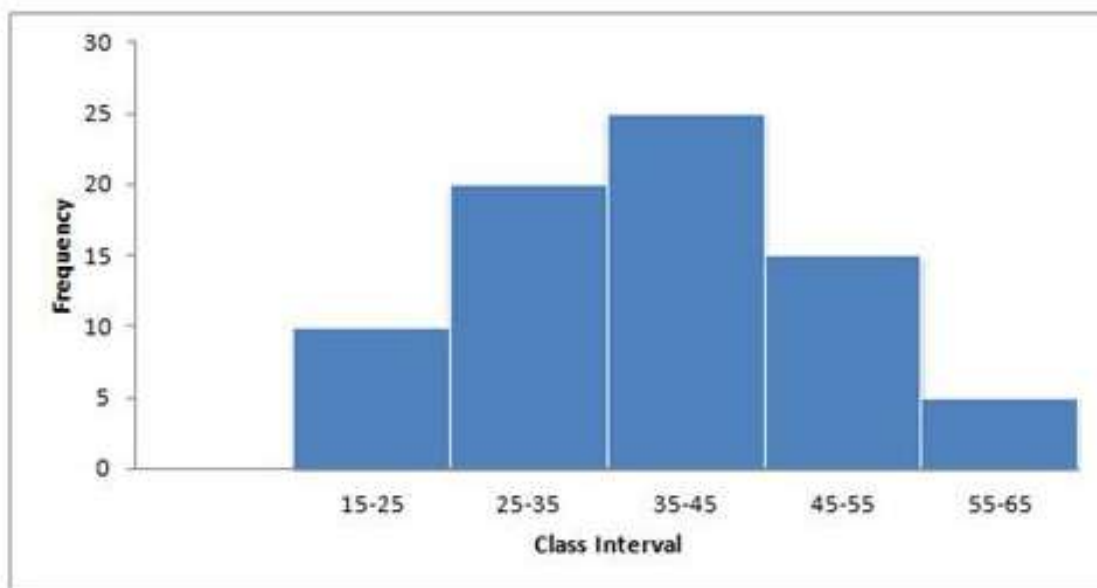
Let the assumed mean  $A = 72.5$

| C.I   | $f_i$ | Mid value<br>( $x_i$ ) | $d_i = x_i - A$ | $f_i d_i$ |
|-------|-------|------------------------|-----------------|-----------|
| 50-55 | 5     | 52.5                   | -20             | -100      |
| 55-60 | 20    | 57.5                   | -15             | -300      |
| 60-65 | 10    | 62.5                   | -10             | -100      |
| 65-70 | 10    | 67.5                   | -5              | -50       |
| 70-75 | 9     | 72.5                   | 0               | 0         |
| 75-80 | 6     | 77.5                   | 5               | 30        |
| 80-85 | 12    | 82.5                   | 10              | 120       |
| 85-90 | 8     | 87.5                   | 15              | 120       |
| Total | 80    |                        | -280            |           |

$$\text{Mean} = A + \frac{\sum f_i d_i}{\sum f_i} = 72.5 + \left( -\frac{280}{80} \right) = 69$$

**Question 7.**

Using the information given in the adjoining histogram, calculate the mean.



**Solution:**

| C.I.  | Frequency | Mid value x | fx   |
|-------|-----------|-------------|------|
| 15-25 | 10        | 20          | 200  |
| 25-35 | 20        | 30          | 600  |
| 35-45 | 25        | 40          | 1000 |
| 45-55 | 15        | 50          | 750  |
| 55-65 | 5         | 60          | 300  |
| Total | 75        |             | 2850 |

$$\bar{x} = \frac{\sum fx}{\sum f} = \frac{2850}{75} = 38$$

**Question 8.**

If the mean of the following observations is 54, find the value of 'p'.

| Class     | 0 - 20 | 20 - 40 | 40 - 60 | 60 - 80 | 80 - 100 |
|-----------|--------|---------|---------|---------|----------|
| Frequency | 7      | p       | 10      | 9       | 13       |

**Solution:**

| Class    | Frequency (f) | Mid Value (x) | fx         |
|----------|---------------|---------------|------------|
| 0 - 20   | 7             | 10            | 70         |
| 20 - 40  | p             | 30            | 30p        |
| 40 - 60  | 10            | 50            | 500        |
| 60 - 80  | 9             | 70            | 630        |
| 80 - 100 | 13            | 90            | 1170       |
| Total    | 39 + p        |               | 2370 + 30p |

$$\bar{x} = \frac{\sum fx}{\sum f} = \frac{2370 + 30p}{39 + p} \dots\dots(i)$$

Here mean = 54 ..(ii)

from (i) and (ii)

$$\frac{2370 + 30p}{39 + p} = 54$$

$$\Rightarrow 2370 + 30p = 2106 + 54p$$

$$\Rightarrow 54p - 30p = 2370 - 2106$$

$$\Rightarrow p = \frac{264}{24} = 11$$

**Question 9.**

The mean of the following distribution is 62.8 and the sum of all the frequencies is 50. Find the missing frequencies  $f_1$  and  $f_2$ .

|       |      |       |       |       |        |         |
|-------|------|-------|-------|-------|--------|---------|
| Class | 0-20 | 20-40 | 40-60 | 60-80 | 80-100 | 100-120 |
| Freq  | 5    | $f_1$ | 10    | $f_2$ | 7      | 8       |

**Solution:**

| Class   | Freq (f)     | Mid value | fx                 |
|---------|--------------|-----------|--------------------|
| 0-20    | 5            | 10        | 50                 |
| 20-40   | $f_1$        | 30        | $30f_1$            |
| 40-60   | 10           | 50        | 500                |
| 60-80   | $f_2$        | 70        | $70f_2$            |
| 80-100  | 7            | 90        | 630                |
| 100-120 | 8            | 110       | 880                |
| Total   | $30+f_1+f_2$ |           | $2060+30f_1+70f_2$ |

Now,  $\sum f = 30 + f_1 + f_2$  and  $\sum fx = 2060 + 30f_1 + 70f_2, \dots (i)$

$\sum f = 50$ ; mean = 62.8....(ii)

from (i)

$$30 + f_1 + f_2 = 50$$

$$f_1 + f_2 = 20, \dots (iii)$$

using (i) and (ii)

$$\text{mean} = \frac{2060 + 30f_1 + 70f_2}{50}$$

$$62.8 = \frac{2060 + 30f_1 + 70f_2}{50}$$

$$2060 + 30f_1 + 70f_2 = 62.8 \times 50$$

$$2060 + 30f_1 + 70f_2 = 3140$$

$$30f_1 + 70f_2 = 1080$$

$$3f_1 + 7f_2 = 108, \dots (iv)$$

from (iii) and (iv)

$$f_1 = 8$$

$$f_2 = 12$$

**Question 10.**

Calculate the mean of the distribution, given below, using the short cut method:

| Mark            | 11-20 | 21-30 | 31-40 | 41-50 | 51-60 | 61-70 | 71-80 |
|-----------------|-------|-------|-------|-------|-------|-------|-------|
| No. of students | 2     | 6     | 10    | 12    | 9     | 7     | 4     |

**Solution:**

| Marks   | f               | x        | d = x - A<br>= x - 45.5 | fd               |
|---------|-----------------|----------|-------------------------|------------------|
| 11 - 20 | 2               | 15.5     | -30                     | -60              |
| 21 - 30 | 6               | 25.5     | -20                     | -120             |
| 31 - 40 | 10              | 35.5     | -10                     | -100             |
| 41 - 50 | 12              | A = 45.5 | 0                       | 0                |
| 51 - 60 | 9               | 55.5     | 10                      | 90               |
| 61 - 70 | 7               | 65.5     | 20                      | 140              |
| 71 - 80 | 4               | 75.5     | 30                      | 120              |
|         | $\Sigma f = 50$ |          |                         | $\Sigma fd = 70$ |

$$\begin{aligned}
 \therefore \text{Mean} &= A + \frac{\Sigma fd}{\Sigma f} \\
 &= 45.5 + \frac{70}{50} \\
 &= 45.5 + \frac{7}{5} \\
 &= \frac{227.5 + 7}{5} \\
 &= \frac{234.5}{5} \\
 &= 46.9
 \end{aligned}$$

**Question 11.**

Calculate the mean of the following distribution:

| Class interval | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 | 50-60 |
|----------------|------|-------|-------|-------|-------|-------|
| Frequency      | 8    | 5     | 12    | 35    | 24    | 16    |

**Solution:**

We have,

| C.I.    | f                | Class mark<br>x | fx                 |
|---------|------------------|-----------------|--------------------|
| 0 – 10  | 8                | 5               | 40                 |
| 10 – 20 | 5                | 15              | 75                 |
| 20 – 30 | 12               | 25              | 300                |
| 30 – 40 | 35               | 35              | 1225               |
| 40 – 50 | 24               | 45              | 1080               |
| 50 – 60 | 16               | 55              | 880                |
|         | $\Sigma f = 100$ |                 | $\Sigma fx = 3600$ |

$$\text{Now, Mean} = \frac{\Sigma fx}{\Sigma f} = \frac{3600}{100} = 36$$

**Exercise 24C****Question 1.**

A student got the following marks in 9 questions of a question paper.

3, 5, 7, 3, 8, 0, 1, 4 and 6.

Find the median of these marks.

**Solution:**

Arranging the given data in descending order:

8, 7, 6, 5, 4, 3, 3, 1, 0

The middle term is 4 which is the 5th term.

Median = 4

**Question 2.**

The weights (in kg) of 10 students of a class are given below:

21, 28.5, 20.5, 24, 25.5, 22, 27.5, 28, 21 and 24.

Find the median of their weights.

**Solution:**

Arranging the given data in descending order:

28.5, 28, 27.5, 25.5, 24, 24, 22, 21, 21, 20.5

The middle terms are 24 and 24, 5<sup>th</sup> and 6<sup>th</sup> terms

$$\therefore \text{median} = \frac{24 + 24}{2} = \frac{48}{2} = 24$$

**Question 3.**

The marks obtained by 19 students of a class are given below:

27, 36, 22, 31, 25, 26, 33, 24, 37, 32, 29, 28, 36, 35, 27, 26, 32, 35 and 28. Find:

- (i) median
- (ii) lower quartile
- (iii) upper quartile
- (iv) interquartile range

**Solution:**

Arranging in ascending order:

22, 24, 25, 26, 26, 27, 27, 28, 28, 29, 31, 32, 32, 33, 35, 35, 36, 36, 37

(i) Middle term is 10<sup>th</sup> term i.e. 29

Median = 29

(ii) Lower quartile =

$$q_1 = \frac{n+1}{4} \text{ term}$$

$$q_1 = \frac{19+1}{4} \text{ term}$$

$$q_1 = 5^{\text{th}} \text{ term} = 26$$

(iii) Upper quartile =

$$q_3 = \left[ \frac{3(n+1)}{4} \right]^{\text{th}} \text{ term}$$

$$q_3 = \left[ \frac{3(19+1)}{4} \right]^{\text{th}} \text{ term}$$

$$q_3 = 15^{\text{th}} \text{ term} = 35$$

(iv) Interquartile range =  $q_3 - q_1 = 35 - 26 = 9$

**Question 4.**

From the following data, find:

- (i) Median
- (ii) Upper quartile
- (iii) Inter-quartile range

25, 10, 40, 88, 45, 60, 77, 36, 18, 95, 56, 65, 7, 0, 38 and 83

**Solution:**

Arrange in ascending order:

0, 7, 10, 18, 25, 36, 38, 40, 45, 56, 60, 65, 77, 83, 88, 95

(i) Median is the mean of 8<sup>th</sup> and 9<sup>th</sup> term

$$= \frac{40 + 45}{2} = \frac{85}{2} = 42.5$$

(ii) Upper quartile =

$$q_3 = \left( \frac{3(n)}{4} \right)^{\text{th}} \text{ term}$$

$$q_3 = \frac{3 \times 16}{4} \text{ term} = 12^{\text{th}} \text{ term} = 65$$

(iii) Interquartile range =

$$q_1 = \frac{16}{4} \text{ term} = 4^{\text{th}} \text{ term} = 18; q_3 = 65$$

$$\text{Interquartile range} = q_3 - q_1$$

$$\begin{aligned} \therefore q_3 - q_1 &= 65 - 18 \\ &= 47 \end{aligned}$$

**Question 5.**

The ages of 37 students in a class are given in the following table:

|                |    |    |    |    |    |    |
|----------------|----|----|----|----|----|----|
| Age (in years) | 11 | 12 | 13 | 14 | 15 | 16 |
| Frequency      | 2  | 4  | 6  | 10 | 8  | 7  |

Find the median.

**Solution:**

| Age<br>(in years) | Frequency | Cumulative<br>Frequency |
|-------------------|-----------|-------------------------|
| 11                | 2         | 2                       |
| 12                | 4         | 6                       |
| 13                | 6         | 12                      |
| 14                | 10        | 22                      |
| 15                | 8         | 30                      |
| 16                | 7         | 37                      |

Number of terms = 37

$$\text{Median} = \frac{37 + 1^{\text{th}}}{2} \text{ term} = 19^{\text{th}} \text{ term}$$

Median = 14

**Question 6.**

The weight of 60 boys are given in the following distribution table:

|             |    |    |    |    |    |
|-------------|----|----|----|----|----|
| Weight (kg) | 37 | 38 | 39 | 40 | 41 |
| No. of boys | 10 | 14 | 18 | 12 | 6  |

Find:

(i) median

(ii) lower quartile

(iii) upper quartile

(iv) interquartile range



**Solution:**

| Weight<br>(kg) x | no. of boys<br>f | cumulative frequency |
|------------------|------------------|----------------------|
| 37               | 10               | 10                   |
| 38               | 14               | 24                   |
| 39               | 18               | 42                   |
| 40               | 12               | 54                   |
| 41               | 6                | 60                   |

Number of terms = 60

(i) median = the mean of the 30<sup>th</sup> and the 31<sup>st</sup> terms

$$\therefore \text{median} = \frac{39 + 39}{2} = \frac{78}{2} = 39$$

(ii) lower quartile ( $Q_1$ ) =  $\frac{60^{\text{th}}}{4}$  term = 15<sup>th</sup> term = 38

(iii) upper quartile ( $Q_3$ ) =  $\frac{3 \times 60^{\text{th}}}{4}$  term = 45<sup>th</sup> term = 40

(iv) Interquartile range =  $Q_3 - Q_1 = 40 - 38 = 2$

**Question 7.**

Estimate the median for the given data by drawing an ogive:

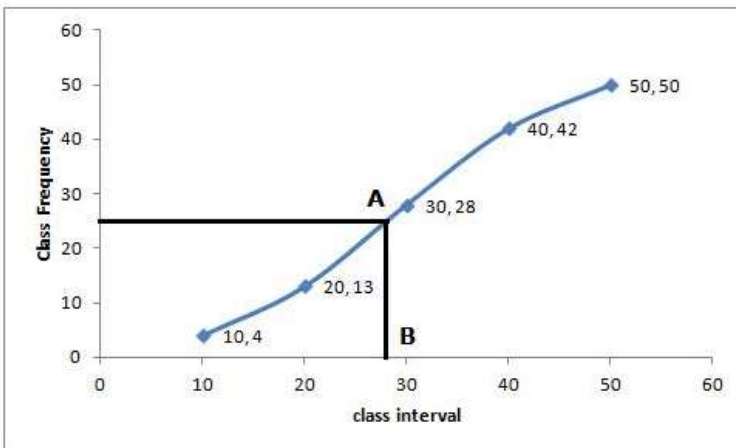
| Class     | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 |
|-----------|------|-------|-------|-------|-------|
| frequency | 4    | 9     | 15    | 14    | 8     |

**Solution:**

| Class | Frequency | Cumulative Frequency |
|-------|-----------|----------------------|
| 0-10  | 4         | 4                    |
| 10-20 | 9         | 13                   |
| 20-30 | 15        | 28                   |
| 30-40 | 14        | 42                   |
| 40-50 | 8         | 50                   |

Number of terms = 50

$$\therefore \text{Median} = \frac{25 + 26^{\text{th}}}{2} \text{ term} = 25.5^{\text{th}} \text{ term}$$



Through mark of 25.5 on the y-axis, draw a line parallel to x-axis which meets the curve at A. From A, draw a perpendicular to x-axis, which meets x-axis at B.

The value of B is the median which is 28.

**Question 8.**

By drawing an ogive, estimate the median for the following frequency distribution:

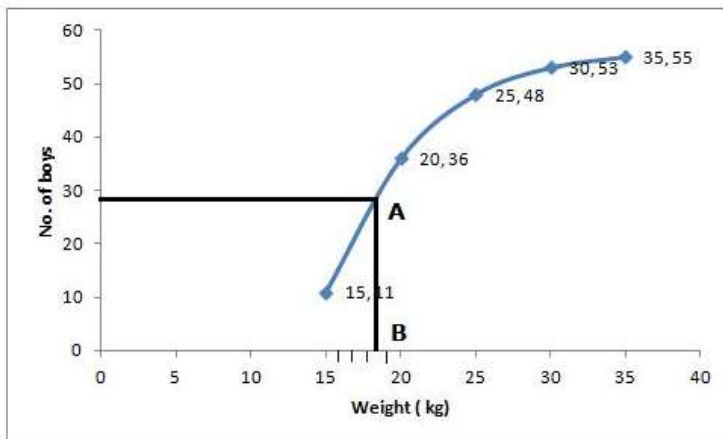
| Weight (kg) | 10-15 | 15-20 | 20-25 | 25-30 | 30-35 |
|-------------|-------|-------|-------|-------|-------|
| No. of boys | 11    | 25    | 12    | 5     | 2     |

**Solution:**

| Weight (kg) | No. of boys | Cumulative Frequency |
|-------------|-------------|----------------------|
| 10-15       | 11          | 11                   |
| 15-20       | 25          | 36                   |
| 20-25       | 12          | 48                   |
| 25-30       | 5           | 53                   |
| 30-35       | 2           | 55                   |

Number of terms = 55

$$\therefore \text{Median} = \frac{55 + 1^{\text{th}}}{2} \text{ term} = 28^{\text{th}} \text{ term}$$



Through mark of 28 on the y-axis, draw a line parallel to x-axis which meets the curve at A. From A, draw a perpendicular to x-axis, which meets x-axis at B.

The value of B is the median which is 18.4 kg

**Question 9.**

From the following cumulative frequency table, find:

- (i) median
- (ii) lower quartile
- (iii) upper quartile

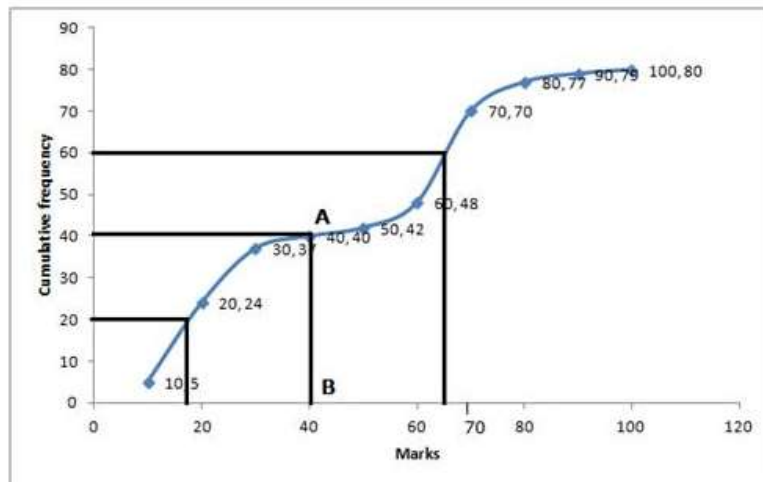
| Marks(less than)     | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | 100 |
|----------------------|----|----|----|----|----|----|----|----|----|-----|
| Cumulative frequency | 5  | 24 | 37 | 40 | 42 | 48 | 70 | 77 | 79 | 80  |

### Solution:

| Marks<br>(less than) | Cumulative frequency |
|----------------------|----------------------|
| 10                   | 5                    |
| 20                   | 24                   |
| 30                   | 37                   |
| 40                   | 40                   |
| 50                   | 42                   |
| 60                   | 48                   |
| 70                   | 70                   |
| 80                   | 77                   |
| 90                   | 79                   |
| 100                  | 80                   |

Number of terms = 80

Median = 40<sup>th</sup> term.



(i) Median = Through 40<sup>th</sup> term mark draw a line parallel to the x-axis which meets the curve at A. From A, draw a perpendicular to x-axis which meets it at B.

Value of B is the median = 40

(ii) Lower quartile ( $Q_1$ ) = 20<sup>th</sup> term = 18

(iii) Upper Quartile ( $Q_3$ ) = 60<sup>th</sup> term = 66

### Question 10.

In a school, 100 pupils have heights as tabulated below:

| Height<br>(in cm) | No. of<br>pupils |
|-------------------|------------------|
| 121 - 130         | 12               |
| 131 - 140         | 16               |
| 141 - 150         | 30               |
| 151 - 160         | 20               |
| 161 - 170         | 14               |
| 171 - 180         | 8                |

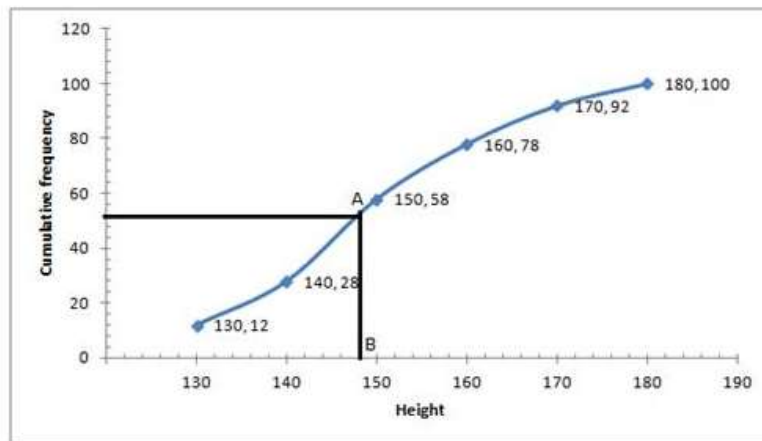
Find the median height by drawing an ogive.

### Solution:

| Height (in cm) | No. of pupils | Cumulative Frequency |
|----------------|---------------|----------------------|
| 121 - 130      | 12            | 12                   |
| 131 - 140      | 16            | 28                   |
| 141 - 150      | 30            | 58                   |
| 151 - 160      | 20            | 78                   |
| 161 - 170      | 14            | 92                   |
| 171 - 180      | 8             | 100                  |

Number of terms = 100

$$\therefore \text{Median} = \frac{100}{2} = 50^{\text{th}} \text{ term}$$



Through  $50^{\text{th}}$  term mark draw a line parallel to the x-axis which meets the curve at A. From A, draw a perpendicular to x-axis which meets it at B.

Value of B is the median = 148

⇒ Median height = 148cm

### Question 11.

Attempt this question on a graph paper. The table shows the distribution of marks gained by a group of 400 students in an examination.

| Marks (less than) | 10 | 20 | 30 | 40 | 50  | 60  | 70  | 80  | 90  | 100 |
|-------------------|----|----|----|----|-----|-----|-----|-----|-----|-----|
| No. Of Students   | 5  | 10 | 30 | 60 | 105 | 180 | 270 | 355 | 390 | 400 |

Using a scale of 2 cm to represent 10 marks and 2 cm to represent 50 students, plot these points and draw a smooth curve through the points.

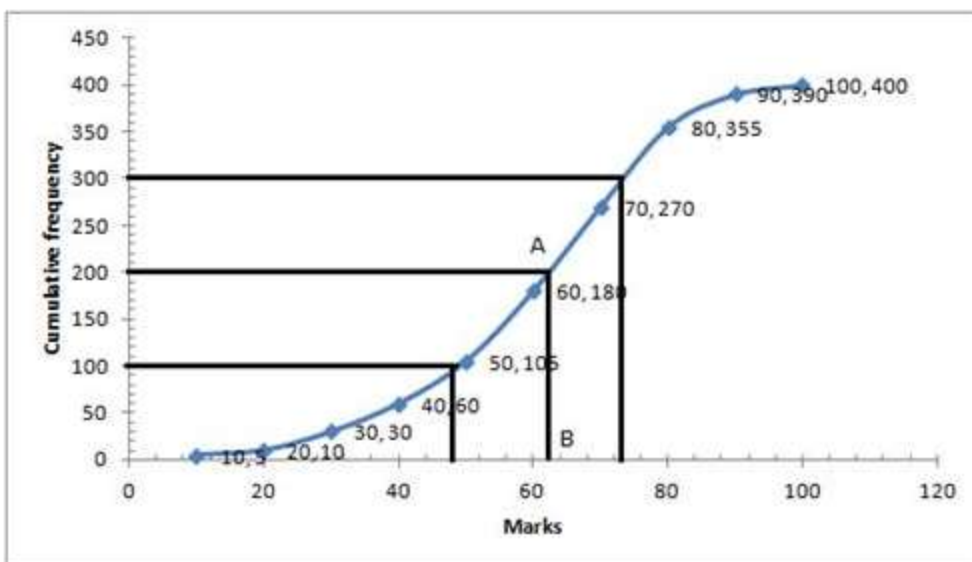
Estimate from the graph:

- (i) the median marks
- (ii) the quartile marks

### Solution:

| Marks<br>(less than) | No. of students |
|----------------------|-----------------|
| 10                   | 5               |
| 20                   | 10              |
| 30                   | 30              |
| 40                   | 60              |
| 50                   | 105             |
| 60                   | 180             |
| 70                   | 270             |
| 80                   | 355             |
| 90                   | 390             |
| 100                  | 400             |

Number of terms = 400



$$(i) \therefore \text{Median} = \frac{400}{2} = 200^{\text{th}} \text{ term}$$

Through 200<sup>th</sup> term mark draw a line parallel to the x-axis which meets the curve at A. From A, draw a perpendicular to x-axis which meets it at B.

Value of B is the median = 62

$$(ii) \text{ Lower Quartile} = Q_1 = \frac{400}{4} = 100^{\text{th}} \text{ term} = 49$$

$$\text{Upper Quartile} = 400 \times \frac{3}{4} = 300^{\text{th}} \text{ term} = 74$$

## Question 12.

Attempt this question on graph paper.

| Age (yrs)         | 5-15 | 15-25 | 25-35 | 35-45 | 45-55 | 55-65 | 65-75 |
|-------------------|------|-------|-------|-------|-------|-------|-------|
| No. of casualties | 6    | 10    | 15    | 13    | 24    | 8     | 7     |

(i) Construct the 'less than' cumulative frequency curve for the above data. Using 2 cm = 10 years on one axis and 2 cm = 10 casualties on the other.

(ii) From your graph determine:

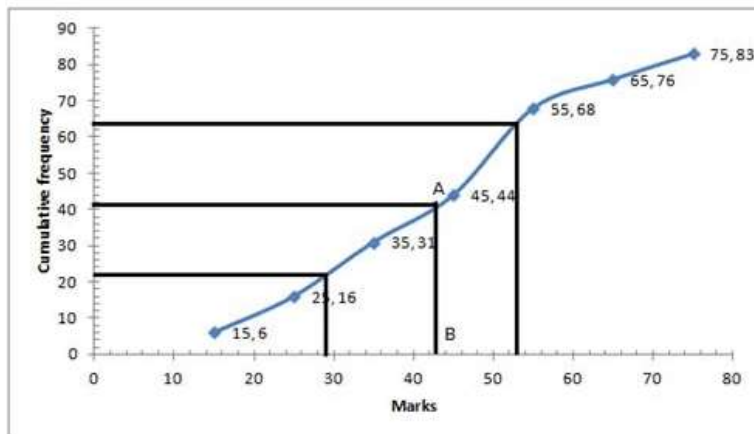
(a) the median

(b) the lower quartile

## Solution:

| Age (years) | No. of casualties | Cumulative Frequency |
|-------------|-------------------|----------------------|
| 5-15        | 6                 | 6                    |
| 15-25       | 10                | 16                   |
| 25-35       | 15                | 31                   |
| 35-45       | 13                | 44                   |
| 45-55       | 24                | 68                   |
| 55-65       | 8                 | 76                   |
| 65-75       | 7                 | 83                   |

Number of terms = 83



$$(i) \therefore \text{Median} = \frac{83}{2} = 41.5^{\text{th}} \text{ term}$$

Through  $41.5^{\text{th}}$  term mark draw a line parallel to the x-axis which meets the curve at A. From A, draw a perpendicular to x-axis which meets it at B.

Value of B is the median = 43

$$(ii) \text{Lower Quartile} = Q_1 = \frac{83}{4} = 20\frac{3}{4} \text{ term} = 29$$

$$\text{Upper Quartile} = 83 \times \frac{3}{4} = 62\frac{1}{4} \text{ term} = 53$$

## Exercise 24D

### Question 1.

Find the mode of the following data:

- (i) 7, 9, 8, 7, 7, 6, 8, 10, 7 and 6
- (ii) 9, 11, 8, 11, 16, 9, 11, 5, 3, 11, 17 and 8

### Solution:

(i) Mode = 7

Since 7 occurs 4 times

(ii) Mode = 11

Since it occurs 4 times

### Question 2.

The following table shows the frequency distribution of heights of 50 boys:

|             |     |     |     |     |     |
|-------------|-----|-----|-----|-----|-----|
| Height (cm) | 120 | 121 | 122 | 123 | 124 |
| Frequency   | 5   | 8   | 18  | 10  | 9   |

Find the mode of heights.

### Solution:

Mode is 122 cm because it occur maximum number of times. i.e. frequency is 18.

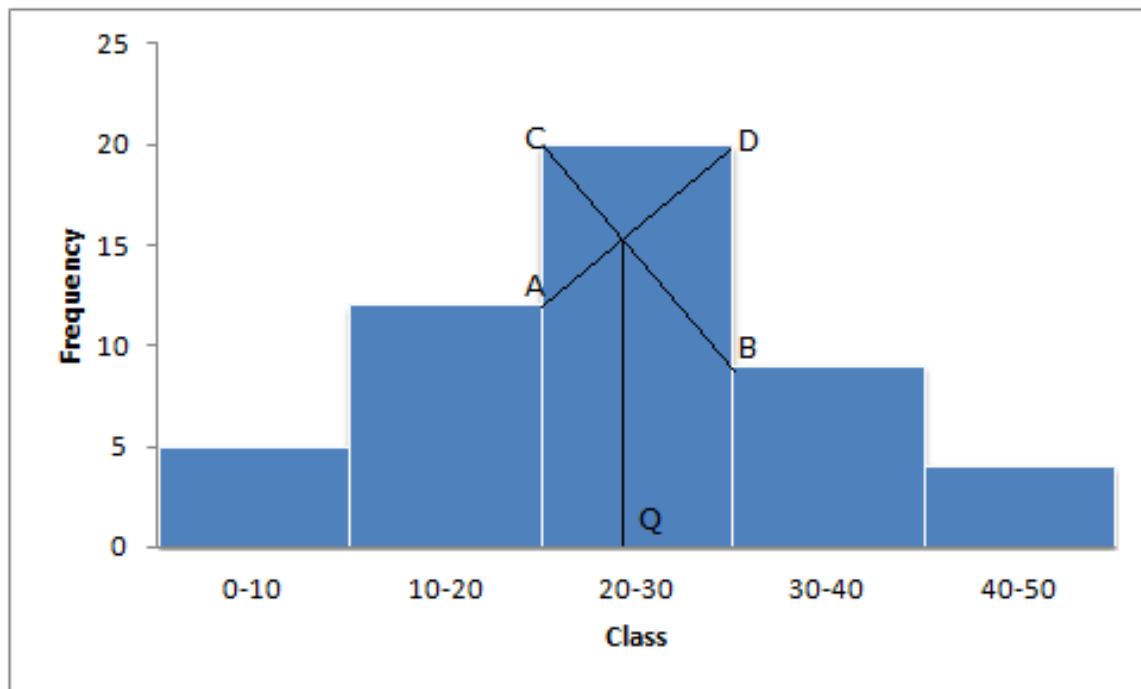
### Question 3.

Find the mode of following data, using a histogram:

|           |      |       |       |       |       |
|-----------|------|-------|-------|-------|-------|
| Class     | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 |
| Frequency | 5    | 12    | 20    | 9     | 4     |



**Solution:**



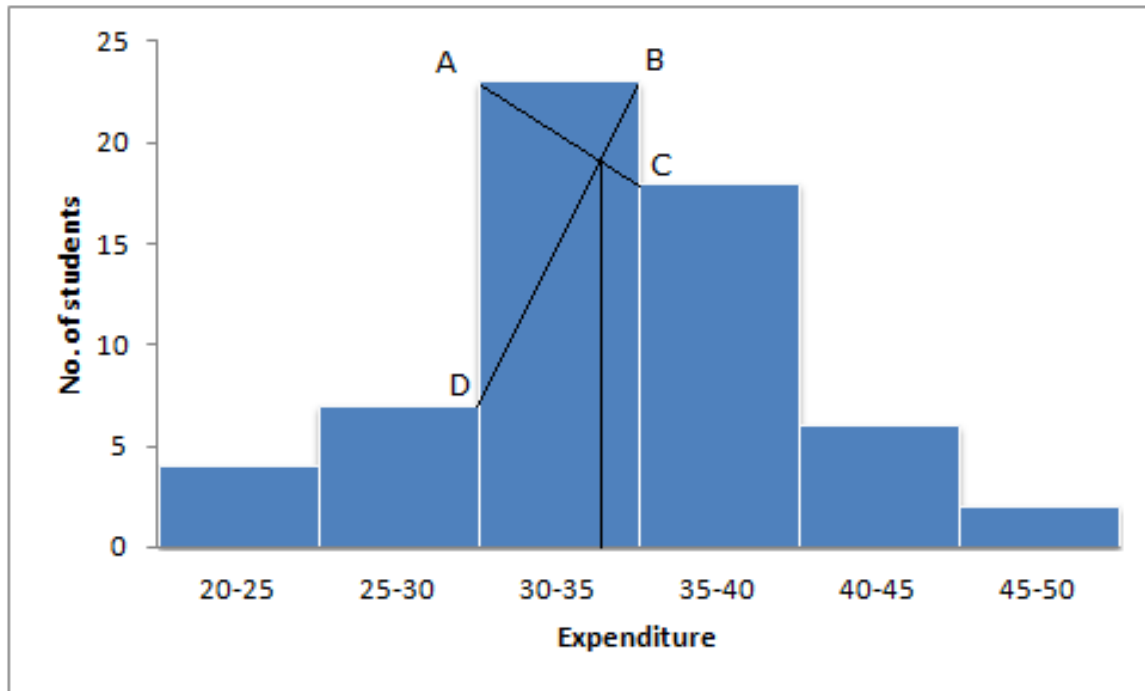
Mode is in 20-30, because in this class there are 20 frequencies.

**Question 4.**

The following table shows the expenditure of 60 boys on books. Find the mode of their expenditure:

| Expenditure (Rs) | No. of students |
|------------------|-----------------|
| 20-25            | 4               |
| 25-30            | 7               |
| 30-35            | 23              |
| 35-40            | 18              |
| 40-45            | 6               |
| 45-50            | 2               |

**Solution:**



Mode is in 30-35 because it has the maximum frequency.

**Question 5.**

Find the median and mode for the set of numbers:

2, 2, 3, 5, 5, 5, 6, 8 and 9

**Solution:**

$$\text{Median} = \frac{9+1}{2} = 5^{\text{th}} \text{ term which is 5.}$$

Mode = 5 because it occurs maximum number of times.

**Question 6.**

A boy scored following marks in various class tests during a term; each test being marked out of 20.

15, 17, 16, 7, 10, 12, 14, 16, 19, 12 and 16

- (i) What are his modal marks?
- (ii) What are his median marks?
- (iii) What are his total marks?
- (iv) What are his mean marks?

**Solution:**

Arranging the given data in ascending order:

7, 10, 12, 12, 14, 15, 16, 16, 16, 17, 19

(i) Mode = 16 as it occurs maximum number of times.

(ii) Median =  $\frac{11+1}{2} = 6^{\text{th}}$  term = 15

(iii) Total marks =  $7+10+12+12+14+15+16+16+16+17+19 =$

154

(iv) Mean( $\bar{x}$ ) =  $\frac{x_1 + x_2 + x_3 + \dots + x_n}{n} = \frac{154}{11} = 14$

**Question 7.**

Find the mean, median and mode of the following marks obtained by 16 students in a class test marked out of 10 marks.

0, 0, 2, 2, 3, 3, 3, 4, 5, 5, 5, 5, 6, 6, 7 and 8.

**Solution:**

(i) Mean =  $\frac{0+0+2+2+3+3+3+4+5+5+5+5+6+6+7+8}{16} = \frac{64}{16} = 4$

(ii) Median = mean of 8<sup>th</sup> and 9<sup>th</sup> term

$= \frac{4+5}{2} = \frac{9}{2} = 4.5$

(iii) Mode = 5 as it occurs maximum number of times.

**Question 8.**

At a shooting competition the score of a competitor were as given below:

|              |   |   |   |   |   |   |
|--------------|---|---|---|---|---|---|
| Score        | 0 | 1 | 2 | 3 | 4 | 5 |
| No. of shots | 0 | 3 | 6 | 4 | 7 | 5 |

(i) What was his modal score?

(ii) What was his median score?

(iii) What was his total score?

(iv) What was his mean score?

**Solution:**

| Score<br>x | No. of shots<br>f | fx |
|------------|-------------------|----|
| 0          | 0                 | 0  |
| 1          | 3                 | 3  |
| 2          | 6                 | 12 |
| 3          | 4                 | 12 |
| 4          | 7                 | 28 |
| 5          | 5                 | 25 |
| Total      | 25                | 80 |

(i) Modal score = 4 as it has maximum frequency 7.

(ii) Median =  $\frac{25 + 1}{2} = 13^{\text{th}}$  term = 3

(iii) Total score = 80

(iv) Mean =  $\frac{80}{25} = 3.2$

## Exercise 24E

### Question 1.

The following distribution represents the height of 160 students of a school.

| Height (in cm) | No. of Students |
|----------------|-----------------|
| 140-145        | 12              |
| 145-150        | 20              |
| 150-155        | 30              |
| 155-160        | 38              |
| 160-165        | 24              |
| 165-170        | 16              |
| 170-175        | 12              |
| 175-180        | 8               |

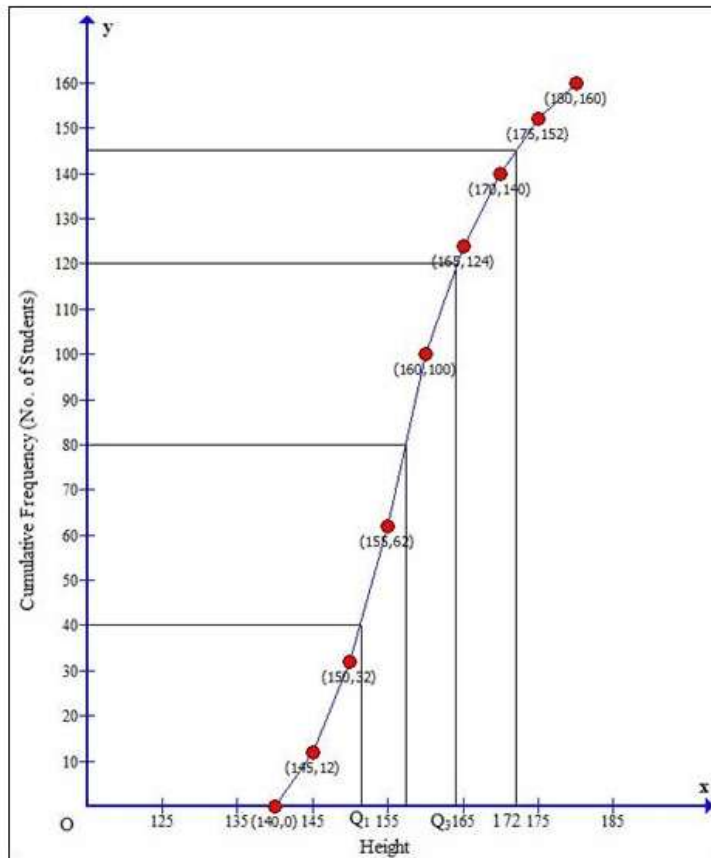
Draw an ogive for the given distribution taking 2 cm = 5 cm of height on one axis and 2 cm = 20 students on the other axis. Using the graph, determine:

- The median height.
- The interquartile range.
- The number of students whose height is above 172 cm.

**Solution:**

| Height (in cm) | No. of Students | Cumulative frequency |
|----------------|-----------------|----------------------|
| 140-145        | 12              | 12                   |
| 145-150        | 20              | 32                   |
| 150-155        | 30              | 62                   |
| 155-160        | 38              | 100                  |
| 160-165        | 24              | 124                  |
| 165-170        | 16              | 140                  |
| 170-175        | 12              | 152                  |
| 175-180        | 8               | 160                  |
| N = 160        |                 |                      |

Taking Height of student along x-axis and cumulative frequency along y-axis we will draw an ogive.



(i)

$$\therefore \text{Median} = \frac{160}{2} = 80^{\text{th}} \text{ term}$$

Through mark for 80, draw a parallel line to x-axis which meets the curve; then from the curve draw a vertical line which meets the x-axis at the mark of 157.5.

(ii) Since, number of terms = 160

$$\text{Lower quartile } (Q_1) = \left( \frac{160}{4} \right) = 40^{\text{th}} \text{ term} = 152$$

$$\text{Upper quartile } (Q_3) = \left( \frac{3 \times 160}{4} \right) = 120^{\text{th}} \text{ term} = 164$$

$$\begin{aligned} \text{Inner Quartile range} &= Q_3 - Q_1 \\ &= 164 - 152 \\ &= 12 \end{aligned}$$

(iii) Through mark for 172 on x-axis, draw a vertical line which meets the curve; then from the curve draw a horizontal line which meets the y-axis at the mark of 145.

The number of students whose height is above 172 cm

$$= 160 - 144 = 16$$

## Question 2.

The following table gives the weekly wages of workers in a factory:

| Weekly wages<br>(in Rs) | No. of<br>workers |
|-------------------------|-------------------|
| 50-55                   | 5                 |
| 55-60                   | 20                |
| 60-65                   | 10                |
| 65-70                   | 10                |
| 70-75                   | 9                 |
| 75-80                   | 6                 |
| 80-85                   | 12                |
| 85-90                   | 8                 |

Calculate: (i) the mean, (ii) the modal class, (iii) the number of workers getting weekly wages below Rs.80 and (iv) the number of workers getting Rs.65 or more but less than Rs.85 as weekly wages.

### Solution:

| Weekly wages<br>(in Rs) | No. of<br>workers<br>(f) | Cumulative<br>frequency | Class Marks<br>(x) | fx     |
|-------------------------|--------------------------|-------------------------|--------------------|--------|
| 50-55                   | 5                        | 5                       | 52.5               | 262.5  |
| 55-60                   | 20                       | 25                      | 57.5               | 1150.0 |
| 60-65                   | 10                       | 35                      | 62.5               | 625.0  |
| 65-70                   | 10                       | 45                      | 67.5               | 675.0  |
| 70-75                   | 9                        | 54                      | 72.5               | 652.5  |
| 75-80                   | 6                        | 60                      | 77.5               | 465.0  |
| 80-85                   | 12                       | 72                      | 82.5               | 990.0  |
| 85-90                   | 8                        | 80                      | 87.5               | 700.0  |
| Total                   | 80                       |                         |                    | 5520.0 |

$$(i) \text{ Mean} = \frac{\sum fx}{\sum f} = \frac{5520}{80} = 69$$

(ii) Modal class = 55-60 as it has maximum frequencies.

(iii) Number of workers getting wages below Rs.80 = 60

(iv) Number of workers getting Rs.65 or more and less than Rs.85 = 72 - 35 = 37

**Question 3.**

Draw an ogive for the data given below and from the graph determine:

(i) the median marks

(ii) the number of students who obtained more than 75% marks

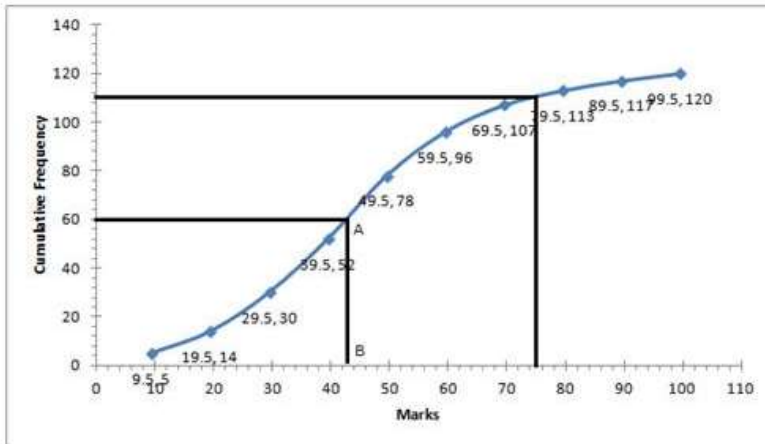
| Marks | No. of Students |
|-------|-----------------|
| 0-9   | 5               |
| 10-19 | 9               |
| 20-29 | 16              |
| 30-39 | 22              |
| 40-49 | 26              |
| 50-59 | 18              |
| 60-69 | 11              |
| 70-79 | 6               |
| 80-89 | 4               |
| 90-99 | 3               |

**Solution:**

| Marks     | No. of Students | Cumulative frequency |
|-----------|-----------------|----------------------|
| 0.5-9.5   | 5               | 5                    |
| 9.5-19.5  | 9               | 14                   |
| 19.5-29.5 | 16              | 30                   |
| 29.5-39.5 | 22              | 52                   |
| 39.5-49.5 | 26              | 78                   |
| 49.5-59.5 | 18              | 96                   |
| 59.5-69.5 | 11              | 107                  |
| 69.5-79.5 | 6               | 113                  |
| 79.5-89.5 | 4               | 117                  |
| 89.5-99.5 | 3               | 120                  |

Total number of terms = 120





(i)  $\therefore \text{Median} = \frac{120}{2} = 60^{\text{th}} \text{ term}$

Through mark 60, draw a parallel line to x-axis which meets the curve at A, From A draw a perpendicular to x-axis meeting it at B.  
The value of point B is the median = 43

(ii) Total marks = 100

75% of total marks =  $\frac{75}{100} \times 100 = 75$

The number of students getting more than 75% marks =  $120 - 111 = 9$

#### Question 4.

The mean of 1, 7, 5, 3, 4 and 4 is m. The numbers 3, 2, 4, 2, 3, 3 and p have mean m-1 and median q. Find p and q.

#### Solution:

Mean of 1, 7, 5, 3, 4 and 4 =  $\frac{24}{6} = 4$

$\Rightarrow m=4$

Now, mean of 3, 2, 4, 2, 3, 3 and p =  $m-1 = 4-1 = 3$

Therefore,  $17+p = 3 \times n$  .... Where  $n = 7$

$17+p = 21$

$p = 4$

Arranging in ascending order:

2, 2, 3, 3, 3, 3, 4

Mean =  $4^{\text{th}} \text{ term} = 3$

Therefore,  $q = 3$

**Question 5.**

The marks of 200 students in a test were recorded as follows:

| Marks | No. of students |
|-------|-----------------|
| 10-19 | 7               |
| 20-29 | 11              |
| 30-39 | 20              |
| 40-49 | 46              |
| 50-59 | 57              |
| 60-69 | 37              |
| 70-79 | 15              |
| 80-89 | 7               |

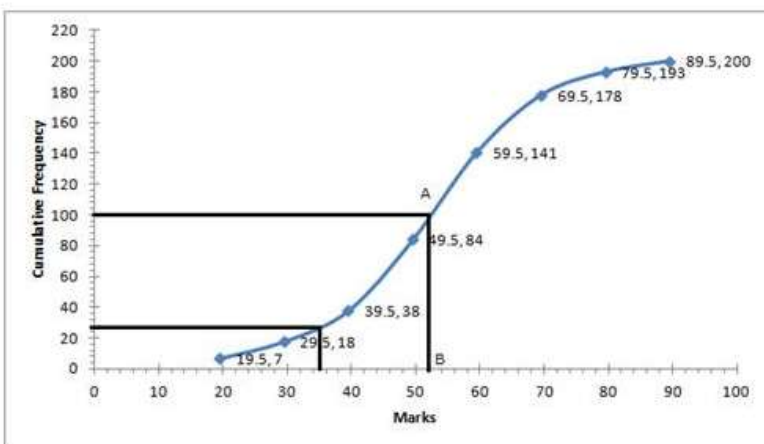
Construct the cumulative frequency table. Draw the ogive and use it to find:

- (i) the median and
- (ii) the number of students who score more than 35% marks.

**Solution:**

| Marks     | No. of students | Cumulative frequency |
|-----------|-----------------|----------------------|
| 9.5-19.5  | 7               | 7                    |
| 19.5-29.5 | 11              | 18                   |
| 29.5-39.5 | 20              | 38                   |
| 39.5-49.5 | 46              | 84                   |
| 49.5-59.5 | 57              | 141                  |
| 59.5-69.5 | 37              | 178                  |
| 69.5-79.5 | 15              | 193                  |
| 79.5-89.5 | 7               | 200                  |

Number of terms = 200



(i)  $\therefore \text{Median} = \frac{200}{2} = 100^{\text{th}} \text{ term}$

Through mark 100, draw a parallel line to x-axis which meets the curve at A, From A draw a perpendicular to x-axis meeting it at B.

The value of point B is the median = 52.5

(ii) Total marks = 100

35% of total marks =  $\frac{35}{100} \times 100 = 35$

The number of students who score more than 35% marks =  $200 - 28 = 172$

### Question 6.

The marks of 20 students in a test were as follows:

2, 6, 8, 9, 10, 11, 11, 12, 13, 13, 14, 14, 15, 15, 15, 16, 16, 18, 19 and 20.

Calculate:

(i) the mean (ii) the median (iii) the mode

### Solution:

Arranging the terms in ascending order:

2, 6, 8, 9, 10, 11, 11, 12, 13, 13, 14, 14, 15, 15, 15, 16, 16, 18, 19, 20

Number of terms = 20

$$\sum x = 2 + 6 + 8 + 9 + 10 + 11 + 11 + 12 + 13 + 13 + 14 + 14 + 15 + 15 + 15 + 16 + 16 + 18 + 19 + 20$$

$$= 257$$

(i) Mean =  $\frac{\sum x}{\sum n} = \frac{257}{20} = 12.85$

(ii) Median =  $\frac{10^{\text{th}} \text{ term} + 11^{\text{th}} \text{ term}}{2} = \frac{13 + 14}{2} = \frac{27}{2} = 13.5$

(iii) Mode = 15 as it has maximum frequencies i.e. 3

### Question 7.

The marks obtained by 120 students in a mathematics test is given below:

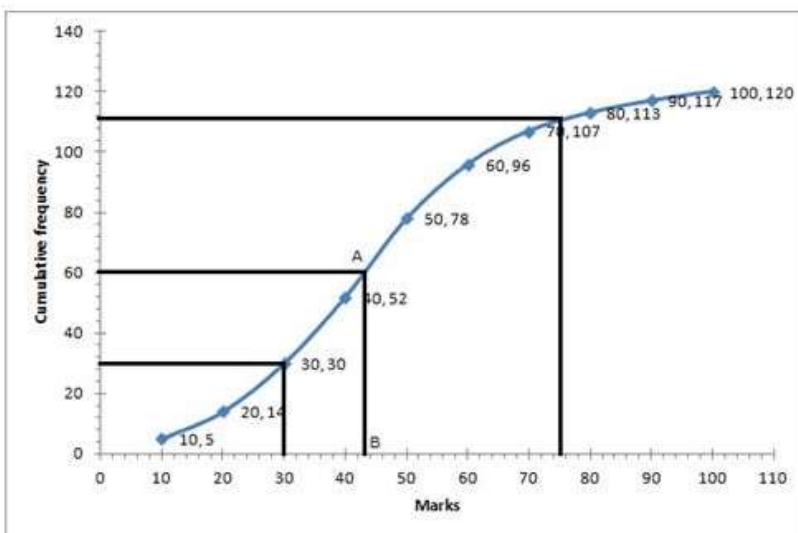
| Marks  | No. of students |
|--------|-----------------|
| 0-10   | 5               |
| 10-20  | 9               |
| 20-30  | 16              |
| 30-40  | 22              |
| 40-50  | 26              |
| 50-60  | 18              |
| 60-70  | 11              |
| 70-80  | 6               |
| 80-90  | 4               |
| 90-100 | 3               |

Draw an ogive for the given distribution on a graph sheet. Use a suitable scale for your ogive. Use your ogive to estimate:

- (i) the median
- (ii) the number of students who obtained more than 75% in test.
- (iii) the number of students who did not pass in the test if the pass percentage was 40.
- (iv) the lower quartile

**Solution:**

| Marks  | No. of students | c.f. |
|--------|-----------------|------|
| 0-10   | 5               | 5    |
| 10-20  | 9               | 14   |
| 20-30  | 16              | 30   |
| 30-40  | 22              | 52   |
| 40-50  | 26              | 78   |
| 50-60  | 18              | 96   |
| 60-70  | 11              | 107  |
| 70-80  | 6               | 113  |
| 80-90  | 4               | 117  |
| 90-100 | 3               | 120  |



(i) Median =  $\frac{120 + 1}{2} = 60.5^{\text{th}}$  term

Through mark 60.5, draw a parallel line to x-axis which meets the curve at A, From A draw a perpendicular to x-axis meeting it at B.

The value of point B is the median = 43

(ii) Number of students who obtained up to 75% marks in the test = 110

Number of students who obtained more than 75% marks in the test =  $120 - 110 = 10$

(iii) Number of students who obtained less than 40% marks in the test = 52 (from the graph;  $x=40$ ,  $y=52$ )

(iv) Lower quartile =  $Q_1 = 120 \times \frac{1}{4} = 30^{\text{th}}$  term = 30

### Question 8.

Using a graph paper, draw an ogive for the following distribution which shows a record of the weight in kilograms of 200 students.

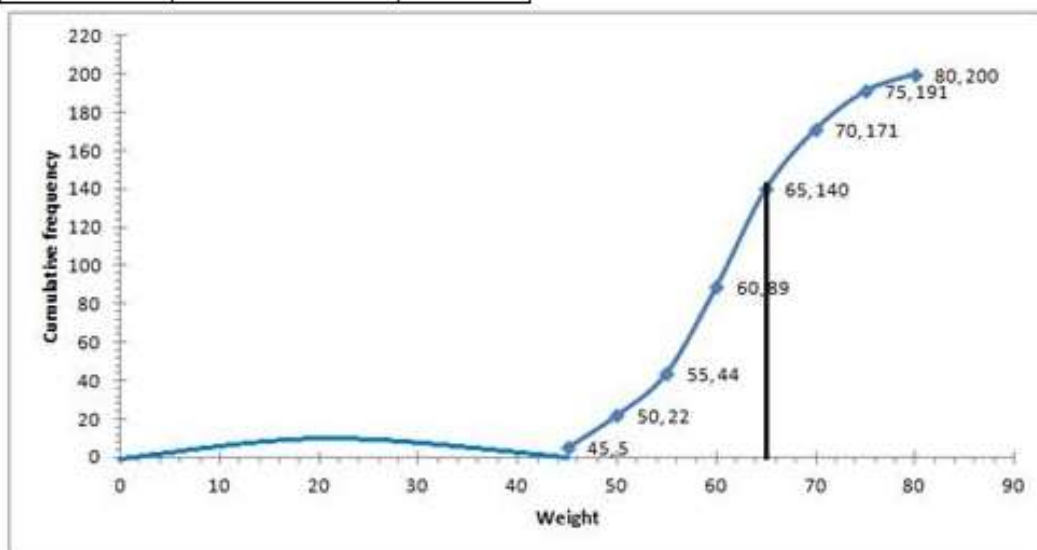
| Weight | Frequency |
|--------|-----------|
| 40-45  | 5         |
| 45-50  | 17        |
| 50-55  | 22        |
| 55-60  | 45        |
| 60-65  | 51        |
| 65-70  | 31        |
| 70-75  | 20        |
| 75-80  | 9         |

Use your ogive to estimate the following:

- (i) The percentage of students weighing 55 kg or more
  - (ii) The weight above which the heaviest 30% of the student fall
  - (iii) The number of students who are
    - (a) underweight
    - (b) overweight,
- if 55.70 kg is considered as standard weight.

**Solution:**

| Weight | Frequency | C. f. |
|--------|-----------|-------|
| 40-45  | 5         | 5     |
| 45-50  | 17        | 22    |
| 50-55  | 22        | 44    |
| 55-60  | 45        | 89    |
| 60-65  | 51        | 140   |
| 65-70  | 31        | 171   |
| 70-75  | 20        | 191   |
| 75-80  | 9         | 200   |



(i) Number of students weighing more than 55 kg =  $200 - 44 = 156$

Therefore, percentage of students weighing 55 kg or more

$$= \frac{156}{200} \times 100 = 78\%$$

$$(ii) 30\% \text{ of students} = \frac{30 \times 200}{100} = 60$$

Heaviest 60 students in weight =  $9 + 21 + 30 = 60$

weight = 65 kg (from table)

(iii) (a) underweight students when 55.70 kg is standard = 46 (approx) from graph

(b) overweight students when 55.70 kg is standard =  $200 - 55.70 = 154$  (approx) from graph

**Question 9.**

The distribution, given below, shows the marks obtained by 25 students in an aptitude test. Find the mean, median and mode of the distribution.

|                 |   |   |   |   |   |    |
|-----------------|---|---|---|---|---|----|
| Marks obtained  | 5 | 6 | 7 | 8 | 9 | 10 |
| No. of students | 3 | 9 | 6 | 4 | 2 | 1  |

**Solution:**

| Marks obtained(x) | No. of students (f) | c.f. | fx  |
|-------------------|---------------------|------|-----|
| 5                 | 3                   | 3    | 15  |
| 6                 | 9                   | 12   | 54  |
| 7                 | 6                   | 18   | 42  |
| 8                 | 4                   | 22   | 32  |
| 9                 | 2                   | 24   | 18  |
| 10                | 1                   | 25   | 10  |
| Total             | 25                  |      | 171 |

Number of terms = 25

$$(i) \text{ Mean} = \frac{171}{25} = 6.84$$

$$(ii) \text{ Median} = \frac{25 + 1^{\text{th}}}{2} \text{ term} = 13^{\text{th}} \text{ term} = 7$$

(iii) Mode = 6 as it has maximum frequencies i.e. 6

**Question 10.**

The mean of the following distribution is 52 and the frequency of class interval 30-40 is 'f'. Find f.

|      |       |       |       |       |       |       |       |
|------|-------|-------|-------|-------|-------|-------|-------|
| C.I  | 10-20 | 20-30 | 30-40 | 40-50 | 50-60 | 60-70 | 70-80 |
| Freq | 5     | 3     | f     | 7     | 2     | 6     | 13    |



**Solution:**

| C.I.  | Frequency(f) | Mid value (x) | fx       |
|-------|--------------|---------------|----------|
| 10-20 | 5            | 15            | 75       |
| 20-30 | 3            | 25            | 75       |
| 30-40 | f            | 35            | 35f      |
| 40-50 | 7            | 45            | 315      |
| 50-60 | 2            | 55            | 110      |
| 60-70 | 6            | 65            | 390      |
| 70-80 | 13           | 75            | 975      |
| Total | 36+f         |               | 1940+35f |

$$\text{Mean} = \frac{\sum fx}{\sum f} = \frac{1940 + 35f}{36 + f} \dots\dots(i)$$

$$\text{But, mean} = 52 \dots\dots(ii)$$

From (i) and (ii)

$$\frac{1940 + 35f}{36 + f} = 52$$

$$1940 + 35f = 1872 + 52f$$

$$17f = 68$$

$$f = 4$$

**Question 11.**

The monthly income of a group of 320 employees in a company is given below:

| Monthly Income (thousands) | No. of employees |
|----------------------------|------------------|
| 6-7                        | 20               |
| 7-8                        | 45               |
| 8-9                        | 65               |
| 9-10                       | 95               |
| 10-11                      | 60               |
| 11-12                      | 30               |
| 12-13                      | 5                |

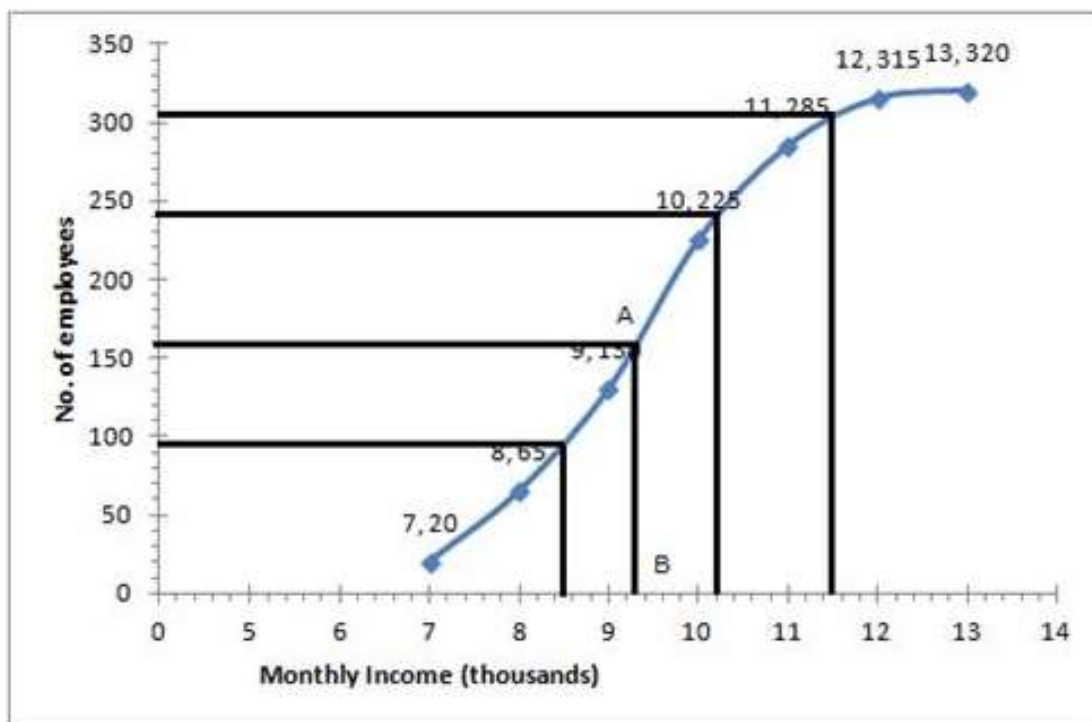
Draw an ogive of the given distribution on a graph paper taking 2 cm = Rs 1000 on one axis and 2 cm = 50 employees on the other axis. From the graph determine :

- the median wage.
- number of employees whose income is below Rs 8500.
- If salary of a senior employee is above Rs 11,500, find the number of senior employees in the company.
- the upper quartile.

**Solution:**

| Monthly Income (thousands) | No. of employees (f) | Cumulative frequency |
|----------------------------|----------------------|----------------------|
| 6-7                        | 20                   | 20                   |
| 7-8                        | 45                   | 65                   |
| 8-9                        | 65                   | 130                  |
| 9-10                       | 95                   | 225                  |
| 10-11                      | 60                   | 285                  |
| 11-12                      | 30                   | 315                  |
| 12-13                      | 5                    | 320                  |
| Total                      | 320                  |                      |

Number of employees = 320



(i) Median =  $\frac{320}{2} = 160^{\text{th}}$  term

Through mark 160, draw a parallel line to x-axis which meets the curve at A, From A draw a perpendicular to x-axis meeting it at B.

The value of point B is the median = Rs 9.3 thousands

(ii) The number of employees with income below Rs 8500 = 95 (approx from the graph)

(iii) Number of employees with income below Rs 11500 = 305 (approx from the graph)

Therefore number of employees (senior employees) = 320-305 = 15

(iv) Upper quartile =  $Q_3 = 320 \times \frac{3}{4} = 240^{\text{th}}$  term = 10.3 thousands = Rs. 10,300

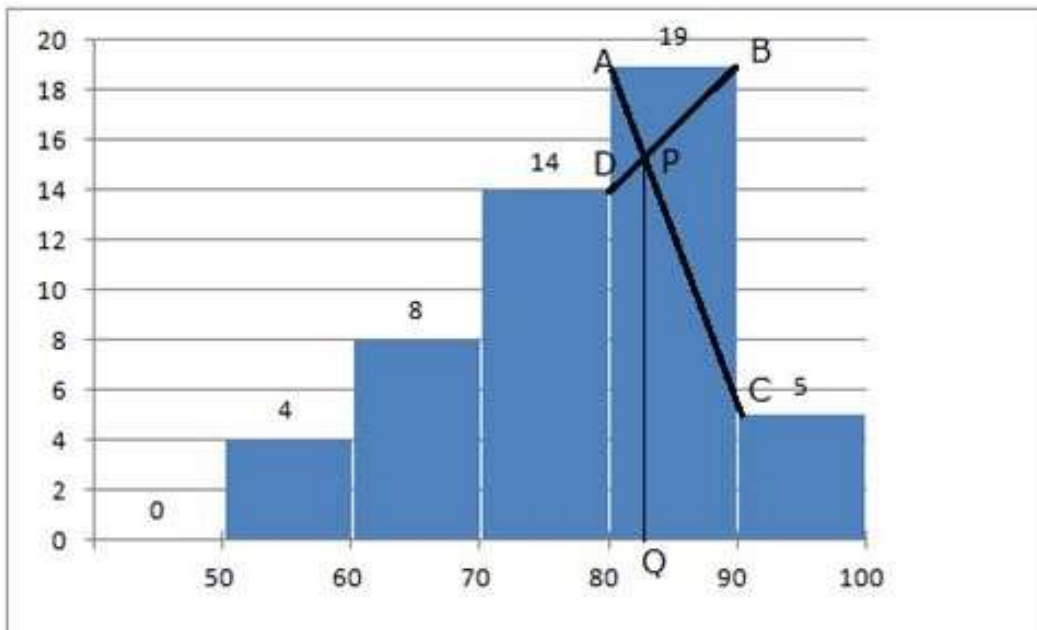
### Question 12.

A mathematics aptitude test of 50 students was recorded as follows:

| Marks  | No. of students |
|--------|-----------------|
| 50-60  | 4               |
| 60-70  | 8               |
| 70-80  | 14              |
| 80-90  | 19              |
| 90-100 | 5               |

Draw a histogram for the above data using a graph paper and locate the mode.

**Solution:**



- (i) Draw the histogram
- (ii) In the highest rectangle which represents modal class draw two lines AC and BD intersecting at P.
- (iii) From P, draw a perpendicular to x-axis meeting at Q.
- (iv) Value of Q is the mode = 82 (approx)

### Question 13.

Marks obtained by 200 students in an examination are given below:

| Marks  | No. of students |
|--------|-----------------|
| 0-10   | 5               |
| 10-20  | 11              |
| 20-30  | 10              |
| 30-40  | 20              |
| 40-50  | 28              |
| 50-60  | 37              |
| 60-70  | 40              |
| 70-80  | 29              |
| 80-90  | 14              |
| 90-100 | 6               |

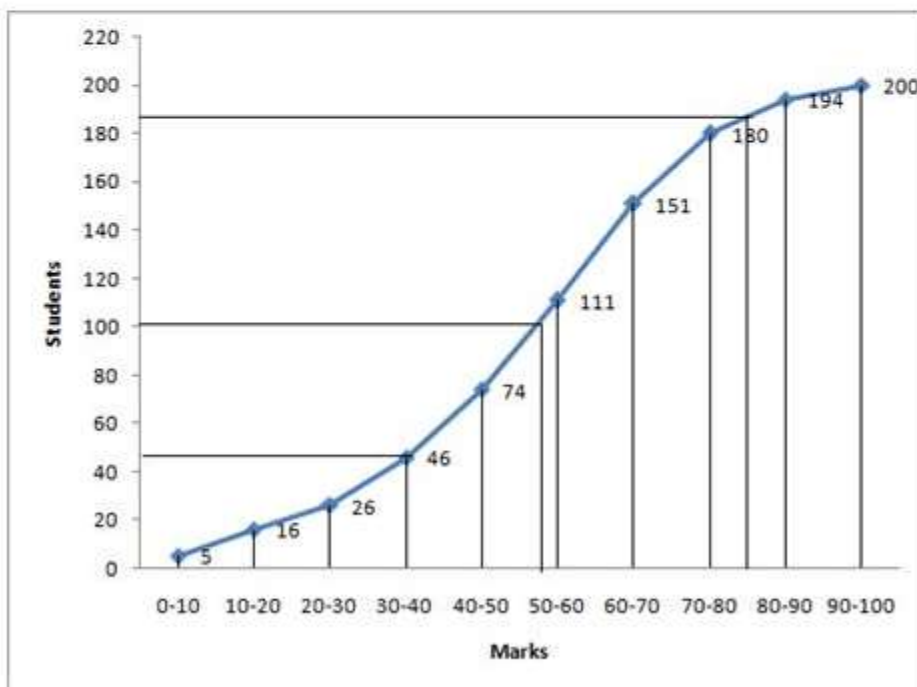
Draw an ogive of the given distribution on a graph paper taking 2 cm = 10 marks on one axis and 2 cm = 20 students on the other axis. Using the graph:

- (i) the median wage.
- (ii) number of students who failed if minimum marks required to pass is 40
- (iii) if scoring 85 and more marks is considered as grade one, find the number of students who secured grade one in the examination.

**Solution:**

| Marks  | No. of students | Cumulative frequency |
|--------|-----------------|----------------------|
| 0-10   | 5               | 5                    |
| 10-20  | 11              | 16                   |
| 20-30  | 10              | 26                   |
| 30-40  | 20              | 46                   |
| 40-50  | 28              | 74                   |
| 50-60  | 37              | 111                  |
| 60-70  | 40              | 151                  |
| 70-80  | 29              | 180                  |
| 80-90  | 14              | 194                  |
| 90-100 | 6               | 200                  |

Number of students = 200



(i) Median =  $\frac{200}{2} = 100^{\text{th}}$  term

Through mark 100, draw a parallel line to x-axis which meets the curve at A, From A draw a perpendicular to x-axis meeting it at B.

The value of point B is the median = 57 marks (approx)

(ii) The number of students who failed (if minimum marks required to pass is 40) = 46 (approx from the graph)

(iii) The number of students who secured grade one in the examination =  $200 - 188 = 12$  (approx from the graph)

**Question 14.**

The marks obtained by 40 students in a short assessment is given below, where a and b are two missing data.

|                    |   |   |    |    |   |
|--------------------|---|---|----|----|---|
| Marks              | 5 | 6 | 7  | 8  | 9 |
| Number of Students | 6 | a | 16 | 13 | b |

If mean of the distribution is 7.2, find a and b.

**Solution:**

$$\begin{aligned}\text{Mean} &= \frac{\sum fx}{\sum f} \\ \Rightarrow 7.2 &= \frac{6 \times 5 + a \times 6 + 16 \times 7 + 13 \times 8 + b \times 9}{6 + a + 16 + 13 + b} \\ \Rightarrow 7.2 &= \frac{246 + 6a + 9b}{35 + a + b} \\ \Rightarrow 1.2a - 1.8b &= -6 \dots\dots\dots(i)\end{aligned}$$

$$\begin{aligned}\text{Total number of students} &= 6 + a + 16 + 13 + b \\ \Rightarrow 40 &= 35 + a + b \\ \Rightarrow a + b &= 5 \dots\dots\dots(ii)\end{aligned}$$

Multiply equation(ii) by 1.8 and add it to equation (i)

$$\begin{aligned}1.8a + 1.8b &= 9 \\ \underline{1.2a - 1.8b} &= \underline{-6} \\ 3a &= 3 \\ \Rightarrow a &= 1\end{aligned}$$

$$\begin{aligned}\text{Substituting } a = 1 \text{ in equation (ii) we get,} \\ 1 + b &= 5 \\ \Rightarrow b &= 4\end{aligned}$$

**Question 15.**

Find the mode and the median of the following frequency distribution.

|   |    |    |    |    |    |    |
|---|----|----|----|----|----|----|
| x | 10 | 11 | 12 | 13 | 14 | 15 |
| f | 1  | 4  | 7  | 5  | 9  | 3  |

**Solution:**

Since the frequency for  $x = 14$  is maximum.

So Mode = 14.

| x      | f | Cumulative frequency |
|--------|---|----------------------|
| 10     | 1 | 1                    |
| 11     | 4 | 5                    |
| 12     | 7 | 12                   |
| 13     | 5 | 17                   |
| 14     | 9 | 26                   |
| 15     | 3 | 29                   |
| N = 29 |   |                      |

$$\begin{aligned}
 \text{Median} &= \left( \frac{n+1}{2} \right)^{\text{th}} \text{ term} \\
 &= \left( \frac{30}{2} \right)^{\text{th}} \text{ term} \\
 &= 15^{\text{th}} \text{ term} \\
 &= \text{frequency of the } 15^{\text{th}} \text{ term}
 \end{aligned}$$

According to the table it can be observed that the value of  $x$  from the 13<sup>th</sup> term to the 17<sup>th</sup> term is 13.

So the median = 13.

**Question 16.**

The median of the observations 11, 12, 14,  $(x - 2)$ ,  $(x + 4)$ ,  $(x + 9)$ , 32, 38, 47 arranged in ascending order is 24. Find the value of  $x$  and hence find the mean.

**Solution:**

Data in ascending order:

11, 12, 14,  $(x - 2)$ ,  $(x + 4)$ ,  $(x + 9)$ , 32, 38, 47

Total number of observations =  $n = 9$  (odd)

$$\Rightarrow \text{Median} = \left( \frac{n+1}{2} \right)^{\text{th}} \text{ term} = \left( \frac{9+1}{2} \right)^{\text{th}} \text{ term} = 5^{\text{th}} \text{ term}$$

Given, median = 24

$$\Rightarrow 5^{\text{th}} \text{ term} = 24$$

$$\Rightarrow x + 4 = 24$$

$$\Rightarrow x = 20$$

Thus, the observation are as follows:

11, 12, 14, 18, 24, 29, 32, 38, 47

$$\therefore \text{Mean} = \frac{\sum x}{n} = \frac{11+12+14+18+24+29+32+38+47}{9} = \frac{225}{9} = 25$$

### Question 17.

The number 6, 8, 10, 12, 13 and x are arranged in an ascending order. If the mean of the observations is equal to the median, find the value of x.

### Solution:

Data in ascending order: 6, 8, 10, 12, 13 and x

Total number of observations = n = 6 (even)

$$\therefore \text{Mean} = \frac{\sum x}{n} = \frac{6+8+10+12+13+x}{6} = \frac{49+x}{6}$$

$$\text{Median} = \frac{\left(\frac{n}{2}\right)^{\text{th}} \text{ term} + \left(\frac{n}{2} + 1\right)^{\text{th}} \text{ term}}{2} = \frac{3^{\text{rd}} \text{ term} + 4^{\text{th}} \text{ term}}{2} = \frac{10+12}{2} = \frac{22}{2} = 11$$

Given,

Mean = Median

$$\Rightarrow \frac{49+x}{6} = 11$$

$$\Rightarrow 49+x = 66$$

$$\Rightarrow x = 17$$

### Question 18.

(Use a graph paper for this question). The daily pocket expenses of 200 students in a school are given below :

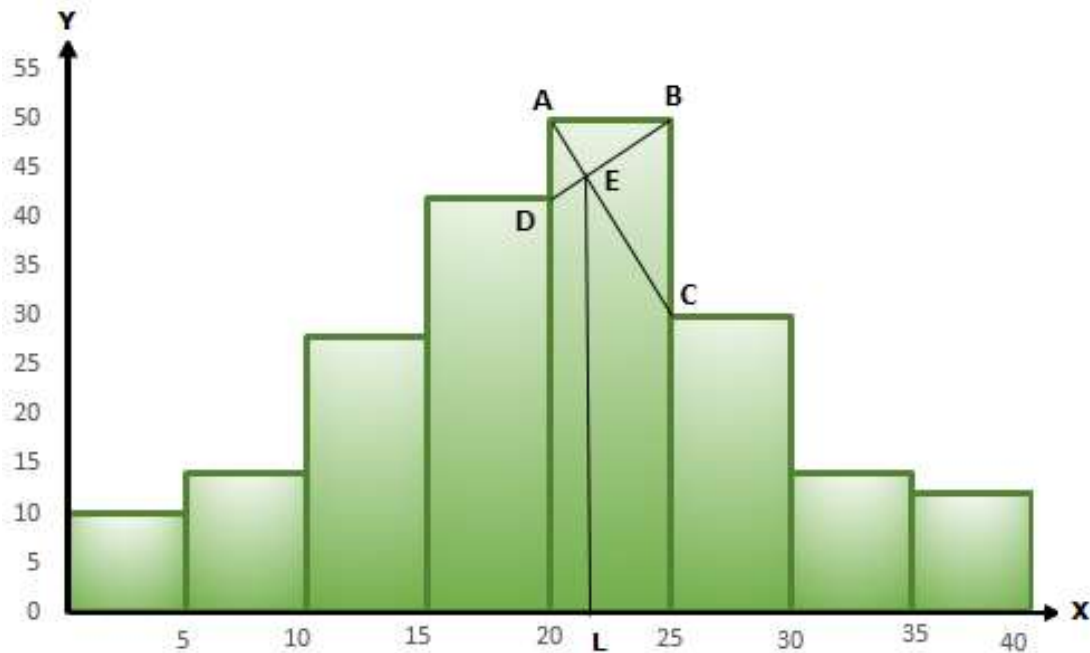
| Pocket expenses (in Rs)     | 0-5 | 5-10 | 10-15 | 15-20 | 20-25 | 25-30 | 30-35 | 35-40 |
|-----------------------------|-----|------|-------|-------|-------|-------|-------|-------|
| No. of students (frequency) | 10  | 14   | 28    | 42    | 50    | 30    | 14    | 12    |

Draw a histogram representing the above distribution and estimate the mode from the graph.

### Solution:

Histogram is as follows:





In the highest rectangle which represents modal class draw two lines AC and BD intersecting at E.

From E, draw a perpendicular to x-axis meeting at L.  
Value of L is the mode. Hence, mode = 21.5

### Question 19.

The marks obtained by 100 students in a mathematics test are given below :

| Marks           | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 | 50-60 | 60-70 | 70-80 | 80-90 | 90-100 |
|-----------------|------|-------|-------|-------|-------|-------|-------|-------|-------|--------|
| No. of students | 3    | 7     | 12    | 17    | 23    | 14    | 9     | 6     | 5     | 4      |

Draw an ogive for the given distribution on a graph sheet.

Use a scale of 2 cm = 10 units on both the axes.

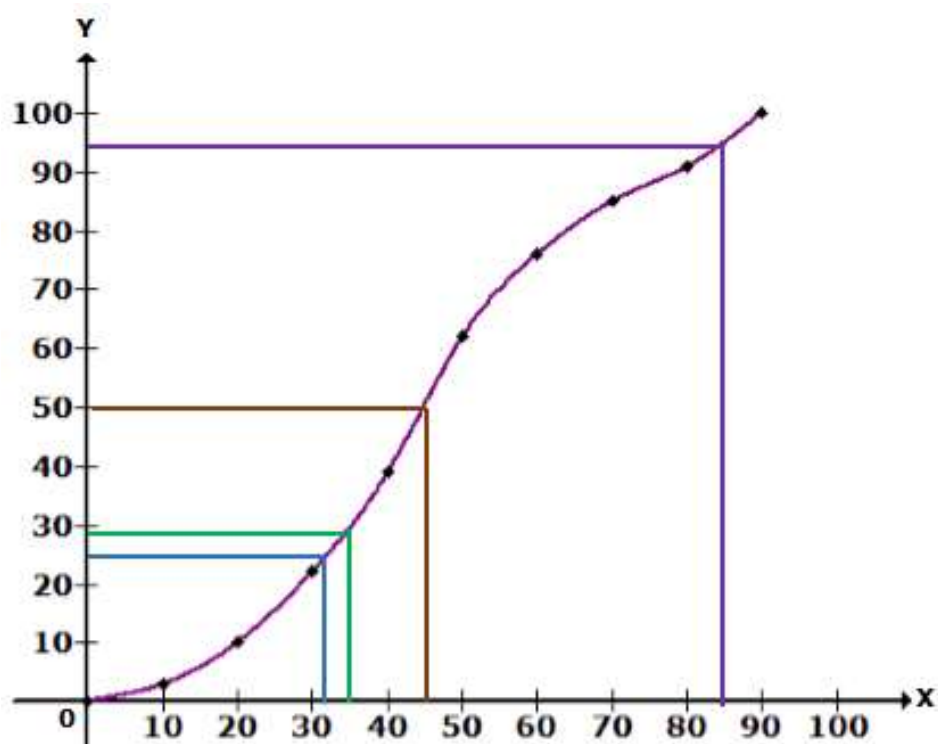
Use the ogive to estimate :

- Median
- Lower quartile
- Number of students who obtained more than 85% marks in the test.
- Number of students failed, if the pass percentage was 35.

**Solution:**

| Marks  | Number of students<br>(Frequency) | Cumulative Frequency |
|--------|-----------------------------------|----------------------|
| 0-10   | 3                                 | 3                    |
| 10-20  | 7                                 | 10                   |
| 20-30  | 12                                | 22                   |
| 30-40  | 17                                | 39                   |
| 40-50  | 23                                | 62                   |
| 50-60  | 14                                | 76                   |
| 60-70  | 9                                 | 85                   |
| 70-80  | 6                                 | 91                   |
| 80-90  | 5                                 | 96                   |
| 90-100 | 4                                 | 100                  |

The ogive is as follows:



$$(i) \text{ Median} = \left(\frac{N}{2}\right)^{\text{th}} \text{ term} = \left(\frac{100}{2}\right)^{\text{th}} \text{ term} = 50^{\text{th}} \text{ term} = 45$$

$$(ii) \text{ Lower quartile} = \left(\frac{N}{4}\right)^{\text{th}} \text{ term} = \left(\frac{100}{4}\right)^{\text{th}} \text{ term} = 25^{\text{th}} \text{ term} = 32$$

$$(iii) \text{ Number of students who obtained more than 85\% marks} \\ = 100 - 94 \\ = 6$$

$$(iv) \text{ Number of students who failed} \\ = 29 \\ = 6$$

### Question 20.

The mean of following numbers is 68. Find the value of 'x'.

45, 52, 60, x, 69, 70, 26, 81 and 94.

Hence, estimate the median.

### Solution:

$$\text{Mean} = \frac{\text{Sum of all observations}}{\text{Total number of observations}}$$

$$\therefore 68 = \frac{45 + 52 + 60 + x + 69 + 70 + 26 + 81 + 94}{9}$$

$$\Rightarrow 68 = \frac{497 + x}{9}$$

$$\Rightarrow 612 = 497 + x$$

$$\Rightarrow x = 612 - 497$$

$$\Rightarrow x = 115$$

Data in ascending order

26, 45, 52, 60, 69, 70, 81, 94, 115

Since the number of observations is odd, the median is the  $\left(\frac{n+1}{2}\right)^{\text{th}}$  observation.

$$\Rightarrow \text{Median} = \left(\frac{9+1}{2}\right)^{\text{th}} \text{ observation} = 5^{\text{th}} \text{ observation}$$

Hence, the median is 69.

**Question 21.**

The marks of 10 students of a class in an examination arranged in ascending order is as follows:

13, 35, 43, 46, x, x + 4, 55, 61, 71, 80

If the median marks is 48, find the value of x. Hence, find the mode of the given data.

**Solution:**

Here the number of observations i. e is 10, which is even.'

$$\begin{aligned}\therefore \text{Median} &= \frac{\left(\frac{n}{2}\right)^{\text{th}} \text{ term} + \left(\frac{n}{2} + 1\right)^{\text{th}} \text{ term}}{2} \\ \therefore 48 &= \frac{\left(\frac{10}{2}\right)^{\text{th}} \text{ term} + \left(\frac{10}{2} + 1\right)^{\text{th}} \text{ term}}{2} \\ \therefore 48 &= \frac{5^{\text{th}} \text{ term} + 6^{\text{th}} \text{ term}}{2} \\ \therefore 48 &= \frac{x + x + 4}{2} \\ \therefore 96 &= 2x + 4 \\ \therefore 92 &= 2x \\ \therefore x &= 46\end{aligned}$$

So, the given data is 13, 35, 43, 46, 46, 50, 55, 61, 71, 80.

In the given data, 46 occurs most frequently.

$\therefore$  Mode = 46

**Question 22.**

The daily wages of 80 workers in a project are given below.

| Wages         | 400- 450 | 450-500 | 500- 550 | 550-600 | 600-650 | 650-700 | 700-750 |
|---------------|----------|---------|----------|---------|---------|---------|---------|
| No.of workers | 2        | 6       | 12       | 18      | 24      | 13      | 5       |

Use a graph paper to draw an ogive for the above distribution. (Use a scale of 2 cm = Rs. 50 on x – axis and 2 cm = 10 workers on y – axis). Use your ogive to estimate.

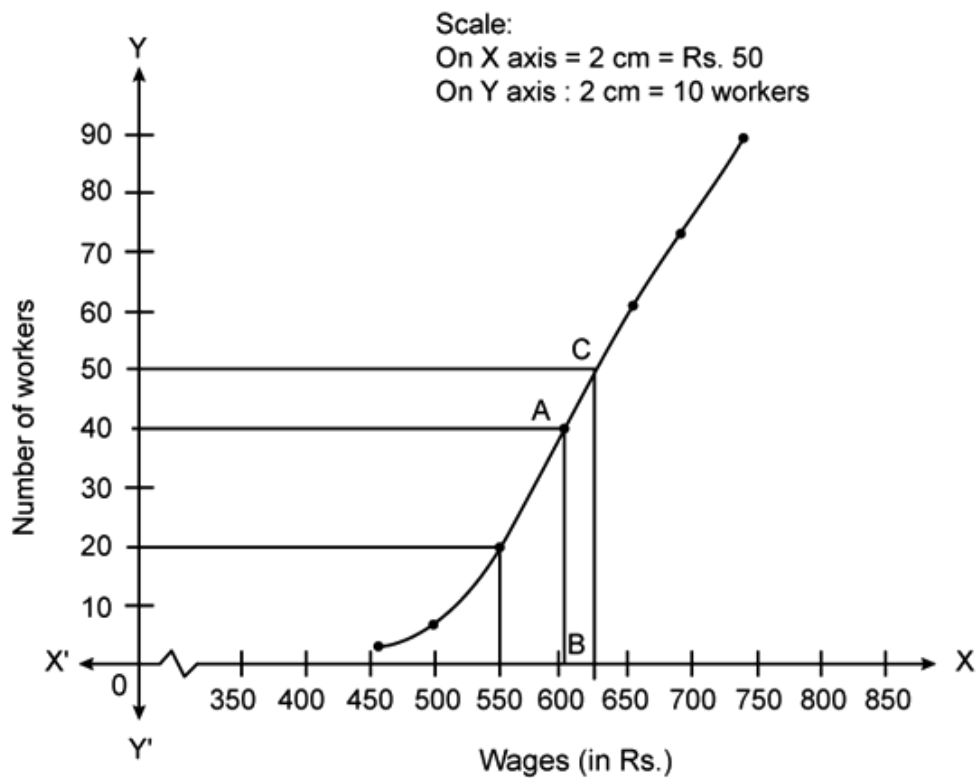
- the median wages of the workers.
- The lower quartile wage of workers.
- the number of workers who earn more than Rs. 625 daily.

**Solution:**

The cumulative frequency table of the given distribution is as follows:

| Wages (Rs.) | Upper limit | No. of workers | C.f. |
|-------------|-------------|----------------|------|
| 400-450     | 450         | 2              | 2    |
| 450-500     | 500         | 6              | 8    |
| 500-550     | 550         | 12             | 20   |
| 550-600     | 600         | 18             | 38   |
| 600-650     | 650         | 24             | 62   |
| 650-700     | 700         | 13             | 75   |
| 700-750     | 750         | 5              | 80   |

The ogive is as follows:



Number of workers =  $n = 80$

1) Median =  $\left(\frac{n}{2}\right)^{\text{th}}$  term =  $40^{\text{th}}$  term, draw a horizontal line which meets the curve at point A.

Draw vertical line parallel to y axis from A to meet x axis at B.

The value of point B is 605.

2) Lower quartile ( $Q_1$ ) =  $\left(\frac{n}{4}\right)^{\text{th}}$  term =  $20^{\text{th}}$  term = 550

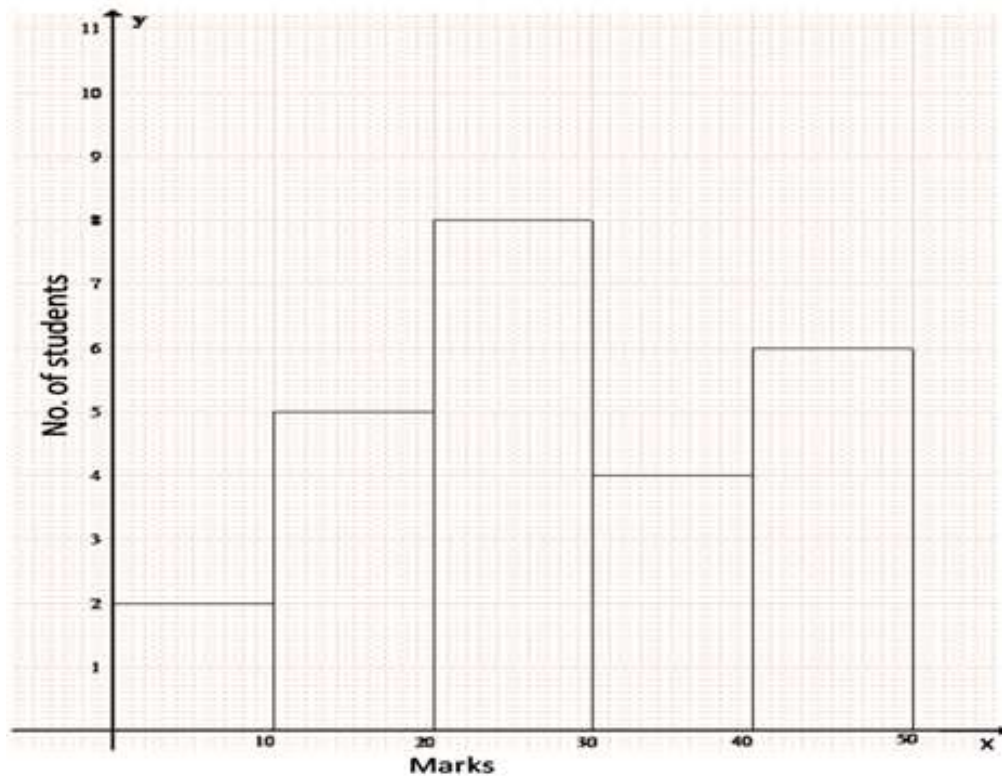
3) Through mark of point 625 on x axis draw a vertical line which meets the graph at point C. Then through point C, draw a horizontal line which meets the y axis at the mark of 50.

Thus, the number of workers that earn more than Rs. 625 daily =  $80 - 50 = 30$

### Question 23.

The histogram below represents the scores obtained by 25 students in a Mathematics mental test. Use the data to:

- Frame a frequency distribution table.
- To calculate mean.
- To determine the Modal class.



**Solution:**

i. The frequency distribution table is as follows:

| Class interval | Frequency |
|----------------|-----------|
| 0-10           | 2         |
| 10- 20         | 5         |
| 20-30          | 8         |
| 30-40          | 4         |
| 40-50          | 6         |

ii.

| Class interval | Frequency<br>(f) | Mean value (x) | fx       |
|----------------|------------------|----------------|----------|
| 0-10           | 2                | 5              | 10       |
| 10- 20         | 5                | 15             | 75       |
| 20-30          | 8                | 25             | 200      |
| 30-40          | 4                | 35             | 140      |
| 40-50          | 6                | 45             | 270      |
|                | Sf = 25          |                | Sf = 695 |

$$\therefore \text{Mean} = \frac{\sum fx}{\sum f} = \frac{695}{25} = 27.8$$

iii. Here the maximum frequency is 8 which is corresponding to class 20 - 30.  
Hence, the modal class is 20 - 30.