

Decimal Fractions (Decimals)

POINTS TO REMEMBER

1. Decimal fraction (or a decimal number)

A decimal fraction is a fraction whose denominator is 10 or a higher power of 10. In order to express a given decimal fraction in shorter form, the denominator is not written but its absence is shown by a dot which is called a decimal point inserted in a proper place.

Note :

(i) When there is no number is the left of the decimal point, generally, a zero is written.

(ii) Generally, a decimal fraction has two parts, the first part which is on the right of the decimal point is called decimal part and the part on the left side of the decimal point, is called integral part.

(iii) The decimal part is always less than 1.

2. Reading Decimal Numbers

The integral part is read according to its value and the decimal part is read by naming each digit, in order, separately

3. Converting a decimal number into a vulgar fraction :

Remove the decimal point from the decimal number and write in its denominator with as many zeros as the number of digits are in the decimal parts to the right of 1.

In the decimal number, the name of each place is given as under is the place value chart:

Thousands	Hundreds	Tens	Units	•	Tenths	Hundredths	Thousandth
				Decimal point			and so on

4. Converting a given fraction in to a decimal fraction :

(a) When the denominator in given fraction is 10, 100, 1000 etc., then count from extreme right to left, mark decimal point after as many digits of the numerator as there are zeroes in the denominator.

(b) When the denominator of the given number is other than 10 or higher power of 10, then divide in an ordinary way and mark the decimal point in the quotient just after the division of unit digit is completed. After this, any number of zeroes can be borrowed to complete the division.

Note : The number of figures that follow the decimal part is called the number of decimal places.

5. **Addition and Subtraction of decimal numbers.**

(a) Addition : Write the given decimal numbers in such a way, that the decimal points of all the numbers fall in the same vertical line. Digits with the same place value are placed one below the other (units are written below units, tens below tens and so on).

Addition is started from the right side, as done in the usual addition (empty places may be filled up by zeroes). In the result (total), the decimal point is placed under decimal points of the numbers added.

(b) Subtraction : In subtraction also, the numbers are written in such a way that their decimals are in the same vertical line. Digits with the same place value are placed one below the other (empty places may be filled by zeroes).

Subtraction is started from the right side, as in the case of normal subtraction. In the result, decimal point is placed just under the other decimal points.

6. **Multiplication of decimal numbers :**

(1) Multiplication by 10, 100, 1000 etc. shift the decimal point, in the multiplicand, to the right by as many digits as there are zeroes in the multiplier.

(2) Multiplication by a whole number : Multiply in an ordinary way, without considering the decimal point. In the product, the decimal point should be fixed by counting as many digits from the right as there are decimal places in the multiplicand.

Thus, (i) $0.3 \times 6 = 1.8$ (ii) $0.26 \times 18 = 4.68$ and so on.

(3) Multiplication of a decimal number by another decimal number :

Multiply the two numbers in a normal way, ignoring their decimals. In the product, decimal point is fixed counting from right, the digits equal to the sum of decimal places in the multiplicand and the multiplier.

Thus, $32.5 \times (0.07) = 2.275$

Since, the multiplicand (32.5) has one decimal place and multiplier (0.07) has two decimal places, their product will have $1+2 = 3$ decimal places.

7. **Division of decimal numbers :**

(1) Division by 10, 100, 1000 etc : Shift the decimal points to the left as many digits as there are zeroes in the divisor. .

(2) Division by a whole number : Divide in the normal manner, ignoring the decimal, and mark the decimal point; in the quotient, while just crossing over the decimal point in the dividend.

8. **Recurring Decimals :**

On performing a division, sometimes we find that the same remainder is left, no matter how long we continue the division process. For this reason, the same digit appears again and again in the quotient. This fact is shown by putting a dot as a bar over the repeating digits.

9. **Rounding off of decimal numbers :**

(i) If the answer required is correct to two decimal places, we retain digits upto three decimal places.

(ii) If the digit in the third decimal place is five or more than five, then the digit in

the second decimal place is increased by one and, if the digit in the third decimal place is less than five, then the digit in the second decimal place is not altered.

(iii) The third digit which was retained is now omitted.

Thus, for getting 8.4813 correct to two decimal places.

Write the given number upto three decimal places i.e. 8.481.

Since, the digit in the third decimal place is 1 which is less than 5.

∴ The digit in the second decimal place is not altered.

And, so 8.4813 = 8.48, correct to two decimal places.

In the same way, to get 3.946824 correct to nearest thousandths i.e., correct to three decimal places, first write it as 3.9468.

Then according to the rule, the digit in the third place changes from 6 to 7.

3.9468 = 3.947, correct to three decimal places.

EXERCISE 4 (A)

Question 1.

Convert the following into fractions in their lowest terms :

(i) 3.75

(ii) 0.5

(iii) 2.04

(iv) 0.65

(v) 2.405

(vi) 0.085

(vii) 8.025

Answer:

$$\begin{aligned}(i) 3.75 &= \frac{375}{100} = \frac{375 \div 25}{100 \div 25} \\ &\quad (\text{HCF of 375 and 100} = 25) \\ &= \frac{15}{4} \text{ Ans.}\end{aligned}$$

$$(ii) 0.5 = \frac{5}{10} = \frac{1}{2} \text{ Ans.}$$

$$\begin{aligned}(iii) 2.04 &= \frac{204}{100} = \frac{204 \div 4}{100 \div 4} \\ &\quad (\text{HCF of 204 and 100} = 4) \\ &= \frac{51}{25} \text{ Ans.}\end{aligned}$$

$$(iv) 0.65 = \frac{65}{100} = \frac{65 \div 5}{100 \div 5} = \frac{13}{20} \text{ Ans.}$$

$$(v) 2.405 = \frac{2405}{1000} = \frac{2405 \div 5}{1000 \div 5} = \frac{481}{200} \text{ Ans.}$$

$$(vi) 0.085 = \frac{85}{1000} = \frac{85 \div 5}{1000 \div 5} = \frac{17}{200} \text{ Ans.}$$

$$(vii) 8.025 = \frac{8025}{1000} = \frac{8025 \div 25}{1000 \div 25}$$

Question 2.

Convert into decimal fractions

$$(i) 2\frac{4}{5}$$

$$(ii) \frac{79}{100}$$

$$(iii) \frac{37}{10,000}$$

$$(iv) \frac{7543}{10^4}$$

$$(v) \frac{3}{4}$$

$$(vi) 9\frac{3}{5}$$

$$(vii) 8\frac{5}{8}$$

$$(viii) 5\frac{7}{8}$$

Answer:

$$\begin{aligned}(i) (i) 2\frac{4}{5} &= \frac{14}{5} \\ &= \frac{14}{5} \times \frac{2}{2} = \frac{28}{10} = 2.8\end{aligned}$$

$$(ii) \frac{79}{100} = 0.79 \text{ Ans.}$$

$$(iii) \frac{37}{10,000} = 0.0037 \text{ Ans.}$$

$$\begin{aligned}(iv) \frac{7543}{10^4} &= \frac{7543}{10000} \\ &= 0.7543 \text{ Ans.}\end{aligned}$$

$$(v) \frac{3}{4} = 0.75 \text{ Ans.}$$

$$\begin{array}{r} 0.75 \\ 4 \overline{) 3.00} \\ \underline{28} \\ 20 \\ \underline{20} \\ \underline{ \times} \end{array}$$

$$(vi) 9\frac{3}{5} = \frac{48}{5} = 9.6$$

$$\begin{array}{r} 9.6 \\ 5 \overline{) 48.0} \\ \underline{45} \\ 30 \\ \underline{30} \\ \times \end{array}$$

$$(vii) 8\frac{5}{8} = 8.625$$

$$\begin{array}{r} 0.625 \\ 8 \overline{) 5.000} \\ \underline{48} \\ 20 \\ \underline{16} \\ 40 \\ \underline{40} \\ \times \end{array}$$

$$(viii) 5\frac{7}{8} = 5.875$$

$$\begin{array}{r} 8.75 \\ 8 \overline{) 7.000} \\ \underline{64} \\ 60 \\ \underline{56} \\ 40 \\ \underline{40} \\ \times \end{array}$$

Question 3.

Write the number of decimal places in :

- (i) 0.4762
- (ii) 7.00349
- (iii) 8235.403
- (iv) 35.4
- (v) 2.608
- (vi) 0.000879

Answer:

- (i) In 0.4762, there are four places.
- (ii) In 7.00349, there are five places.
- (iii) In 8235.403, there are three places.
- (iv) In 35.4, there is one place.
- (v) In 2.608, there are three places.
- (vi) In 0.000879, there are six places.

Question 4.

Write the following decimals as word statements :

- (i) 0.4, 0.9, 0.1
- (ii) 1.9, 4.4, 7.5
- (iii) 0.02, 0.56, 13.06
- (iv) 0.005, 0.207, 111.519
- (v) 0.8, 0.08, 0.008, 0.0008
- (vi) 256.1, 10.22, 0.634

Answer:

- (i) 0.4 = zero point four, 0.9 = zero point nine, 0.1 = zero point one.
- (ii) 1.9 = one point nine, 4.4 = four point four, 7.5 = seven point five.
- (iii) 0.02 = zero point zero two, 0.56 = zero point five six, 13.06 = thirteen point zero six.
- (iv) 0.005 = zero point zero zero five, 0.207 = zero point two zero seven, 111.519 = one hundred eleven point five one nine.
- (v) 0.8 = zero point eight, 0.08 = zero point zero eight, 0.008 = zero point zero zero eight, 0.0008 = zero point zero zero zero eight
- (vi) 256.1 = Two hundred fifty six point one, 10.22 = Ten point two two, 0.634 = zero point six three four.

Question 5.

Convert the given fractions into like fractions:

- (i) 0.5, 3.62, 43.987 and 232.0037
- (ii) 215.78, 33.0006, 530.3 and 0.03569

Answer:

- (i) 0.5, 3.62, 43.987 and 232.0037
In these decimals, the greatest places of decimal is 4
 $\therefore 0.5 = 0.5000$
 $3.62 = 3.6200$
 $43.987 = 43.9870$
 $232.0037 = 232.0037$
- (ii) 215.78, 33.0006, 530.3 and 0.03569
In these decimals, the greatest places of decimal is 5
 $\therefore 215.78 = 215.78000$
 $33.0006 = 33.00060$
 $530.3 = 530.30000$
 $0.03569 = 0.03569$

EXERCISE 4 (B)

Question 1.

Add:

(i) 0.5 and 0.37 (ii) 3.8 and 8.7

(iii) 0.02, 0.008 and 0.309

(iv) 0.4136, 0.3195 and 0.52

(v) 9.25, 3.4 and 6.666

(vi) 3.007, 0.587 and 18.341

(vii) 0.2, 0.02 and 2.0002

(viii) 6.08, 60.8, 0.608 and 0.0608

(ix) 29.03, 0.0003, 0.3 and 7.2

(x) 3.4, 2.025, 9.36 and 3.6221

Answer:

(i) $0.5 + 0.37 = 0.87$ Ans.

$$\begin{array}{r} 0.5 \\ + 0.37 \\ \hline 0.87 \end{array}$$

(ii) $3.8 + 8.7 = 12.5$ Ans.

$$\begin{array}{r} 3.8 \\ + 8.7 \\ \hline 12.5 \end{array}$$

(iii) $0.02 + 0.008 + 0.309 = 0.337$ Ans.

$$\begin{array}{r} 0.02 \\ + 0.008 \\ + 0.309 \\ \hline 0.337 \end{array}$$

(iv) $0.4136 + 0.3195 + 0.52 = 1.2531$ Ans.

$$\begin{array}{r} 0.4136 \\ + 0.3195 \\ + 0.52 \\ \hline 1.2531 \end{array}$$

(v) $9.25 + 3.4 + 6.666 = 19.316$ Ans.

$$\begin{array}{r} 9.25 \\ + 3.4 \\ + 6.666 \\ \hline 19.316 \end{array}$$

(vi) $3.007 + 0.587 + 18.341 = 21.935$ Ans.

$$\begin{array}{r} 3.007 \\ + 0.587 \\ + 18.341 \\ \hline 21.935 \end{array}$$

(vii) $0.2 + 0.02 + 2.0002 = 2.2202$ Ans.

$$\begin{array}{r} 0.2 \\ + 0.02 \\ + 2.0002 \\ \hline 2.2202 \end{array}$$

$$(viii) 6.08 + 60.8 + 0.608 + 0.0608 = 67.5488$$

Ans.

$$\begin{array}{r} 6.08 \\ + 60.8 \\ + 0.608 \\ + 0.0608 \\ \hline 67.5488 \end{array}$$

$$(ix) 29.03 + 0.0003 + 0.3 + 7.2 = 36.5303 \text{ Ans.}$$

$$\begin{array}{r} 29.03 \\ + 0.0003 \\ + 0.3 \\ + 7.2 \\ \hline 36.5303 \end{array}$$

$$(x) 3.4 + 2.025 + 9.36 + 3.6221 = 18.4071 \text{ Ans.}$$

$$\begin{array}{r} 3.4 \\ + 2.025 \\ + 9.36 \\ + 3.6221 \\ \hline 18.4071 \end{array}$$

Question 2.

Subtract the first! number from the second :

(i) 5.4, 9.8

(ii) 0.16, 4.3

(iii) 0.82, 8.6

(v) 2.237, 9.425

(vi) 41.03, 59.46

(vii) 3.92, 26.86

(viii) 4.73, 8.5

(ix) 12.63, 36.2

(x) 0.845, 3.71

Answer:

(i) $9.8 - 5.4 = 4.4$ **Ans.**

$$\begin{array}{r} 9.8 \\ - 5.4 \\ \hline 4.4 \end{array}$$

(ii) $4.30 - 0.16 = 4.14$ **Ans.**

$$\begin{array}{r} 4.30 \\ - 0.16 \\ \hline 4.14 \end{array}$$

(iii) $8.60 - 0.82 = 7.78$ **Ans.**

$$\begin{array}{r} 8.60 \\ - 0.82 \\ \hline 7.78 \end{array}$$

(iv) $8.43 - 0.07 = 8.36$ **Ans.**

$$\begin{array}{r} 8.43 \\ - 0.07 \\ \hline 8.36 \end{array}$$

(v) $9.425 - 2.237 = 7.188$ **Ans.**

$$\begin{array}{r} 9.425 \\ - 2.237 \\ \hline 7.188 \end{array}$$

(vi) $59.46 - 41.03 = 18.43$ **Ans.**

$$\begin{array}{r} 59.46 \\ - 41.03 \\ \hline 18.43 \end{array}$$

(vii) $26.86 - 3.92 = 22.94$ **Ans.**

$$\begin{array}{r} 26.86 \\ - 3.92 \\ \hline 22.94 \end{array}$$

(viii) $8.50 - 4.73 = 3.77$ **Ans.**

$$\begin{array}{r} 8.50 \\ - 4.73 \\ \hline 3.77 \end{array}$$

(ix) $36.20 - 12.63 = 23.57$ **Ans.**

$$\begin{array}{r} 36.20 \\ - 12.63 \\ \hline 23.57 \end{array}$$

(x) $3.710 - 0.845 = 2.865$ **Ans.**

$$\begin{array}{r} 3.710 \\ - 0.845 \\ \hline 2.865 \end{array}$$

Question 3.

Simplify :

(i) $28.796 - 13.42 - 2.555$

(ii) $93.354 - 62.82 - 13.045$

(iii) $36 - 18.59 - 3.2$

(iv) $86 + 16.95 - 3.0042$

(v) $32.8 - 13 - 10.725 + 3.517$

(vi) $4000 - 30.51 - 753.101 - 69.43$

(vii) $0.1835 + 163.2005 - 25.9 - 100$

(viii) $38.00 - 30 + 200.200 - 0.230$

(ix) $555.555 + 55.555 - 5.55 - 0.555$

Answer:

$$\begin{aligned}(i) & 28.796 - 13.42 - 2.555 \\ &= 28.796 - (13.42 + 2.555) \\ &= 28.796 - 15.975 = 12.821 \text{ Ans.}\end{aligned}$$

$$\begin{array}{r} 28.796 \\ - 15.975 \\ \hline 12.821 \end{array} \qquad \begin{array}{r} 13.420 \\ + 2.555 \\ \hline 15.975 \end{array}$$

$$\begin{aligned}(ii) & 93.354 - 62.82 - 13.045 \\ &= 93.354 - (62.82 + 13.045) \\ &= 93.354 - 75.865 = 17.489 \text{ Ans.}\end{aligned}$$

$$\begin{array}{r} 93.354 \\ - 75.865 \\ \hline 17.489 \end{array} \qquad \begin{array}{r} 62.820 \\ + 13.045 \\ \hline 75.865 \end{array}$$

$$\begin{aligned}(iii) & 36 - 18.59 - 3.2 = 36 - (18.59 + 3.2) \\ &= 36 - (21.79) = 14.21 \text{ Ans.}\end{aligned}$$

$$\begin{array}{r} 36.00 \\ - 21.79 \\ \hline 14.21 \end{array} \qquad \begin{array}{r} 18.59 \\ + 3.20 \\ \hline 21.79 \end{array}$$

$$\begin{aligned}(iv) & 86 + 16.95 - 3.0042 = 102.95 - 3.0042 \\ &= 99.9458 \text{ Ans.}\end{aligned}$$

$$\begin{array}{r} 102.9500 \\ - 3.0042 \\ \hline 99.9458 \end{array} \qquad \begin{array}{r} 86.00 \\ + 16.95 \\ \hline 102.95 \end{array}$$

$$\begin{aligned}(v) & 32.8 - 13 - 10.725 + 3.517 \\ &= (32.8 + 3.517) - (13 + 10.725) \\ &= 36.317 - 23.725 = 12.592 \text{ Ans.}\end{aligned}$$

$$\begin{array}{r} 13.000 \\ + 10.725 \\ \hline 23.725 \end{array} \qquad \begin{array}{r} 32.8 \\ + 3.517 \\ \hline 36.317 \end{array} \qquad \begin{array}{r} 36.317 \\ - 23.725 \\ \hline 12.592 \end{array}$$

$$\begin{aligned}(vi) & 4000 - 30.51 - 753.101 - 69.43 \\ &= 4000 - (30.51 + 753.101 + 69.43) \\ &= 4000 - 853.041 = 3146.959 \text{ Ans.}\end{aligned}$$

$$\begin{array}{r} 30.510 \\ + 753.101 \\ + 69.430 \\ \hline 853.041 \end{array} \qquad \begin{array}{r} 4000.000 \\ - 853.041 \\ \hline 3146.959 \end{array}$$

$$\begin{aligned}
 \text{(vii)} \quad & 0.1835 + 163.2005 - 25.9 - 100 \\
 &= (0.1835 + 163.2005) - (25.9 + 100) \\
 &= 163.3840 - 125.9 = 37.484 \text{ Ans.}
 \end{aligned}$$

$$\begin{array}{r}
 25.9 \\
 + 100.0 \\
 \hline
 125.9
 \end{array}$$

$$\begin{array}{r}
 0.1835 \\
 + 163.2005 \\
 \hline
 163.3840
 \end{array}
 \qquad
 \begin{array}{r}
 163.3840 \\
 - 125.9000 \\
 \hline
 37.4840
 \end{array}$$

$$\begin{aligned}
 \text{(viii)} \quad & 38.00 - 30 + 200.200 - 0.230 \\
 &= (38.00 + 200.200) - (30 + 0.230) \\
 &= 238.200 - 30.230 \\
 &= 207.970 = 207.97 \text{ Ans.}
 \end{aligned}$$

$$\begin{array}{r}
 238.200 \\
 - 30.230 \\
 \hline
 207.970
 \end{array}$$

$$\begin{aligned}
 \text{(ix)} \quad & 555.555 + 55.555 - 5.55 - 0.555 \\
 &= (555.555 + 55.555) - (5.55 + 0.555) \\
 &= 611.110 - 6.105 = 605.005 \text{ Ans.}
 \end{aligned}$$

$$\begin{array}{r}
 555.555 \\
 + 55.555 \\
 \hline
 611.110
 \end{array}
 \qquad
 \begin{array}{r}
 611.110 \\
 - 6.105 \\
 \hline
 605.005
 \end{array}$$

Question 4.

Find the difference between 6.85 and 0.685.

Answer:

Difference between 6.85 and 0.685

$$= 6.85 - 0.685 = 6.165 \text{ Ans.}$$

$$\begin{array}{r}
 6.850 \\
 - 0.685 \\
 \hline
 6.165
 \end{array}$$

Question 5.

Take out the sum of 19.38 and 56.025 then subtract it from 200. 111.

Answer:

$$\text{Sum of } 19.38 + 56.025 = 75.405$$

$$\begin{array}{r} 19.38 \\ + 56.025 \\ \hline 75.405 \end{array}$$

Difference of 200.111 and 75.405

$$= 200.111 - 75.405 = 124.706 \text{ Ans.}$$

$$\begin{array}{r} 200.111 \\ - 75.405 \\ \hline 124.706 \end{array}$$

Question 6.

Add 13.95 and 1.003 ; and from the result, subtract the sum of 2.794 and 6.2.

Answer:

Sum of 13.95 and 1.003

$$= 13.95 + 1.003 = 14.953$$

$$\begin{array}{r} 13.95 \\ + 1.003 \\ \hline 14.953 \end{array}$$

Sum of 2.794 and 6.2

$$= 2.794 + 6.2 = 8.994$$

$$\begin{array}{r} 2.794 \\ + 6.200 \\ \hline 8.994 \end{array}$$

Difference of 14.953 and 8.994

$$= 14.953 - 8.994 = 5.959 \text{ Ans.}$$

$$\begin{array}{r} 14.953 \\ - 8.994 \\ \hline 5.959 \end{array}$$

Question 7.

What should be added to 39.587 to give 80.375 ?

Answer:

$$\text{Sum} = 80.375$$

$$\text{Given number} = 39.587$$

∴ The number which is to be added

$$= 80.375 - 39.587 = 40.788 \text{ Ans.}$$

$$\begin{array}{r} 80.375 \\ - 39.587 \\ \hline 40.788 \end{array}$$

Question 8.

What should be subtracted from 100 to give 19.29?

Answer:

$$\text{Sum} = 100$$

$$\text{The number} = 19.29$$

∴ The number which is to be subtracted

$$= 100 - 19.29 = 80.71 \text{ Ans.}$$

$$\begin{array}{r} 100.00 \\ - 19.29 \\ \hline 80.71 \end{array}$$

Question 9.

What is the excess of 584.29 over 213.95 ?

Answer:

$$\text{Total} = 584.29$$

$$\text{Given number} = 213.95$$

$$\text{Required difference} = 584.29 - 213.95$$

$$= 370.34 \text{ Ans.}$$

$$\begin{array}{r} 584.29 \\ - 213.95 \\ \hline 370.34 \end{array}$$

Question 10.

Evaluate:

(i) $(5.4 - 0.8) + (2.97 - 1.462)$

(ii) $(6.25 + 0.36) - (17.2 - 8.97)$

(iii) $9.004 + (3 - 2.462)$

(iv) $879.4 - (87.94 - 8.794)$

Answer:

$$\begin{array}{r} \text{(i) } (5.4 - 0.8) + (2.97 - 1.462) \\ = 4.6 + 1.508 = 6.108 \end{array} \quad \begin{array}{r} \sim \text{ } \\ -1.4 \\ \hline 1.5 \end{array}$$

$$\begin{array}{r} \text{(ii) } (6.25 + 0.36) - (17.2 - 8.97) \\ = 6.61 - 8.23 = -1.62 \end{array}$$

$$\begin{array}{r} 6.25 \quad 17.20 \quad 8.23 \\ + 0.36 \quad - 8.97 \quad - 6.61 \\ \hline 6.61 \quad 8.23 \quad -1.62 \end{array}$$

$$\begin{array}{r} \text{(iii) } 9.004 + (3 - 2.462) \\ = 9.004 + 0.538 = 9.542 \end{array}$$

$$\begin{array}{r} 3.000 \\ - 2.462 \\ \hline 0.538 \end{array}$$

$$\begin{array}{r} \text{(iv) } 879.4 - (87.94 - 8.794) \\ = 879.4 - 79.146 = 800.254 \end{array}$$

$$\begin{array}{r} 87.940 \quad 879.400 \\ - 8.794 \quad - 79.146 \\ \hline 79.146 \quad 800.254 \end{array}$$

Question 11.

What is the excess of 75 over 48.29?

Answer:

Excess of 75 over 48.29

$$\begin{array}{r} 75.00 \\ - 48.29 \\ \hline 26.71 \end{array}$$

 $\therefore$ Excess of 75 over 48.29 is 26.71

Question 12.

If $A = 237.98$ and $B = 83.47$.

Find :

(i) $A - B$

(ii) $B - A$.

Answer:

(i) $A - B$

$$\begin{array}{r} A = 237.98 \\ B = 83.47 \\ \hline \end{array} \begin{array}{r} 237.98 \\ -83.47 \\ \hline 154.51 \end{array}$$

$$\Rightarrow A - B = 154.51$$

(ii) $B - A$

$$= 83.47 - 237.98 = -154.51$$

Question 13.

The cost of one kg of sugar increases from ₹28.47 to ₹32.65. Find the increase in cost.

Answer:

$$\begin{array}{r} \text{Initial cost of sugar} = ₹28.47 \\ \text{Increase cost of sugar} = ₹32.65 \\ \hline \end{array} \begin{array}{r} 32.65 \\ -28.47 \\ \hline 5.18 \end{array}$$

$$\therefore \text{Increase of sugar in cost} = ₹5.18$$

EXERCISE 4 (C)**Question 1.**

Multiply:

(i) 0.87 by 10

(ii) 2.948 by 100

(iii) 6.4 by 1000

(iv) 5.8 by 4

(v) 16.32 by 28

(vi) 5.037 by 8

(vii) 4.6 by 2.1

(viii) 0.568 by 6.4

Answer:

(i) $0.87 \times 10 = 8.7$

(ii) $2.948 \times 100 = 294.8$

(iii) $6.4 \times 1000 = 6400$

(iv) $5.8 \times 4 = 23.2$

(v) $16.32 \times 28 = 456.96$

$$\begin{array}{r} 16.32 \\ \times 28 \\ \hline 130.56 \\ 326.40 \\ \hline 456.96 \end{array}$$

(vi) $5.037 \times 8 = 40.296$

$$\begin{array}{r} 5.037 \\ \times 8 \\ \hline 40.296 \end{array}$$

(vii) $4.6 \times 2.1 = 9.66$

$$\begin{array}{r} 4.6 \\ \times 2.1 \\ \hline 46 \\ 92 \times \\ \hline 9.66 \end{array}$$

(viii) $0.568 \times 6.4 = 3.6352$

$$\begin{array}{r} 0.568 \\ \times 6.4 \\ \hline 2272 \\ 34080 \\ \hline 3.6352 \end{array}$$

Question 2.

Multiply each number by 10, 100, 1000 :

(i) 0.5

(ii) 0.112

(iii) 4.8

(iv) 0.0359

(v) 16.27

(vi) 234.8

Answer:

(i) $0.5 \times 10 = 5, 0.5 \times 100 = 50,$

$0.5 \times 1000 = 500$

(ii) $0.112 \times 10 = 1.12, 0.112 \times 100$

$= 11.2, 0.112 \times 1000 = 112$

(iii) $4.8 \times 10 = 48, 4.8 \times 100 = 480,$

$4.8 \times 1000 = 4800$

(iv) $0.0359 \times 10 = 0.359, 0.0359 \times 100 = 3.59, 0.0359 \times 1000 = 35.9$

(v) $16.27 \times 10 = 162.7, 16.27 \times 100 = 1627, 16.27 \times 1000 = 16270$

(vi) $234.8 \times 10 = 2348, 234.8 \times 100 = 23480, 234.8 \times 1000 = 234800$

Question 3.

Evaluate:

(i) 5.897×2.3

(ii) 0.894×87

(iii) 0.01×0.001

(iv) $0.84 \times 2.2 \times 4$

(v) $4.75 \times 0.08 \times 3$

(vi) $2.4 \times 3.5 \times 4.8$

(vii) $0.8 \times 1.2 \times 0.25$

(viii) $0.3 \times 0.03 \times 0.003$

(ix) $12.003 \times (0.2)^5$

Answer:

(i) $5.897 \times 2.3 = 13.5631$ Ans.

$$\begin{array}{r} 5.897 \\ \times 2.3 \\ \hline 17691 \\ 11794 \times \\ \hline 13.5631 \end{array}$$

(ii) $0.894 \times 87 = 77.778$ Ans.

$$\begin{array}{r} .894 \\ \times 87 \\ \hline 6258 \\ 7152 \times \\ \hline 77.778 \end{array}$$

(iii) $0.01 \times 0.001 = 0.00001$ Ans.

(iv) $0.84 \times 2.2 \times 4$

$= 0.84 \times 8.8$

$= 7.392$ Ans.

$$\begin{array}{r} 84 \\ \times 88 \\ \hline 672 \\ 672 \times \\ \hline 7392 \end{array}$$

(v) $4.75 \times 0.08 \times 3 = 4.75 \times 0.08 \times 3$

$= 4.75 \times 0.24$

$= 1.1400 = 1.14$ Ans.

$$\begin{array}{r} 4.75 \\ 0.24 \\ \hline 1900 \\ 950 \times \\ \hline 1.1400 \end{array}$$

$$\begin{aligned}
 \text{(vi)} \quad 2.4 \times 3.5 \times 4.8 &= 8.40 \times 4.8 \\
 &= 8.4 \times 4.8 \\
 &= 40.32 \text{ Ans.}
 \end{aligned}$$

$ \begin{array}{r} 24 \\ \times 35 \\ \hline 120 \\ 72 \times \\ \hline 840 \end{array} $	$ \begin{array}{r} 8.4 \\ \times 4.8 \\ \hline 672 \\ 336 \times \\ \hline 4032 \end{array} $
---	---

$$\begin{aligned}
 \text{(vii)} \quad 0.8 \times 1.2 \times 0.25 &= 0.96 \times 0.25 \\
 &= 0.2400 \\
 &= 0.24 \text{ Ans.}
 \end{aligned}$$

$$\begin{array}{r}
 96 \\
 \times 25 \\
 \hline
 480 \\
 192 \times \\
 \hline
 2400
 \end{array}$$

$$\begin{aligned}
 \text{(viii)} \quad 0.3 \times 0.03 \times 0.003 \\
 &= 0.009 \times 0.003 \\
 &= 0.000027 \text{ Ans.}
 \end{aligned}$$

$$\begin{aligned}
 \text{(ix)} \quad 12.003 \times (0.2)^5 \\
 &= 12.003 \times 0.2 \times 0.2 \times 0.2 \times 0.2 \times 0.2 \\
 &= 12.003 \times 0.00032 = 0.00384096 \text{ Ans.}
 \end{aligned}$$

$$\begin{array}{r}
 12003 \\
 \times 32 \\
 \hline
 24006 \\
 36009 \times \\
 \hline
 384096
 \end{array}$$

Question 4.

Divide :

(i) 54.9 by 10

(ii) 7.8 by 100

(iii) 324.76 by 1000

(iv) 12.8 by 4

(v) 27.918 by 9

(vi) 4.672 by 8

(vii) 4.32 by 1.2

(viii) 7.644 by 1.4

(ix) 4.8432 by 0.08

Answer:

(i) $54.9 \div 10 = 5.49$ Ans.

(ii) $7.8 \div 100 = 0.078$ Ans.

(iii) $324.76 \div 1000 = 0.32476$ Ans.

(iv) $12.8 \div 4 = 3.2$ Ans.

(v) $27.918 \div 9 = 3.102$ Ans.

(vi) $4.672 \div 8 = 0.584$ Ans.

$$\begin{array}{r} 0.584 \\ 8 \overline{) 4.672} \\ \underline{-40} \\ 67 \\ \underline{-64} \\ 32 \\ \underline{-32} \\ \times \end{array}$$

(vii) $4.32 \div 1.2 = 4.32 \div 1.20$

$= 432 \div 120 = 3.6$ Ans.

$$\begin{array}{r} 3.6 \\ 120 \overline{) 432.0} \\ \underline{-360} \\ 720 \\ \underline{-720} \\ \times \end{array}$$

(viii) $7.644 \div 1.4 = 7.644 \div 1.400$

$= 7644 \div 1400 = 5.46$ Ans.

$$\begin{array}{r} 5.46 \\ 1400 \overline{) 7644.00} \\ \underline{-7000} \\ 6440 \\ \underline{-5600} \\ 8400 \\ \underline{-8400} \\ \times \end{array}$$

$$(ix) 4.8432 \div 0.08 = 4.8432 \div 0.0800$$

$$= 48432 \div 800 = 60.54 \text{ Ans.}$$

$$\begin{array}{r}
 60.54 \\
 \hline
 800 \overline{) 48432.00} \\
 \underline{-4800} \\
 4320 \\
 \underline{-4000} \\
 3200 \\
 \underline{-3200} \\
 \hline
 x
 \end{array}$$

Question 5.

Divide each of the given numbers by 10, 100, 1000 and 10000

(i) 2.1

(ii) 8.64

(iii) 5.01

(iv) 0.0906

(v) 0.125

(vi) 111.11

(vii) 0.848×3

(viii) $4.906 \times (0.2)^2$

(ix) $(1.2)^2 \times (0.9)^2$

Answer:

(i) $2.1 \div 10 = 0.21$, $2.1 \div 100 = 0.021$,

$2.1 \div 1000 = 0.0021$

and $2.1 \div 10000 = 0.00021$

(ii) $8.64 \div 10 = 0.864$, $8.64 \div 100 = 0.0864$,

$8.64 \div 1000 = 0.00864$

and $8.64 \div 10000 = 0.000864$

(iii) $5.01 \div 10 = 0.501$,

$5.01 \div 100 = 0.0501$,

$5.01 \div 1000 = 0.00501$,

$5.01 \div 10000 = 0.000501$

(iv) $0.0906 \div 10 = 0.00906$,
 $0.0906 \div 100 = 0.000906$,
 $0.0906 \div 1000 = 0.000906$,
 $0.0906 \div 10000 = 0.0000906$

(v) 0.125
Now $0.125 \div 10 = 0.0125$,
 $0.125 \div 100 = 0.00125$,
 $0.125 \div 1000 = 0.000125$,
 $0.125 \div 10000 = 0.0000125$

(vi) $111.11 \div 10 = 11.111$,
 $111.11 \div 100 = 1.1111$,
 $111.11 \div 1000 = 0.11111$,
 $111.11 \div 10000 = 0.011111$

(vii) $0.848 \times 3 = 2.544$,
Now $2.544 \div 10 = 0.2544$,
 $2.544 \div 100 = 0.02544$,
 $2.544 \div 1000 = 0.002544$,
 $2.544 \div 10000 = 0.0002544$

(viii) $4.906 \times (0.2)^2 = 4.906 \times 0.2 \times 0.2$
 $= 4.906 \times 0.04 = 0.19624$
Now $0.19624 \div 10 = 0.019624$,
 $0.19624 \div 100 = 0.0019624$,
 $0.19624 \div 1000 = 0.00019624$,
 $0.19624 \div 10000 = 0.000019624$

(ix) $(1.2)^2 \times (0.9)^2 = 1.2 \times 1.2 \times 0.9 \times 0.9 = 1.44 \times 0.81 = 1.1664$
Now $1.1664 \div 10 = 0.11664$,
 $1.1664 \div 100 = 0.011664$,
 $1.1664 \div 1000 = 0.0011664$,
 $1.1664 \div 10000 = 0.00011664$

Question 6.

Evaluate :

(i) $9.75 + 5$

(ii) $4.4064 + 4$

(iii) $27.69 + 30$

(iv) $19.25 + 25$

(v) $20.64 + 16$

(vi) $3.204 + 9$

(vii) $0.125 + 25$

(viii) $0.14616 + 72$

(ix) $0.6227 + 1300$

(x) $257.894 + 0.169$

(xi) $6.3 + (0.3)^2$

Answer:

(i) $9.75 \div 5 = 1.95$ **Ans.**

$$\begin{array}{r} 1.95 \\ 5 \overline{) 9.75} \\ \underline{-5} \\ 47 \\ \underline{-45} \\ 25 \\ \underline{-25} \\ \underline{ \times} \end{array}$$

(ii) $4.4064 \div 4 = 1.1016$ **Ans.**

(iii) $27.69 \div 30 = 0.923$ **Ans.**

$$\begin{array}{r} 0.923 \\ 30 \overline{) 27.690} \\ \underline{-270} \\ 69 \\ \underline{-60} \\ 90 \\ \underline{-90} \\ \underline{ \times} \end{array}$$

(iv) $19.25 \div 25 = 0.77$ **Ans.**

$$\begin{array}{r} 0.77 \\ 25 \overline{) 19.25} \\ \underline{-175} \\ 175 \\ \underline{-175} \\ \hline \times \end{array}$$

(v) $20.64 \div 16 = 1.29$ **Ans.**

$$\begin{array}{r} 1.29 \\ 16 \overline{) 20.64} \\ \underline{-16} \\ 46 \\ \underline{-32} \\ 144 \\ \underline{-144} \\ \hline \times \end{array}$$

(vi) $3.204 \div 9 = 0.356$ **Ans.**

$$\begin{array}{r} 0.356 \\ 9 \overline{) 3.204} \\ \underline{-27} \\ 50 \\ \underline{-45} \\ 54 \\ \underline{-54} \\ \hline \times \end{array}$$

(vii) $0.125 \div 25 = 0.005$ **Ans.**

$$\begin{array}{r} 0.005 \\ 25 \overline{) 0.125} \\ \underline{-125} \\ \hline \times \end{array}$$

(viii) $0.14616 \div 72 = 0.00203$ **Ans.**

$$\begin{array}{r}
 0.00203 \\
 72 \overline{) 0.14616} \\
 \underline{-144} \\
 216 \\
 \underline{-216} \\
 \underline{ \times}
 \end{array}$$

(ix) $0.6227 \div 1300 = 0.000479$

$$\begin{array}{r}
 0.000479 \\
 1300 \overline{) 0.62270} \\
 \underline{-5200} \\
 10270 \\
 \underline{-9100} \\
 11700 \\
 \underline{-11700} \\
 \underline{ \times}
 \end{array}$$

(x) $257.894 \div 0.169$

$= 257894 \div 169 = 1526$

$$\begin{array}{r}
 1526 \\
 169 \overline{) 257894} \\
 \underline{-169} \\
 888 \\
 \underline{-845} \\
 439 \\
 \underline{-338} \\
 1014 \\
 \underline{-1014} \\
 \underline{ \times}
 \end{array}$$

(xi) $6.3 \div (0.3)^2 = 6.3 \div (0.3 \times 0.3)$

$= 6.3 \div (0.09) = 630 \div 09$

$= 630 \div 9 = 70$

Question 7.

Evaluate:

(i) $4.3 \times 0.52 \times 0.3$

(ii) $3.2 \times 2.5 \times 0.7$

(iii) $0.8 \times 1.5 \times 0.6$

(iv) $0.3 \times 0.3 \times 0.3$

(v) $1.2 \times 1.2 \times 0.4$

(vi) $0.4 \times 0.04 \times 0.004$

(vii) $0.5 \times 0.6 \times 0.7$

(Viii) $0.5 \times 0.06 \times 0.007$

Answer:

(i) $4.3 \times 0.52 \times 0.3$

$$\begin{array}{r} 0.52 \\ \times 4.3 \\ \hline 156 \\ 208 \times \\ \hline 2.236 \\ \times 0.3 \\ \hline 6708 \\ 0000 \times \\ \hline \underline{0.6708} \end{array}$$

(Sum of decimal places = $1 + 2 + 1 = 4$)

$$\therefore 4.3 \times 0.52 \times 0.3 = 0.6708$$

(ii) $3.2 \times 2.5 \times 0.7$

$$\begin{array}{r} 3.2 \\ \times 2.5 \\ \hline 160 \\ 64 \times \\ \hline 8.00 \\ \times 0.7 \\ \hline 5600 \\ 000 \times \\ \hline 5.600 \end{array}$$

(Sum of decimal places = $1 + 1 + 1 = 3$)

$$\therefore 3.2 \times 2.5 \times 0.7 = 5.600 \text{ or } 5.6$$

(iii) $0.8 \times 1.5 \times 0.6$

$$\begin{array}{r} 1.5 \\ \times 0.8 \\ \hline 120 \\ 00 \times \\ \hline 1.20 \\ \times 0.6 \\ \hline 720 \\ 000 \times \\ \hline 0.720 \end{array}$$

(Sum of decimal places = $1 + 1 + 1 = 3$)

$$\therefore 0.8 \times 1.5 \times 0.6 = 0.720 \text{ or } 0.72$$

(iv) $0.3 \times 0.3 \times 0.3$

$$\begin{array}{r} 0.3 \\ \times 0.3 \\ \hline 09 \\ 00 \times \\ \hline 0.09 \\ \times 0.3 \\ \hline 0.027 \end{array}$$

(Sum of decimal places = $1 + 1 + 1 = 3$)

$$\therefore 0.3 \times 0.3 \times 0.3 = 0.027$$

(v) $1.2 \times 1.2 \times 0.4$

$$\begin{array}{r}
 1.2 \\
 \times 1.2 \\
 \hline
 .24 \\
 12 \times \\
 \hline
 1.44 \\
 \times 0.4 \\
 \hline
 576 \\
 000 \times \\
 \hline
 0.576
 \end{array}$$

(Sum of decimal places = 1 + 1 + 1 = 3)

$$\therefore 1.2 \times 1.2 \times 0.4 = 0.576$$

(vi) $0.4 \times 0.04 \times 0.004$

$$\begin{array}{r}
 0.004 \\
 \times 0.04 \\
 \hline
 0016 \\
 0000 \times \\
 \hline
 0000 \times \times \\
 \hline
 0.00016 \\
 \times 0.4 \\
 \hline
 0.000064
 \end{array}$$

(Sum of decimal places = 1 + 2 + 3 = 6)

$$\therefore 0.4 \times 0.04 \times 0.004 = 0.000064$$

(vii) $0.5 \times 0.6 \times 0.7$

$$\begin{array}{r}
 0.5 \\
 \times 0.6 \\
 \hline
 .30 \\
 00 \times \\
 \hline
 0.30 \\
 \times 0.7 \\
 \hline
 210 \\
 000 \times \\
 \hline
 0.210
 \end{array}$$

(Sum of decimal places = $1 + 1 + 1 = 3$)

$$\therefore 0.5 \times 0.6 \times 0.7 = 0.210 \text{ or } 0.21$$

(viii) $0.5 \times 0.06 \times 0.007$

$$\begin{array}{r} 0.007 \\ \times 0.06 \\ \hline 0.00042 \\ \times 0.5 \\ \hline \underline{0.00021} \end{array}$$

(Sum of decimal places = $1 + 2 + 3 = 5$)

$$\therefore 0.5 \times 0.06 \times 0.007 = 0.00021$$

Question 8.

Evaluate:

(i) $(0.9)^2$

(ii) $(0.6)^2 \times 0.5$

(iii) $0.3 \times (0.5)^2$

(iv) $(0.4)^3$

(v) $(0.2)^3 \times 5$

(vi) $(0.2)^3 \times 0.05$

Answer:

(i) $(0.9)^2$

$$\Rightarrow 0.9 \times 0.9 = 0.81$$

(Sum of decimal places $1 + 1 = 2$)

(ii) $(0.6)^2 \times 0.5$

$$\Rightarrow 0.6 \times 0.6 \times 0.5$$

$$\Rightarrow 0.36 \times 0.5 = 0.180 \text{ or } 0.18$$

(Sum of decimal places = $1 + 1 + 1 = 3$)

(iii) $0.3 \times (0.5)^2$

$$\Rightarrow 0.3 \times 0.5 \times 0.5$$

$$\Rightarrow 0.3 \times 0.25 = 0.075$$

(Sum of decimal places $1 + 1 + 1 = 3$)

(iv) $(0.4)^3$

$$\Rightarrow 0.4 \times 0.4 \times 0.4$$

$$\Rightarrow 0.16 \times 0.4 = 0.064$$

(Sum of decimal places $1 + 1 + 1 = 3$)

(v) $(0.2)^3 \times 5$
 $\Rightarrow 0.2 \times 0.2 \times 0.2 \times 5$
 $\Rightarrow 0.08 \times 5 = 0.40$ or 0.4
 (Sum of decimal places $1 + 1 + 1 = 3$)

(vi) $(0.2)^3 \times 0.05$
 $\Rightarrow 0.2 \times 0.2 \times 0.2 \times 0.05$
 $\Rightarrow 0.008 \times 0.05 = 0.00040$
 (Sum of decimal places = 5)

Question 9.

Find the cost of 36.75 kg wheat at the rate of ₹12.80 per kg.

Answer:

Total weight of wheat = 36.75 kg

Cost of 1 kg of wheat = ₹12.80

$\therefore$ Cost of 36.75 kg of wheat
 $= 36.75 \times 12.80 = ₹470.40$

$$\begin{array}{r} 36.75 \\ \times 12.80 \\ \hline 470.40 \end{array}$$

Question 10.

The cost of a pen is ₹56.15. Find the cost of 16 such pens.

Answer:

Cost of one pen = ₹56.15

$\therefore$ Cost of 16 pens
 $= ₹56.15 \times 16 = ₹898.40$

$$\begin{array}{r} 56.15 \\ \times 16 \\ \hline 898.40 \end{array}$$

Question 11.**Evaluate:**

(i) $0.0072 \div 0.06$

(ii) $0.621 \div 0.3$

(iii) $0.0532 \div 0.005$

(iv) $0.01162 \div 0.14$

(v) $(7.5 \times 40.4) \div 25$

(vi) $2.1 \div (0.1 \times 0.1)$

Answer:

(i) $0.0072 \div 0.06$

$$= \frac{0.0072 \times 100}{0.06 \times 100}$$

$$= \frac{0.72}{6} = 0.12$$

(ii) $0.621 \div 0.3$

$$= \frac{0.621 \times 10}{0.3 \times 10}$$

$$= \frac{6.21}{3} = 2.07$$

(iii) $0.0532 \div 0.005$

$$= \frac{0.0532 \times 1000}{0.005 \times 1000} = \frac{53.2}{5} = 10.64$$

(iv) $0.01162 \div 0.14$

$$= \frac{0.01162 \times 100}{0.14 \times 100}$$

$$= \frac{1.162}{14} = 0.083$$

(v) $(7.5 \times 40.4) \div 25$

$$= \frac{303}{25} = 12.12$$

(vi) $2.1 \div (0.1 \times 0.1)$

$$= \frac{2.1 \times 100}{0.01 \times 100} = \frac{210}{1} = 210$$

Question 12.

Fifteen identical articles weigh 31.50 kg. Find the weight of each article.

Answer:

Weight of 15 articles = 31.50 kg

∴ Weight of one article

= $31.50 \div 15 = 2.1$ kg

Question 13.

The product of two numbers is 211.2. If one of these two numbers is 16.5, find the other number.

Answer:

The product of two numbers = 211.2

One number = 16.5

∴ Second number = $211.2 \div 16.5$

$$\begin{aligned} &= \frac{211.2 \times 10}{16.5 \times 10} \\ &= \frac{2112}{165} = 12.8 \end{aligned}$$

Question 14.

One dozen identical articles cost ₹45.96. Find the cost of each article.

Answer:

∴ Weight of one dozen articles = ₹45.96

One dozen = 12

∴ Cost of one article = $45.96 \div 12 = ₹3.83$

EXERCISE 4 (D)**Question 1.**

Find whether the given division forms a terminating decimal or a non-terminating decimal:

(i) $3 \div 8$

(ii) $8 \div 3$

(iii) $6 \div 5$

(iv) $5 \div 6$

(v) $12.5 \div 4$

(vi) $23 \div 0.7$

(vii) $42 \div 9$

(viii) $0.56 \div 0.11$

Answer:

$$(i) 3 \div 8 = 0.375$$

Hence it is terminating decimal.

$$\begin{array}{r} 0.375 \\ 8 \overline{) 3.00} \\ \underline{24} \\ 60 \\ \underline{56} \\ 40 \\ \underline{40} \\ \underline{ \times} \end{array}$$

$$(ii) 8 \div 3 = 2.666.....$$

Hence it is non-terminating decimal.

$$\begin{array}{r} 2.666..... \\ 3 \overline{) 8.000} \\ \underline{6} \\ 20 \\ \underline{18} \\ 20 \\ \underline{18} \\ 20 \\ \underline{18} \\ \underline{ 2} \end{array}$$

$$(iii) 6 \div 5 = 1.2$$

Hence it is terminating decimal.

$$\begin{array}{r} 1.2 \\ 5 \overline{) 6.0} \\ \underline{5} \\ 10 \\ \underline{10} \\ \hline \times \end{array}$$

$$(iv) 5 \div 6 = 0.8333.....$$

Hence it is non-terminating decimal.

$$\begin{array}{r} 0.8333..... \\ 6 \overline{) 5.0000} \\ \underline{48} \\ 20 \\ \underline{18} \\ 20 \\ \underline{18} \\ 20 \\ \underline{18} \\ 2 \end{array}$$

$$(v) 12.5 \div 4 = 3.125$$

Hence it is terminating decimal.

$$\begin{array}{r} 3.125 \\ 4 \overline{) 12.500} \\ \underline{12} \\ 5 \\ \underline{4} \\ 10 \\ \underline{8} \\ 20 \\ \underline{20} \\ \hline \times \end{array}$$

(vi) $23 \div 0.7 = 230 \div 7 = 32.8571428.....$

Hence it is non-terminating decimal. **Ans.**

$32.8571428.....$

$$\begin{array}{r}
 7 \overline{) 230.000000} \\
 \underline{21} \\
 20 \\
 \underline{14} \\
 60 \\
 \underline{56} \\
 40 \\
 \underline{35} \\
 50 \\
 \underline{49} \\
 10 \\
 \underline{7} \\
 30 \\
 \underline{28} \\
 20 \\
 \underline{14} \\
 60 \\
 \underline{56} \\
 4
 \end{array}$$

(vii) $42 \div 9 = 4.666.....$

Hence it is non-terminating decimal. **Ans.**

$4.666.....$

$$\begin{array}{r}
 9 \overline{) 42.000} \\
 \underline{36} \\
 60 \\
 \underline{54} \\
 60 \\
 \underline{54} \\
 60 \\
 \underline{54} \\
 6
 \end{array}$$

(viii) $0.56 \div 0.11 = 56 \div 11 = 5.0909.....$

Hence it is non-terminating decimal. **Ans.**

$$\begin{array}{r}
 5.0909..... \\
 11 \overline{) 56.0000} \\
 \underline{55} \\
 100 \\
 \underline{99} \\
 100 \\
 \underline{99} \\
 1
 \end{array}$$

Question 2.

Express as recurring decimals :

(i) $1\frac{1}{3}$

(ii) $\frac{10}{11}$

(iii) $\frac{5}{6}$

(iv) $\frac{2}{13}$

(v) $\frac{1}{9}$

(vi) $\frac{17}{90}$

(vii) $\frac{5}{18}$

(viii) $\frac{7}{12}$

Answer:

$$(i) 1\frac{1}{3} = \frac{4}{3} = 1.333.....$$
$$= 1.\bar{3} \text{ Ans.}$$

$$\begin{array}{r} 1.333..... \\ 3 \overline{) 4.000} \\ \underline{3} \\ 10 \\ \underline{9} \\ 10 \\ \underline{9} \\ 10 \\ \underline{9} \\ 1 \\ \underline{} \end{array}$$

$$(ii) \frac{10}{11} = 0.909090.....$$
$$= 0.\bar{90} \text{ Ans.}$$

$$\begin{array}{r} 0.909090..... \\ 11 \overline{) 10.0000000} \\ \underline{99} \\ 100 \\ \underline{99} \\ 100 \\ \underline{99} \\ 100 \\ \underline{99} \\ 1 \\ \underline{} \end{array}$$

$$(iii) \frac{5}{6} = 0.8333.....$$

$$\overline{6)5.0000(0.8333}$$

$$\underline{48}$$

$$\underline{20}$$

$$\underline{18}$$

$$\underline{20}$$

$$\underline{18}$$

$$\underline{20}$$

$$\underline{18}$$

$$\underline{2}$$

$$= 0.8\bar{3}$$

$$(iv) \frac{2}{13} = 0.153846153846... = 0.\overline{153846}$$

$$0.153846153846.....$$

$$13 \overline{) 2.000000000000}$$

$$\underline{13}$$

$$\underline{70}$$

$$\underline{65}$$

$$\underline{50}$$

$$\underline{39}$$

$$\underline{110}$$

$$\underline{104}$$

$$\underline{60}$$

$$\underline{52}$$

$$\underline{80}$$

$$\underline{78}$$

$$\underline{20}$$

$$\underline{13}$$

$$\underline{70}$$

$$\underline{65}$$

$$\underline{50}$$

$$\underline{39}$$

$$\underline{110}$$

$$\underline{104}$$

$$\underline{60}$$

$$\underline{52}$$

$$\underline{80}$$

$$\underline{78}$$

$$\underline{2}$$

$$(v) \frac{1}{9} = 0.1111.....$$

$$= 0.\overline{1} \text{ Ans.}$$

$$0.1111.....$$

$$9 \overline{) 1.0000}$$

$$10$$

$$9$$

$$10$$

$$9$$

$$10$$

$$9$$

$$1$$

$$(vi) \frac{17}{90} = 0.1888.....$$

$$= 0.\overline{18} \text{ Ans.}$$

$$0.1888.....$$

$$90 \overline{) 17.0000}$$

$$90$$

$$800$$

$$720$$

$$800$$

$$720$$

$$800$$

$$720$$

$$80$$

$$(vii) \frac{5}{18}$$

$$= 0.2777.....$$

$$18 \overline{)5.000}(0.2777$$

$$\begin{array}{r} 36 \\ \hline 140 \\ 126 \\ \hline 140 \\ 126 \\ \hline 14 \\ \hline \end{array}$$

$$= 0.2\bar{7}$$

$$(viii) \frac{7}{12}$$

$$= 0.58333.....$$

$$12 \overline{)7.0000}(0.58333$$

$$\begin{array}{r} 60 \\ \hline 100 \\ 96 \\ \hline 40 \\ 36 \\ \hline 40 \\ 36 \\ \hline 40 \\ 36 \\ \hline 4 \\ \hline \end{array}$$

$$= 0.58\bar{3}$$

Question 3.

Convert into vulgar fraction :

(i) $0.\bar{3}$

(ii) $0.\bar{8}$

(iii) $4.\bar{4}$

(iv) $23.\bar{7}$

Answer:

$$(i) \ 0.\bar{3} = \frac{3}{9}$$

$$= \frac{3-0}{9} = \frac{3}{9} = \frac{1}{3}$$

$$(ii) \ 0.\bar{8} = \frac{8}{9}$$

$$= \frac{8-0}{9} = \frac{8}{9}$$

$$(iii) \ 4.\bar{4} = \frac{44}{9}$$

$$= \frac{44-4}{9} = \frac{40}{9}$$

$$= 4\frac{4}{9}$$

$$(iv) \ 23.\bar{7} = \frac{237}{9}$$

$$= \frac{237-23}{9} = \frac{214}{9}$$

$$= 23\frac{7}{9}$$

Question 4.

Convert into vulgar fraction :

(i) $0.\overline{35}$

(ii) $2.\overline{23}$

(iii) $1.\overline{28}$

(iv) $5.\overline{234}$

Answer:

$$(i) \ 0.\overline{35} = \frac{35}{99}$$

$$= \frac{35-0}{99} = \frac{35}{99}$$

$$(ii) \ 2.\overline{23} = 2 + 0.\overline{23}$$

$$= 2 + \frac{23-0}{99}$$

$$= 2 + \frac{23}{99} = 2\frac{23}{99}$$

$$(iii) \ 1.\overline{28} = 1 + 0.\overline{28}$$

$$= 1 + \frac{28-0}{99}$$

$$= 1 + \frac{28}{99} = 1\frac{28}{99}$$

$$(iv) \ 5.\overline{234} = 5 + 0.\overline{234}$$

$$= 5 + \frac{234-0}{999} = 5\frac{234}{999}$$

Question 5.

Convert into vulgar fraction :

(i) $0.0\overline{37}$

(ii) $0.2\overline{45}$

(iii) $0.68\overline{5}$

(iv) $0.4\overline{42}$

Answer:

$$(i) 0.\overline{37} = \frac{37-3}{90}$$

$$= \frac{34}{90} = \frac{17}{45}$$

$$(ii) 0.\overline{245} = \frac{245-2}{990}$$

$$= \frac{243}{990} = \frac{81}{330}$$

$$= \frac{27}{110}$$

$$(iii) 0.\overline{685} = \frac{685-68}{900}$$

$$= \frac{617}{900}$$

$$(iv) 0.\overline{442} = \frac{442-4}{990}$$

$$= \frac{438}{990} = \frac{219}{495}$$

EXERCISE 4 (E)

Question 1.

Round off:

(i) 0.07, 0.112, 3.59, 9.489 to the nearest tenths.

(ii) 0.627, 100.479, 0.065 and 0.024 to the nearest hundredths.

(iii) 4.83, 0.86, 451.943 and 9.08 to the nearest whole number.

Answer:

(i) 0.07 = 0.1,

0.112 = 0.1

3.59 = 3.6, 9.489 = 9.5

(ii) $0.627 = 0.63$,
 $100.479 = 100.48$
 $0.065 = 0.07$,
 $0.024 = 0.02$
 (iii) $4.83 = 5$,
 $0.86 = 1$,
 $451.943 = 452$
 $9.08 = 9$

Question 2.

Simplify, and write your answers correct to the nearest hundredths :

- (i) 18.35×1.2
 (ii) 62.89×0.02

Answer:

(i) $18.35 \times 1.2 = 22.02$

$$\begin{array}{r} 18.35 \\ \times 1.2 \\ \hline 36.70 \\ 183.5 \times \\ \hline 22.020 \end{array}$$

(ii) $62.89 \times 0.02 = 1.2578 = 1.26$

$$\begin{array}{r} 62.89 \\ \times 0.02 \\ \hline 1.2578 \end{array}$$

Question 3.

Write the number of significant figures (digits) in:

- (i) 35.06
 (ii) 0.35
 (iii) 7.0068
 (iv) 19.0
 (v) 0.0062
 (vi) 0.42×0.6
 (vii) 0.08×25
 (viii) $3.6 \div 0.12$

Answer:

- (i) 35.06 : In this significant figures i.e. digits are 4
- (ii) In 0.35, significant figures are 2
- (iii) In 7.0068, significant figures are 5
- (iv) In 19.0, significant figures are 3
- (v) In 0.0062, significant figures are 2
- (vi) In $4.2 \times 0.6 = 2.52$, significant figure are 3
- (vii) In $008 \times 25 = 2.00$ = 2 significant figure is 1
- (viii) In $3.6 \div 0.12$ or $360 \div 12 = 30$, significant figure are 2.

Question 4.

Write :

- (i) 35.869, 0.008426, 4.952 and 382.7, correct to three significant figures.
- (ii) 60.974, 2.8753, 0.001789 and 400.04, correct to four significant figures.
- (iii) 14.29462, 19.2, 46356.82 and 69, correct to five significant figures.

Answer:

- (i) Correct to three significant figures are

$35.869 \rightarrow 35.9$

$0.008426 \rightarrow 0.00843$

$4.952 \rightarrow 4.95$

$382.7 \rightarrow 383$

- (ii) Correct to four significant figures

$60.974 \rightarrow 60.97$

$2.8753 \rightarrow 2.875$

$0.001789 \rightarrow 0.001789$

$400.04 \rightarrow 400.0$

- (iii) Correct to five significant figures

$14.29462 \rightarrow 14.295$

$19.2 \rightarrow 19.200$

$46356.82 \rightarrow 46357$

$69 \rightarrow 69.000$

EXERCISE 4 (F)

Question 1.

The weight of an object is 3.06 kg. Find the total weight of 48 similar objects.

Answer:

Weight of one object = 3.06 kg.

$$\begin{aligned}\therefore \text{Weight of 48 objects} &= 3.06 \times 48 \\ &= 146.88 \text{ kg. Ans.}\end{aligned}$$

$$\begin{array}{r} 3.06 \\ \times 48 \\ \hline 2448 \\ 1224 \times \\ \hline 14688 \end{array}$$

Question 2.

Find the cost of 17.5 m cloth at the rate of Rs. 112.50 per metre.

Answer:

Cost of 1 metre cloth = Rs. 112.50

$$\begin{aligned}\therefore \text{Cost of 17.5 m cloth} \\ &= \text{Rs. } 112.50 \times 17.5 \\ &= \text{Rs. } 1968.750 \\ &= 1968.75 \text{ Ans.}\end{aligned}$$

$$\begin{array}{r} 112.50 \\ 17.5 \\ \hline 56250 \\ 78750 \times \\ 11250 \times \times \\ \hline 1968750 \end{array}$$

Question 3.

One kilogramme of oil costs Rs. 73.40. Find the cost of 9.75 kilogramme of the oil.

Answer:

Cost of 1 kg oil = Rs. 73.40

$$\begin{aligned}\therefore \text{Cost of 9.75 kg oil} &= \text{Rs. } 73.40 \times 9.75 \\ &= \text{Rs. } 715.6500 \\ &= \text{Rs. } 715.65 \text{ Ans.}\end{aligned}$$

$$\begin{array}{r} 73.40 \\ \times 9.75 \\ \hline 36700 \\ 51380 \times \\ 66060 \times \times \\ \hline 7156500 \end{array}$$

Question 4.

Total weight of 8 identical objects is 51.2 kg. Find the weight of each object.

Answer:

Weight of 8 objects = 51.2 kg

$\therefore$ Weight of 1 object = $51.2 \div 8$ kg = 6.4 kg Ans.

Question 5.

18.5 m of cloth costs Rs. 666. Find the cost of 3.8 m cloth.

Answer:

Cost of 18.5 m cloth = Rs. 666

Cost of 1 m cloth = Rs. $666 \div 18.5$ and cost of 3.8 m cloth

= Rs. $(666 \div 18.5) \times 3.8$ = Rs. $(6660 \div 185) \times 3.8$ = Rs. 36×3.8 = Rs. 136.80

$$\begin{array}{r} 36 \\ 185 \overline{) 6660} \\ \underline{555} \\ 1110 \\ \underline{1110} \\ \times \\ \hline 38 \\ \times 36 \\ \hline 228 \\ 114 \times \\ \hline 1368 \end{array}$$

Question 6.

Find the value of:

(i) 0.5 of Rs. 7.60 + 1.62 of Rs. 30

(ii) 2.3 of 7.3 kg + 0.9 of 0.48 kg

(iii) 6.25 of 8.4 – 4.7 of 3.24

(iv) 0.98 of 235 – 0.09 of 3.2

Answer:

(i) 0.5 of Rs. 7.60 + 1.62 of Rs. 30

$$= \text{Rs. } 3.80 + \text{Rs. } 48.60$$

$$= \text{Rs. } 52.40 \text{ Ans.}$$

$$\begin{array}{r} 7.60 \\ \times 0.5 \\ \hline 3.800 \end{array} \qquad \begin{array}{r} 1.62 \\ \times 30 \\ \hline 48.60 \end{array}$$

(ii) 2.3 of 7.3 kg + 0.9 of 0.48 kg

$$= 16.79 \text{ kg} + 0.432 \text{ kg} = 17.222 \text{ kg Ans.}$$

$$\begin{array}{r} 7.3 \\ \times 2.3 \\ \hline 219 \\ 146 \times \\ \hline 1679 \end{array} \qquad \begin{array}{r} 0.48 \\ \times 0.9 \\ \hline 0.432 \end{array} \qquad \begin{array}{r} 16.790 \\ + 0.432 \\ \hline 17.222 \end{array}$$

(iii) 6.25 of 8.4 – 4.7 of 3.24

$$= 52.500 - 15.228 = 37.272 \text{ Ans.}$$

$$\begin{array}{r} 6.25 \\ \times 8.4 \\ \hline 2500 \\ 5000 \times \\ \hline 52500 \end{array} \qquad \begin{array}{r} 3.24 \\ \times 4.7 \\ \hline 2268 \\ 1296 \times \\ \hline 15228 \end{array}$$

(iv) 0.98 of 235 – 0.09 of 3.2 = 230.30 – 0.288

$$= 230.012 \text{ Ans.}$$

$$\begin{array}{r} 235 \\ \times 0.98 \\ \hline 1880 \\ 2115 \times \\ \hline 23030 \end{array} \qquad \begin{array}{r} 230.300 \\ - 0.288 \\ \hline 230.012 \end{array} \qquad \begin{array}{r} 3.20 \\ \times 0.09 \\ \hline 0.2880 \end{array}$$

Question 7.

Evaluate:

(i) $5.6 - 1.5$ of 3.4

(ii) $4.8 \div 0.04$ of 5

(iii) 0.72 of $80 \div 0.2$

(iv) $0.72 \div 80$ of 0.2

(v) $6.45 + (3.9 - 1.75)$

(vi) 0.12 of $(0.104 - 0.02) + 0.36 \times 0.5$

Answer:

(i) $5.6 - 1.5$ of $3.4 = 5.6 - 5.1$

$$\begin{array}{r} 3.4 \\ \times 1.5 \\ \hline 170 \\ 34 \times \\ \hline 5.10 \end{array}$$

$= 5.6 - 5.1 = 0.5$ Ans.

(ii) $4.8 \div 0.04$ of $5 = 4.8 \div 0.20$

$= 4.8 \div 0.2 = 48 \div 2 = 24$ Ans.

(iii) 0.72 of $80 \div 0.2 = 57.60 \div 0.2$

$= 57.6 \div 0.2 = 576 \div 2 = 288$ Ans.

(iv) $0.72 \div 80$ of $0.2 = 0.72 \div 16.0$

$= 0.72 \div 16 = 72 \div 1600$

$$\begin{array}{r} 0.045 \\ 1600 \overline{) 72,000} \cdot 045 \\ \underline{-6400} \\ 8000 \\ \underline{-8000} \\ \hline \times \end{array}$$

$= 0.045$ Ans.

(v) $6.45 \div (3.9 - 1.75) = 6.45 \div (3.90 - 1.75)$

$= 6.45 \div 2.15 = 645 \div 215 = 3$ Ans.

$$\begin{array}{r} 3 \\ 215 \overline{) 645} \\ \underline{-645} \\ \hline \times \end{array}$$

(vi) 0.12 of $(0.104 - 0.02) + 0.36 \times 0.5$

$= 0.12$ of $0.084 + 0.36 \times 0.5$

$= 0.01008 + 0.180 = 0.19008$ Ans.

$$\begin{array}{r} 0.104 \\ - 0.020 \\ \hline 0.084 \end{array} \quad \begin{array}{r} .084 \\ \times .12 \\ \hline 0.01008 \end{array} \quad \begin{array}{r} 0.01008 \\ + 0.180 \\ \hline 0.19008 \end{array}$$