Determinants **Part - 2**



ASSERTION AND REASON BASED MCQs

(1 Mark each)

Directions: In the following questions, A statement of Assertion (A) is followed by a statement of Reason (R). Mark the correct choice as.

- (A) Both A and R are true and R is the correct explanation of A
- (B) Both A and R are true but R is NOT the correct explanation of A
- (C) A is true but R is false
- (D) A is false and R is True
- **Q.** 1. Let A be a 2×2 matrix.

Assertion (A): adj (adj A) = A

Reason (R): |adj A| = |A|

Ans. Option (B) is correct.

Explanation:

$$adj (adj A) = |A|^{n-2} A$$

anation:

$$adj (adj A) = |A|^{n-2} A$$

 $n = 2 \Rightarrow adj (adj A) = A$

Hence A is true.

$$|adj A| = |A|^{n-1}$$

 $n = 2 \Rightarrow |adj A| = |A|$

Hence R is true.

R is not the correct explanation for A.

Q. 2. Assertion (A): If $A = \begin{bmatrix} 2 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 4 \end{bmatrix}$, then

$$A^{-1} = \begin{bmatrix} \frac{1}{2} & 0 & 0 \\ 0 & \frac{1}{3} & 0 \\ 0 & 0 & \frac{1}{4} \end{bmatrix}$$

Reason (R): The inverse of an invertible diagonal matrix is a diagonal matrix.

Ans. Option (B) is correct.

Explanation:

$$|A| = 24$$

$$Adj A = \begin{bmatrix} 12 & 0 & 0 \\ 0 & 8 & 0 \\ 0 & 0 & 6 \end{bmatrix}$$

$$A^{-1} = \frac{1}{|A|} (adj A) = \begin{bmatrix} \frac{1}{2} & 0 & 0 \\ 0 & \frac{1}{3} & 0 \\ 0 & 0 & \frac{1}{4} \end{bmatrix}$$

Hence A is true.

A is a diagonal matrix and its inverse is also a diagonal matrix. Hence R is true.

But R is not the correct explanation of A.

Q. 3. Assertion (A): If every element of a third order determinant of value Δ is multiplied by 5, then the value of the new determinant is 125Δ .

Reason (R): If k is a scalar and A is an $n \times n$ matrix, then $|kA| = k^n |A|$

Ans. Option (A) is correct.

Explanation: If k is a scalar and A is an $n \times n$ matrix, then $|kA| = k^n |A|$.

This is a property of the determinant. Hence R is true.

Using this property, $|5\Delta| = 5^3 \Delta = 125\Delta$ Hence A is true.

R is the correct explanation of A.

Q. 4. Assertion (A): If the matrix
$$A = \begin{bmatrix} 1 & 3 & \lambda + 2 \\ 2 & 4 & 8 \\ 3 & 5 & 10 \end{bmatrix}$$
 is singular, then $\lambda = 4$.

Reason (R): If A is a singular matrix, then |A| = 0.

Ans. Option (A) is correct.

Explanation: A matrix is said to be singular if

Hence R is true.

$$\begin{bmatrix} 1 & 3 & \lambda + 2 \\ 2 & 4 & 8 \\ 3 & 5 & 10 \end{bmatrix} = 0$$

$$\Rightarrow$$
 1(40 - 40) - 3(20 - 24) +

$$(\lambda + 2)(10 - 12) = 0$$

$$0 + 12 - 2\lambda - 4 = 0$$

Hence A is true.

R is the correct explanation for A.

Q. 5. Given
$$A = \begin{bmatrix} 2 & -3 \\ -4 & 7 \end{bmatrix}$$
.

Assertion (A): $2A^{-1} = 9I - A$

Reason (R): $A^{-1} = \frac{1}{|A|} (adj A)$

Ans. Option (A) is correct.

Explanation:
$$A^{-1} = \frac{1}{|A|} (adj A)$$
 is true.

Hence R is true

$$|A| = 2$$
,

$$A^{-1} = \frac{1}{2} \begin{bmatrix} 7 & 3 \\ 4 & 2 \end{bmatrix}$$

$$LHS = 2A^{-1} = \begin{bmatrix} 7 & 3 \\ 4 & 2 \end{bmatrix},$$

$$RHS = 9 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} - \begin{bmatrix} 2 & -3 \\ -4 & 7 \end{bmatrix}$$

$$= \begin{bmatrix} 7 & 3 \\ 4 & 2 \end{bmatrix}$$

$$\therefore 2A^{-1} = 9I - A \text{ is true.}$$

R is the correct explanation for A.

Q. 6. Assertion (A): If
$$A = \begin{bmatrix} 2 & 3 \\ 5 & -2 \end{bmatrix}$$
 and $A^{-1} = kA$, then $k = \frac{1}{9}$

Reason (R):
$$|A^{-1}| = \frac{1}{|A|}$$

Ans. Option (D) is correct.

Explanation:

$$|A| = -4 - 15$$

$$= -19$$

$$A^{-1} = \frac{-1}{19} \begin{bmatrix} -2 & -3 \\ -5 & 2 \end{bmatrix}$$

$$\Rightarrow \frac{-1}{19} \begin{bmatrix} -2 & -3 \\ -5 & 2 \end{bmatrix} = \begin{bmatrix} 2k & 3k \\ 5k & -2k \end{bmatrix}$$

$$\Rightarrow k = \frac{1}{10}$$

A is false

$$\left|A^{-1}\right| = \frac{1}{|A|}$$
 is true.

R is true.