# Factorisation



The factors 2,3, x and (x + 2) are irreducible factors of 6x (x + 2).

# Method of Factorisation

Name	Working
Common factor method	<ol> <li>We can look at each of the term in the algebraic expression, factorize each term</li> <li>Then find common factors to factorize the expression</li> <li>Example</li> <li>2x+4</li> <li>=2(x+2)</li> </ol>
Factorisation by regrouping terms	1) First we see common factor across all the terms 2) we look at grouping the terms and check if we find binomial factor from both the groups. 3) Take the common Binomial factor out <b>Example</b> 2xy + 3x + 2y + 3 $= 2 \times x \times y + 3 \times x + 2 \times y + 3$ $= x \times (2y + 3) + 1 \times (2y + 3)$ = (2y + 3) (x + 1)
Factorisation using identities	Use the below identities to factorise it $(a + b)^2 = a^2 + 2ab + b^2$ $(a - b)^2 = a^2 - 2ab + b^2$ $(a + b) (a - b) = a^2 - b^2$

Factorisation of the form (x+a)(x+b)	Given x <sup>2</sup> + px + q,
	1) we find two factors a and b of q (i.e., the constant term) such that ab = q  and  a + b = p 2) Now expression can be written $x^2 + (a + b) x + ab$ or $x^2 + ax + bx + ab$ or $x(x + a) + b(x + a)$ or $(x + a) (x + b)$ which are the required factors. <b>Example</b> $x^2 - 7x + 12$ Now $12 = 3 \times 4$ and $3 + 4 = 7$ $=x^2 - 3x - 4x + 12$ = x (x - 3) - 4 (x - 3) = (x - 3) (x - 4)

## **Division of algebraic expression**

Division of algebraic expression is performed by Factorisation of both the numerator and denominator and then cancelling the common factors.

#### **Steps of Division**

1) Identify the Numerator and denominator

2) Factorise both the Numerator and denominator by the technique of Factorisation using common factor, regrouping, identities and splitting

3) Identify the common factor between numerator and denominator

4) Cancel the common factors and finalize the result

### Example

 $48 (x^{2}yz + xy^{2}z + xyz^{2}) / 4xyz$ =48xyz (x + y + z)/4xyz = 4 ×12×xyz (x + y + z) / 4xyz = 12 (x + y + z)

Here Dividend=48  $(x^2yz + xy^2z + xyz^2)$ Divisor=4xyz Quotient=12 (x + y + z)

So, we have Dividend = Divisor × Quotient. In general, however, the relation is Dividend = Divisor × Quotient + Remainder When reminder is not zero