Short Answer Type Questions

	Size	20	21	2	22	23		24	_			
	Frequency	6	4	5		1		4	_			
Sol.	Size	Frequency	Frequency $f_i x_i$ $d_i = x_i - x $			f _i d _i						
	20	6	12	0		1.65		9.90	_			
	21	4 84 0.65						2.60				
	22	5	11	110 0.35).35	1.75					
	23	1	2	23		1.35		1.35				
	24	4	90	5	2	2.35		9.40				
	Total	20	43	3				25				
١	Now,	$\overline{x} = \frac{\sum f_i x_i}{\sum f_i} = \frac{433}{20} = 21.65$										
		$MD = \frac{\sum f_i x_i - \bar{x} }{\sum f_i} = \frac{25}{20} = 1.25$										

Q. 1 Find the mean deviation about the mean of the distribution.

Q. 2 Find the mean deviation about the median of the following distribution.

-						-
	Marks obtained	10	11	12	14	15
	Number of students	2	3	8	3	4
Sol.	Marks obtained	f _i	cf	$d_i = x_i $	- M _e	f _i d _i
	10	2	2	2		4
	11	3	5	1		3
	12	8	13	0		0
	14	3	16	2		6
	15	4	20	3		12
	Total	$\sum f_i = 20$				$\sum f_i d_i = 25$

Now,

$$M_e = \left(\frac{20+1}{2}\right) \text{th item } = \left(\frac{21}{2}\right) = 10.5 \text{ th item}$$

$$\therefore \qquad M_e = 12$$

$$\therefore \qquad \text{MD} = \frac{\sum f_i d_i}{\sum f_i} = \frac{25}{20} = 1.25$$

Q. 3 Calculate the mean deviation about the mean of the set of first *n* natural numbers when *n* is an odd number.

Sol. Consider first natural number when *n* is an odd *i.e.*, 1, 2, 3, 4, ..., [odd].

Mean
$$\overline{x} = \frac{1+2+3+...+n}{n} = \frac{n(n+1)}{2n} = \frac{n+1}{2}$$

$$\therefore MD = \frac{\left|1-\frac{n+1}{2}\right| + \left|2-\frac{n+1}{2}\right| + \left|3-\frac{n+1}{2}\right| + ...+\left|n-\frac{n+1}{2}\right|}{n}$$

$$= \frac{+\left|\frac{n+1}{2}-\frac{n+1}{2}\right| + \left|\frac{n+3}{2}-\frac{n+1}{2}\right| + ...+\left|\frac{2n-2}{2}-\frac{n+1}{2}\right| + \left|n-\frac{n+1}{2}\right|}{n}$$

$$= \frac{2n\left[1+2+...+\frac{n-3}{2}+\frac{n-1}{2}\right] \left(\frac{n-1}{2}\right) \text{ terms}}{n}$$

$$= \frac{2}{n}\left[\frac{\left(\frac{n-1}{2}\right)\left(\frac{n-1}{2}+1\right)}{2}\right] \left[\because \text{ sum of first } n \text{ natural numbers} = \frac{n(n+1)}{2}\right]$$

$$= \frac{2}{n} \cdot \frac{1}{2}\left[\left(\frac{n-1}{2}\right)\left(\frac{n+1}{2}\right)\right] = \frac{1}{n}\left(\frac{n^2-1}{4}\right) = \frac{n^2-1}{4n}$$

Q. 4 Calculate the mean deviation about the mean of the set of first n natural numbers when *n* is an even number.

$$\therefore \qquad \text{Mean } \overline{x} = \frac{1+2+3+\ldots+n}{n} = \frac{n(n+1)}{2n} = \frac{n+1}{2}$$

$$\text{MD} = \frac{1}{n} \left[\left| 1 - \frac{n+1}{2} \right| + \left| 2 - \frac{n+1}{2} \right| + \left| 3 - \frac{n+1}{2} \right| \right] + \left| \frac{n-2}{2} - \frac{n+1}{2} \right| + \left| \frac{n}{2} - \frac{n+1}{2} \right|$$

$$+ \left| \frac{n+2}{2} - \frac{n+1}{2} \right| + \ldots + \left| n - \frac{n+1}{2} \right|$$

$$= \frac{1}{n} \left[\left| \frac{1-n}{2} \right| + \left| \frac{3-n}{2} \right| + \left| \frac{5-n}{2} \right| + \ldots + \left| \frac{-3}{2} \right| + \left| \frac{1}{2} \right| + \ldots + \left| \frac{n-1}{2} \right| \right]$$

$$= \frac{2}{n} \left[\frac{1}{2} + \frac{3}{2} + \ldots + \frac{n-1}{2} \right] \left(\frac{n}{2} \right) \text{ terms}$$

$$= \frac{1}{n} \cdot \left(\frac{n}{2} \right)^2 \qquad [\because \text{ sum of first } n \text{ natural numbers } = n^2]$$

$$= \frac{1}{n} \cdot \frac{n^2}{4} = \frac{n}{4}$$

Sol.	x_i	1	2	3	4	5			n					
x_i^2 1 4 9 16 25														
	Now,	Now, $\sum x_i = 1 + 2 + 3 + 4 + \dots + n = \frac{n(n+1)}{2}$												
	and	$\sum x_i^2 = 1^2 + 2^2 + 3^2 + \dots + n^2 = \frac{n(n+1)(2n+1)}{6}$												
	÷		$\sigma = \sqrt{\frac{\sum x_i^2}{N} - \left(\frac{\sum x_i}{N}\right)^2}$											
			$=\sqrt{\frac{n(n)}{n(n)}}$	n + 1)(2 <i>n</i> 6n	<u>+ 1)</u> _ <u>r</u>	$\frac{n^2(n+1)^2}{4n^2}$								
			$=\sqrt{\frac{(n-1)^{n-1}}{n}}$	+ 1)(2 <i>n</i> + 6	<u>+ 1)</u> _ <u>(n -</u>	+ 1) ² 4								
			$=\sqrt{\frac{2(2}{2})}$	2 <i>n</i> ² + 3 <i>r</i>	n + 1) - 3 12	(n ² + 2 n	+ 1)							
		$=\sqrt{\frac{4n^2+6n+2-3n^2-6n-3}{12}}$												
			$=\sqrt{\frac{n^2}{n^2}}$	<u> </u>										

Q. 5 Find the standard deviation of first *n* natural numbers.

Q. 6 The mean and standard deviation of some data for the time taken to complete a test are calculated with the following results Number of observation = 25, mean = 18.2 s, standard, deviation = 3.25 s Further, another set of 15 observations $x_1 x_2 \dots x_{15}$, also in seconds, is now available and we have $\sum_{i=1}^{15} x_i = 279$ and $\sum_{i=1}^{15} x_i^2 = 5524$. Calculate the standard devivation based on all 60 observations

standard derivation based on all 40 observations.

Sol. Given,

$$n_i = 25, \overline{x}_i = 18.2, \sigma_1 = 3.25,$$

 $n_2 = 15, \sum_{i=1}^{15} x_i = 279 \text{ and } \sum_{i=1}^{15} x_i^2 = 5524$
For first set,
 $\Sigma x_i = 25 \times 18.2 = 455$
 \therefore
 $\sigma_1^2 = \frac{\Sigma x_i^2}{25} - (18.2)^2$
 \Rightarrow
 $(3.25)^2 = \frac{\Sigma x_i^2}{25} - 331.24$
 \Rightarrow
 $10.5625 + 331.24 = \frac{\Sigma x_i^2}{25}$
 \Rightarrow
 $\Sigma x_i^2 = 25 \times (10.5625 + 331.24)$
 $= 25 \times 341.8025$
 $= 8545.0625$

For combined SD of the 40 observations n = 40,

Now and

:..

$$\Sigma x_i^2 = 5524 + 8545.0625 = 14069.0625$$

$$\Sigma x_i = 455 + 279 = 734$$

$$SD = \sqrt{\frac{14069.0625}{40} - \left(\frac{734}{40}\right)^2}$$

$$= \sqrt{351.726 - (18.35)^2}$$

$$= \sqrt{351.726 - 336.7225}$$

$$= \sqrt{15.0035} = 3.87$$

Q. 7 The mean and standard deviation of a set of n_1 observations are \overline{x}_1 and s_1 , respectively while the mean and standard deviation of another set of n_2 observations are \overline{x}_2 and s_2 , respectively. Show that the standard deviation of the combined set of $(n_1 + n_2)$ observations is given by

$$SD = \sqrt{\frac{n_1(s_1)^2 + n_2(s_2)^2}{n_1 + n_2}} + \frac{n_1n_2(\overline{x}_1 - \overline{x}_2)^2}{(n_1 - n_2)^2}.$$
$$x_{i}, i = 1, 2, 3 \dots, n_1 \text{ and } y_{j}, j = 1, 2, 3, \dots, n_2$$
$$\overline{x}_1 = \frac{1}{n_1} \sum_{j=1}^{n_1} x_j \text{ and } \overline{x}_2 = \frac{1}{n_2} \sum_{j=1}^{n_2} y_j$$

Sol. Let

$$\overline{x}_{1} = \frac{1}{n_{1}} \sum_{i=1}^{n_{1}} x_{i} \text{ and } \overline{x}_{2} = \frac{1}{n_{2}}$$
$$\sigma_{1}^{2} = \frac{1}{n_{1}} \sum_{i=1}^{n_{1}} (x_{i} - \overline{x}_{1})^{2}$$

 \Rightarrow and

:..

 $\sigma_2^2 = \frac{1}{n_2} \sum_{j=1}^n (y_j - \overline{x}_2)^2$

Now, mean \overline{x} of the given series is given by

$$\overline{x} = \frac{1}{n_1 + n_2} \left[\sum_{i=1}^{n_1} x_i + \sum_{j=1}^{n_2} y_j \right] = \frac{n_1 \, \overline{x}_1 + n_2 \, \overline{x}_2}{n_1 + n_2}$$

The variance σ^2 of the combined series is given by

 n_1

$$\sigma^{2} = \frac{1}{n_{1} + n_{2}} \left[\sum_{i=1}^{n_{1}} (x_{i} - \overline{x})^{2} + \sum_{j=1}^{n_{2}} (y_{j} - \overline{x})^{2} \right]$$
$$\sum_{i=1}^{n_{1}} (x_{i} - \overline{x})^{2} = \sum_{i=1}^{n_{1}} (x_{i} - \overline{x}_{j} + \overline{x}_{j} - \overline{x})^{2}$$

Now.

$$\sum_{i=1}^{n} (x_i - \overline{x})^2 = \sum_{i=1}^{n} (x_i - \overline{x}_j + \overline{x}_j - \overline{x})^2$$
$$= \sum_{i=1}^{n} (x_i - \overline{x}_j)^2 + n_1 (\overline{x}_j - \overline{x})^2 + 2(\overline{x}_j - \overline{x}) \sum_{i=1}^{n} (x_i - \overline{x}_j)^2$$
$$\sum_{i=1}^{n} (x_i - \overline{x}_i) = 0$$

But

[algebraic sum of the deviation of values of first series from their mean is zero]

$$\sum_{i=1}^{1} (x_i - \bar{x})^2 = n_1 s_1^2 + n_1 (\bar{x}_1 - \bar{x})^2 = n_1 s_1^2 + n_1 d_1^2$$
$$d_1 = (\bar{x}_1 - \bar{x})$$

Where.

Simil

and

:..

$$\begin{aligned} \text{Similarly,} \qquad \sum_{j=1}^{n_2} (y_j - \bar{x})^2 &= \sum_{j=1}^{n_2} (y_j - \bar{x}_j + \bar{x}_i - \bar{x})^2 = n_2 s_2^2 + n_2 d_2^2 \\ \text{where,} \qquad d_2 &= \bar{x}_2 - \bar{x} \\ \text{Combined SD,} \qquad \sigma &= \sqrt{\frac{[n_1(s_1^2 + d_1^2) + n_2(s_2^2 + d_2^2)]}{n_1 + n_2}} \\ \text{where,} \qquad d_1 &= \bar{x}_1 - \bar{x} = \bar{x}_1 - \left(\frac{n_1 \bar{x}_1 + n_2 \bar{x}_2}{n_1 + n_2}\right) = \frac{n_2(\bar{x}_1 - \bar{x}_2)}{n_1 + n_2} \\ \text{and} \qquad d_2 &= \bar{x}_2 - \bar{x} = \bar{x}_2 - \frac{n_1 \bar{x}_1 + n_2 \bar{x}_2}{n_1 + n_2} = \frac{n_1(\bar{x}_2 - \bar{x}_1)}{n_1 + n_2} \\ \therefore \qquad \sigma^2 &= \frac{1}{n_1 + n_2} \left[n_1 s_1^2 + n_2 s_2^2 + \frac{n_1 n_2 (\bar{x}_1 - \bar{x}_2)^2}{(n_1 + n_2)^2} + \frac{n_2 n_1 (\bar{x}_2 - \bar{x}_1)^2}{(n_1 + n_2)^2}\right] \\ \text{Also,} \qquad \sigma &= \sqrt{\frac{n_1 s_1^2 + n_2 s_2^2}{n_1 + n_2}} + \frac{n_1 n_2 (\bar{x}_1 - \bar{x}_2)^2}{(n_1 + n_2)^2} \end{aligned}$$

Q. 8 Two sets each of 20 observations, have the same standard deviation 5. The first set has a mean 17 and the second mean 22. Determine the standard deviation of the *x* sets obtained by combining the given two sets.

Sol. Given,
$$n_1 = 20$$
, $\sigma_1 = 5$, $\overline{x}_1 = 17$ and $n_2 = 20$, $\sigma_2 = 5$, $\overline{x}_2 = 22$
We know that, $\sigma = \sqrt{\frac{n_1 s_1^2 + n_2 s_2^2}{n_1 + n_2} + \frac{n_1 n_2 (\overline{x}_1 - \overline{x}_2)^2}{(n_1 + n_2)^2}}$
 $= \sqrt{\frac{20 \times (5)^2 + 20 \times (5)^2}{20 + 20} + \frac{20 \times 20 (17 - 22)^2}{(20 + 20)^2}}$
 $= \sqrt{\frac{1000}{40} + \frac{400 \times 25}{1600}} = \sqrt{25 + \frac{25}{4}} = \sqrt{\frac{125}{4}} = \sqrt{31.25} = 5.59$

Q.9 The frequency distribution

-	x	А	2A	3A	4A	5A	6A
	f	2	1	1	1	1	1

where, A is a positive integer, has a variance of 160. Determine the value of A.

Sol.

x	f _i	$f_i x_i$	$f_i x_i^2$
A	2	2A	2A ²
2A	1	2A	4A ²
3A	1	3A	9A ²
4A	1	4 <i>A</i>	16A ²
5A	1	5A	25A ²
6A	1	6A	36A ²
Total	7	22A	92A ²
	n = 7	$\Sigma f_i n_i = 22A$	$\Sigma f_i n_i^2 = 92A^2$

$$\therefore \qquad \sigma^2 = \frac{\Sigma f_i x_i^2}{n} - \left(\frac{\Sigma f_i x_i}{n}\right)^2$$

$$\Rightarrow \qquad 160 = \frac{92A^2}{7} - \left(\frac{22A}{7}\right)^2$$

$$\Rightarrow \qquad 160 = \frac{92A^2}{7} - \frac{484A^2}{49}$$

$$\Rightarrow \qquad 160 = (644 - 484)\frac{A^2}{49}$$

$$\Rightarrow \qquad 160 = \frac{160A^2}{49} \Rightarrow A^2 = 49$$

$$\therefore \qquad A = 7$$

Q. 10 For the frequency distribution

x	2	3	4	5	6	7
f	4	9	16	14	11	6

Find the standard distribution.

Sol.

x _i	f _i	$d_i = x_i - 4$	f _i d _i	$f_i d_i^2$					
2	4	-2	-8	16					
3	9	-1	-9	9					
4	16	0	0	0					
5	14	1	14	14					
6	11	2	22	44					
7	6	3	18	54					
Total	60		$\Sigma f_i d_i = 37$	$\Sigma f_i d_i^2 = 137$					
$\therefore \qquad SD = \sqrt{\frac{\Sigma f_i d_i^2}{N} - \left(\frac{\Sigma f_i d_i}{N}\right)^2}$ $= \sqrt{\frac{137}{60} - \left(\frac{37}{60}\right)^2}$									
$= \sqrt{2.2833 - (0.616)^2}$									
	•	33 – 0.3794							
		37 = 1.38							

Q. 11 There are 60 students in a class. The following is the frquency distribution of the marks obtained by the students in a test.

Marks	0	1	2	3	4	5
Frequency	x -2	x	<i>x</i> ²	$(x+1)^2$	2 x	<i>x</i> +1

where, \boldsymbol{x} is positive integer. Determine the mean and standard deviation of the marks

Sol. : Sum of frequencies, $x - 2 + x + x^{2} + (x + 1)^{2} + 2x + x + 1 = 60$ $2x - 2 + x^{2} + x^{2} + 1 + 2x + 2x + x + 1 = 60$ \Rightarrow $2x^2 + 7x = 60$ \Rightarrow $2x^2 + 7x - 60 = 0$ \Rightarrow $2x^2 + 15x - 8x - 60 = 0$ \Rightarrow x (2x + 15) - 4 (2x + 15) = 0 \Rightarrow (2x + 15)(x - 4) = 0 \Rightarrow $x = -\frac{15}{2}, 4$ \Rightarrow $x = -\frac{15}{2}$ [inaddmisible] [:: $x \in I^+$] \Rightarrow $f_i d_i^2$ $d_i = x_i - 3$ f_id_i f, x_i 0 2 -3 -6 18 -2 1 4 -8 16 2 -1 -16 16 16 0 0 A = 325 0 4 8 1 8 8 5 5 2 20 10 $\Sigma f_i d_i = -12$ $\Sigma f_i d_i^2 = 78$ $\Sigma f_i = 60$ Total Mean = $A + \frac{\Sigma f_i d_i}{\Sigma f_i} = 3 + \left(\frac{-12}{60}\right) = 2.8$ $\sigma = \sqrt{\frac{\Sigma f_i d_i^2}{\Sigma f_i} - \left(\frac{\Sigma f_i d_i}{\Sigma f_i}\right)^2} = \sqrt{\frac{78}{60} - \left(\frac{-12}{60}\right)^2}$ $=\sqrt{1.3-0.04}=\sqrt{1.26}=1.12$

Q. 12 The mean life of a sample of 60 bulbs was 650 h and the standard deviation was 8 h. If a second sample of 80 bulbs has a mean life of 660 h and standard deviation 7 h, then find the over all standard deviation.

Sol. Here,
$$n_1 = 60$$
, $\overline{x}_1 = 650$, $s_1 = 8$ and $n_2 = 80$, $\overline{x}_2 = 660$, $s_2 = 7$

$$\therefore \qquad \sigma = \sqrt{\frac{n_1 s_1^2 + n_2 s_2^2}{n_1 + n_2} + \frac{n_1 n_2 (\bar{x}_1 - \bar{x}_2)^2}{(n_1 + n_2)^2}}$$
$$= \sqrt{\frac{60 \times (8)^2 + 80 \times (7)^2}{60 + 80} + \frac{60 \times 80(650 - 660)^2}{(60 + 80)^2}}$$
$$= \sqrt{\frac{6 \times 64 + 8 \times 49}{14} + \frac{60 \times 80 \times 100}{140 \times 140}}$$
$$= \sqrt{\frac{192 + 196}{7} + \frac{1200}{49}} = \sqrt{\frac{388}{7} + \frac{1200}{49}}$$
$$= \sqrt{\frac{2716 + 1200}{49}} = \sqrt{\frac{3916}{49}} = \frac{62.58}{7} = 8.9$$

Q. 13 If mean and standard deviation of 100 items are 50 and 4 respectively, then find the sum of all the item and the sum of the squares of item.

- **Sol.** Here, $\overline{x} = 50$, n = 100 and $\sigma = 4$ \therefore $\frac{\Sigma x_i}{100} = 50$ \Rightarrow $\Sigma x_i = 5000$ and $\sigma^2 = \frac{\Sigma f_i x_i^2}{\Sigma f_i} - \left(\frac{\Sigma f_i x_i}{\Sigma f_i}\right)^2$ \Rightarrow $(4)^2 = \frac{\Sigma f_i x_i^2}{100} - (50)^2$ \Rightarrow $16 = \frac{\Sigma f_i x_i^2}{100} - 2500$ \Rightarrow $\frac{\Sigma f_i x_i^2}{100} = 16 + 2500 = 2516$ \therefore $\Sigma f_i x_i^2 = 251600$
- **Q.** 14 If for distribution $\Sigma(x-5) = 3$, $\Sigma(x-5)^2 = 43$ and total number of item is 18. Find the mean and standard deviation.
- Sol. Given, $n = 18, \Sigma(x - 5) = 3 \text{ and } \Sigma(x - 5)^2 = 43$ \therefore Mean $= A + \frac{\Sigma(x - 5)}{18}$ $= 5 + \frac{3}{18} = 5 + 0.1666 = 5.1666 = 5.17$ and $SD = \sqrt{\frac{\Sigma(x - 5)^2}{n} - \left(\frac{\Sigma(x - 5)}{n}\right)^2}$ $= \sqrt{\frac{43}{18} - \left(\frac{3}{18}\right)^2}$ $= \sqrt{2.3944 - (0.166)^2} = \sqrt{2.3944 - 0.2755} = 1.59$

Q. 15 Find the mean and variance of the frequency distribution given below.

	x	$1 \le x \le 3$	$3 \le x \le$	5 $5 \le x \le 7$	$7 \le x \le 10$
	f	6	4	5	1
Cal					
Sol.	x	f _i	x _i	$f_i x_i$	$f_i x_i^2$
	1-3	6	2	12	24
	3-5	4	4	16	64
	5-7	5	6	30	180
	7-10	1	8.5	8.5	72.25
	Total	n=16		$\Sigma f_i x_i = 66.5$	$\Sigma f_i x_i^2 = 340.25$
:		Mea	$\ln = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{6}{2}$	$\frac{66.5}{16} = 4.15$	

and

variance =
$$\sigma^2 = \frac{\Sigma f_i x_i^2}{\Sigma f_i} - \left(\frac{\Sigma f_i x_i}{\Sigma f_i}\right)^2$$

= $\frac{340.25}{16} - (4.15)^2$
= 21.2656 - 17.2225 = 4.043

Long Answer Type Questions

Q. 16 Calculate the mean deviation about the mean for the following frequency distribution.

Class int	erval	0-4		4-8		8-12	12-	16	16-20			
Frequ	ency	4		6		8	5		2			
Class internal		fi		xi		$f_i x_i$	$d_i = x $	$ -\overline{x} $	f _i d _i			
0-4		4		2		8	7.	2	28.8			
4-8		6 8		6	36	36	3.2 0.8		19.2			
8-12				10		80			6.4			
12-16		5		14		70	4.	8	24.0			
16-20		2		18		36	8.8	8	17.6			
Total	$\Sigma f_i =$	=25			Σf_i	x _i = 230			$\Sigma f_i d_i = 96$			
<i>.</i>		Mean $= \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{230}{25} = 9.2$										
and		mean deviation $= \frac{\Sigma f_i}{\Sigma f_i} = \frac{96}{25} = 3.84$										

Q. 17 Calculate the mean deviation from the median of the following data.

	Class inte	rval	0-6	6-12	2	12	-18	18-24	24-30
	Frequer	icy	4	4 5		3		6	2
Sol.	Class interval	Class interval f _i 0-6 4 6-12 5		x _i		cf		$x_i - \overline{m_d}$	f _i d _i
	0-6			3	4		11		44
	6-12			9	0	9	5		25
	12-18	3	1	5	12 18 20			1	3
	18-24	6	2	21			7 13		42
	24-30	2	2	27					26
	Total							$\Sigma f_i d_i = 140$	
			<u>N</u> 2	$=\frac{20}{2}=\frac{1}{2}$	10				

So, the median class is 12-18.

Median =
$$l + \frac{\frac{N}{2} - cf}{f} \times i$$

= $12 + \frac{6}{3}(10 - 9)$
= $12 + 2 = 14$
MD = $\frac{\Sigma f_i d_i}{\Sigma f_i} = \frac{140}{20} = 7$

Q. 18 Determine	the	mean	and	standard	deviation	for	the	following
distributior	ı .							

Marks	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
Frequency	1	6	6	8	8	2	2	3	0	2	1	0	0	0	1
Marks		f _i		$f_i x_i$		d -	- x _i –	-	f _i	d		f _i d	2		
Marks		'i		$I_i \lambda_i$		<i>u_i</i> –	$-x_i$ –	<i>x</i>	'i	ui		I _i u	i		
2		1		2		2 –	6 = -4	4	-	4		16	5		
3		6		18		3 —	6 = -	3	-	18		54	1		
4		6		24		4 -	6 = -2	2	_	12		24	1		
5		8		40		5 —	б=-	1	_	8		8			
6		8		48		6-	6=0		()		0			
7		2		14		7 –	6 = 1		-	2		2			
8		2		16		8-	6=2		2	1		8			
9		3		27		9 -	6=3		Q	9		27	7		
10		0		0		10 -	-6=4	1	()		0			
11		2		22		11 -	-6=5	5	1	0		50)		
12		1		12		12 -	-6=6	5	6	5		36	5		
13		0		0		13 -	-6=7	7	()		0			
14		0		0		14 -	-6=8	3	()		0			
15		0		0		15 -	-6=9)	()		0			
16		1		16		16 -	-6=	0	1	0		10	0		
Total	Σf_i	=40	Σ	$x_i = x_i$	239				$\Sigma f_i d_i$	=-1	Σ	$f_i x_i^2$	= 325	-	
					Σf	. 0	20								

Mean
$$\overline{x} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{239}{40} = 5.975 \approx 6$$

and
$$\sigma = \sqrt{\frac{\Sigma f_i d_i^2}{\Sigma f_i} - \left(\frac{\Sigma f_i d_i}{\Sigma f_i}\right)^2} = \sqrt{\frac{325}{40} - \left(\frac{-1}{40}\right)^2}$$
$$= \sqrt{8.125 - 0.000625} = \sqrt{8.124375} = 2.85$$

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Q. 19 The weights of coffee in 70 jars is shown in the following table

Weight (in g)	Frequency
200-201	13
201-202	27
202-203	18
203-204	10
204-205	1
205-206	1

Determine variance and standard deviation of the above distribution.

6.1								
Sol.	CI	f _i	x_i	$d_i = x_i - \overline{x}$	f _i d _i	$f_i d_i^2$		
	200-201	13	200.5	-2	-26	52		
	201-202	27	201.5	-1	-27	27		
	202-203	18	202.5	0	0	0		
	203-204	10	203.5	1	10	10		
	204-205	1	204.5	2	2	4		
	205-206	1	205.5	3	3	9		
		$\Sigma f_i = 70$			$\sum f_i d_i = -38$	$\Sigma f_i d_i^2 = 102$		
	.:.	$\sigma^2 = \frac{\Sigma f_i d_i^2}{\Sigma f_i} - \left(\frac{\Sigma f_i d_i}{\Sigma f_i}\right)^2 = \frac{102}{70} - \left(\frac{-38}{70}\right)^2$						
	Now,	=1.4571 - 0.2916 = 1.1655 $\sigma = \sqrt{1.1655} = 1.08 \text{ g}$						

Q. 20 Determine mean and standard deviation of first *n* terms of an AP whose first term is a and common difference is *d*.

Cal			
Sol.	x_i	$x_i - a$	$(x_{i} - a)^{2}$
	a	0	0
	a + d	d	d^2
	a + 2d	2 <i>d</i>	$4d^2$
			$9d^2$
	a + (n - 1)d	(n – 1)d	$(n-1)^2 d^2$
	$\Sigma x_i = \frac{n}{2} [2a + (n-1)]$		
÷	Mean = $\frac{\Sigma}{M}$	$\frac{1}{n} = \frac{1}{n} \left[\frac{n}{2} (2a + (n - 1)) \right]$	d]
	= a	$+\frac{(n-1)}{2}d$	

:..

and

$$\begin{split} \Sigma(x_i - a) &= d \left[1 + 2 + 3 + \dots + (n - 1)d \right] \\ &= d \frac{(n - 1)n}{2} \\ \Sigma(x_i - a)^2 &= d^2 \left[1^2 + 2^2 + 3^2 + \dots + (n - 1)^2 \right] \\ &= \frac{d^2(n - 1)n(2n - 1)}{6} \\ \sigma &= \sqrt{\frac{(x_i - a)^2}{n} - \left(\frac{x_i - a}{n}\right)^2} \\ &= \sqrt{\frac{d^2(n - 1)(n)(2n - 1)}{6n} - \left[\frac{d(n - 1)n}{2n}\right]^2} \\ &= \sqrt{\frac{d^2(n - 1)(2n - 1)}{6} - \frac{d^2(n - 1)^2}{4}} \\ &= d\sqrt{\frac{(n - 1)(2n - 1)}{6} - \frac{(n - 1)^2}{4}} \\ &= d\sqrt{\frac{(n - 1)(2n - 1)}{2} - \frac{(n - 1)^2}{4}} \\ &= d\sqrt{\frac{(n - 1)}{2} \left(\frac{2n - 1}{3} - \frac{n - 1}{2}\right)} \\ &= d\sqrt{\frac{(n - 1)(n + 1)}{2}} = d\sqrt{\frac{(n^2 - 1)}{12}} \end{split}$$

Q. 21 Following are the marks obtained, out of 100, by two students Ravi and Hashina in 10 tests

Ravi	25	50	45	30	70	42	36	48	35	60
Hashina	10	70	50	20	95	55	42	60	48	80

Who is more intelligent and who is more consistent?

Sol. For Ravi,

x _i	$d_i = x_i - 45$	d ²
25	-20	400
50	5	25
45	0	0
30	-15	225
70	25	625
42	-3	9
36	-9	81
48	3	9
35	-10	100
60	15	225
Total	$\Sigma d_i = -14$	$\Sigma d^2_i = 1699$

$$\sigma = \sqrt{\frac{\Sigma d^{2_{i}}}{n} - \left(\frac{\Sigma d_{i}}{n}\right)^{2}}$$
$$= \sqrt{\frac{1699}{10} - \left(\frac{-14}{10}\right)^{2}} = \sqrt{169.9 - 0.0196}$$
$$= \sqrt{169.88} = 13.03$$
$$\overline{x} = A + \frac{\Sigma d_{i}}{\Sigma f_{i}} = 45 - \frac{14}{10} = 43.6$$

Now,

r laorinia,							
	x_i	$d_i = x_i - 55$	<i>d</i> ² _{<i>i</i>}				
	10	-45	2025				
	70	25	625				
	50	-5	25				
	20	-35	1225				
	95	40	1600				
	55	0	0				
	42	-13	169				
	60	5	25				
	48	-7	49				
	80	25	625				
	Total	$\Sigma d_i = 0$	$\Sigma d_i^2 = 6368$				
\therefore	Mean =	=55					
÷	σ =	$\sigma = \sqrt{\frac{6368}{10}} = \sqrt{636.8} = 25.2$					
For Ravi,		$CV = \frac{\sigma}{\overline{x}} \times 100 = \frac{13.03}{43.6} \times 100 = 29.88$					
For Hashi	na, CV	$CV = \frac{\sigma}{\overline{x}} \times 100 = \frac{25.2}{55} \times 100 = 45.89$					

For Hashina,

Hence, Hashina is more consistent and intelligent.

 ${f Q}_{f \cdot}$ ${f 22}$ Mean and standard deviation of 100 observations were found to be 40 and 10, respectively. If at the time of calculation two observations were wrongly taken as 30 and 70 in place of 3 and 27 respectively, then find the correct standard deviation.

Sol. Given,

$$n = 100, \overline{x} = 40, \sigma = 10 \text{ and } \overline{x} = 40$$

 $\therefore \qquad \frac{\Sigma x_i}{n} = 40$
 $\Rightarrow \qquad \frac{\Sigma x_i}{100} = 40$
 $\Rightarrow \qquad \Sigma x_i = 4000$
Now,
 $\therefore \qquad Corrected \Sigma x_i = 4000 - 30 - 70 + 3 + 27$
 $\therefore \qquad = 4030 - 100 = 3930$
Corrected mean $= \frac{2930}{100} = 39.3$

Now,

$$\sigma^{2} = \frac{\Sigma x_{i}^{2}}{n} - (40)^{2}$$

$$\Rightarrow \qquad 100 = \frac{\Sigma x_{i}^{2}}{100} - 1600$$

$$\Rightarrow \qquad \Sigma x_{i}^{2} = 170000$$

Now,
Corrected
$$\Sigma x_i^2 = 170000 - (30)^2 - (70)^2 + 3^2 + (27)^2$$

 $= 164939$
 \therefore
Corrected $\sigma = \sqrt{\frac{164939}{100} - (39.3)^2}$
 $= \sqrt{1649.39 - 39.3 \times 39.3}$
 $= \sqrt{1649.39 - 1544.49}$
 $= \sqrt{104.9} = 10.24$

Q. 23 While calculating the mean and variance of 10 readings, a student wrongly used the reading 52 for the correct reading 25. He obtained the mean and variance as 45 and 16, respectively. Find the correct mean and the variance.

Sol.	Given,	$n=10$, $\overline{x}=45$ and $\sigma^2=16$
	.: .	$\overline{x} = 45 \implies \frac{\Sigma x_i}{D} = 45$
	\Rightarrow	$\frac{\Sigma x_i}{10} = 45 \Longrightarrow \Sigma x_i = 450$
		Corrected $\Sigma x_i = 450 - 52 + 25 = 423$
	.:.	$\overline{x} = \frac{423}{10} = 42.3$
	\Rightarrow	$\sigma^2 = \frac{\Sigma x_i^2}{n} - \left(\frac{\Sigma x_i}{n}\right)^2$
	\Rightarrow	$16 = \frac{\Sigma x_i^2}{10} - (45)^2$
	\Rightarrow	$\Sigma x_i^2 = 10 (2025 + 16)$
	\Rightarrow	$\Sigma x_i^2 = 20410$
	<i>.</i> .	Corrected $\Sigma x_i^2 = 20410 - (52)^2 + (25)^2 = 18331$
	and	corrected $\sigma^2 = \frac{18331}{10} - (42.3)^2 = 43.81$

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Now,

Objective Type Questions

${f Q}$. ${f 24}$ The mean deviation of the data 3, 10, 10, 4, 7, 10, 5 from the mean is

(a) 2	(b) 2.57
(c) 3	(d) 3.75

Sol. (b) Given, observations are 3, 10, 10, 4, 7, 10 and 5.

$\bar{x} = \frac{3 + 10 + 10}{10 + 10}$	$\frac{10+4+7+10+5}{7}$
$=\frac{49}{7}=7$,
x _i	$d_i = \left x_i - \overline{x} \right $
3	4
10	3
10	3
4	3
7	0
10	3
5	2
Total	$\Sigma d_i = 18$
MD =	$\frac{\Sigma d_i}{N} = \frac{18}{7} = 2.57$

Q. 25 Mean deviation for *n* observations $x_1, x_2, ..., x_n$ from their mean \overline{x} is given by

(a)
$$\sum_{i=1}^{n} (x_i - \overline{x})$$

(b) $\frac{1}{n} \sum_{i=1}^{n} |x_i - \overline{x}|$
(c) $\sum_{i=1}^{n} (x_i - \overline{x})^2$
(d) $\frac{1}{n} \sum_{i=1}^{n} (x_i - \overline{x})^2$
Sol. (b) $MD = \frac{1}{n} \sum_{i=1}^{n} |x_i - \overline{x}|$

Q. 26 When tested, the lives (in hours) of 5 bulbs were noted as follows 1357, 1090, 1666, 1494, 1623

The mean deviations (in hours) from their mean is
(a) 178 (b) 179 (c) 220 (d) 356
Sol. (a) Since, the lives of 5 bulbs are 1357, 1090, 1666, 1494 and 1623.

$$\therefore \qquad \text{Mean} = \frac{1357 + 1090 + 1666 + 1494 + 1623}{5}$$

$$= \frac{7230}{5} = 1446$$

x_i	$\boldsymbol{d}_i = \left x_i - \overline{x} \right $			
1357	89			
1090	356			
1666	220			
1494	48			
1623	177			
Total	$\Sigma d_i = 890$			
$MD = \frac{\Sigma d_i}{N} = \frac{890}{5} = 178$				

Q. 27 Following are the marks obtained by 9 students in a mathematics test 50, 69, 20, 33, 53, 39, 40, 65, 59

The mean deviation from the median is

(a) 9	(b) 10.5
(c)12.67	(d) 14.76

Sol. (c) Since, marks obtained by 9 students in Mathematics are 50, 69, 20, 33, 53, 39, 40, 65 and 59.

Rewrite the given data in ascending order.

	20,33, 39, 40, 5	0, 53, 59, 65, 69,	
Here,	<i>n</i> = 9		[odd]
	Median = $\left(\frac{9}{1000}\right)$	Median = $\left(\frac{9+1}{2}\right)$ term = 5th term	
	Me = 50		
	x _i	$d_i = x_i - Me $	
	20	30	
	33	17	
	39	11	
	40	10	
	50	0	
	53	3	
	59	9	
	65	15	
	69	19	
	N = 2	$\Sigma d_i = 114$	
	$MD = \frac{114}{9} = 12.67$	7	

Q. 28 The standard deviation of data 6, 5, 9, 13, 12, 8 and 10 is

(a) $\sqrt{\frac{52}{7}}$	(b) $\frac{52}{7}$
(c) $\sqrt{6}$	(d) 6

x_{i}	x_i^2
6	36
5	25
9	81
13	169
12	144
8	64
10	100
$\Sigma \boldsymbol{x}_i = 63$	$\Sigma x_i^2 = 619$
$SD = \sigma = \sqrt{\frac{\Sigma x_i^2}{N} - \left(\frac{\Sigma x_i^2}{N}\right)^2}$	$\frac{\overline{x_i}}{\sqrt{7}} = \sqrt{\frac{619}{7} - \left(\frac{63}{7}\right)^2}$
$=\sqrt{\frac{7 \times 619 - 3969}{49}}$	
$=\sqrt{\frac{4333-3969}{49}}$	
$=\sqrt{\frac{364}{49}}=\sqrt{\frac{52}{7}}$	

Sol. (*a*) Given, data are 6, 5, 9, 13, 12, 8, and 10.

Q. 29 If $x_1, x_2, ..., x_n$ be *n* observations and \overline{x} be their arithmetic mean. Then, formula for the standard deviation is given by

(a) $\Sigma(x_i - \overline{x})^2$ (b) $\frac{\Sigma(x_i - \overline{x})^2}{n}$ (c) $\sqrt{\frac{\Sigma(x_i - \overline{x})^2}{n}}$ (d) $\sqrt{\frac{\Sigma x_i^2}{n} + \overline{x}^{-2}}$ D is given by

Sol. (c) SD is given by

:..

$$\sigma = \sqrt{\frac{\Sigma(x_i - \overline{x})^2}{n}}$$

Q. 30 If the mean of 100 observations is 50 and their standard deviation is 5, than the sum of all squares of all the observations is

	(a) 50000 (c) 252500	(b) 250000 (d) 255000
Sol.	(c) Given,	\overline{x} =50, n = 100 and σ = 5
		$\sum x_i^2 = ?$
	÷	$\overline{x} = \frac{\Sigma x_i}{\overline{x}}$
	⇒	$50 = \frac{\sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{i=1}^{n} \sum_{i=1}^{n} \sum_{i=1}^{n} \sum_{j=1}^{$
	÷	$\Sigma x_i = 50 \times 100 = 5000$

Now,

$$\sigma = \sqrt{\frac{\Sigma x_i^2}{n} - \left(\frac{\Sigma x_i}{n}\right)^2} \Rightarrow \sigma^2 = \frac{\Sigma x_i^2}{n} - (\overline{x})^2$$

$$\Rightarrow \qquad 25 = \frac{\Sigma x_i^2}{100} - (50)^2 \Rightarrow 25 = \frac{\Sigma x_i^2}{100} - 2500$$

$$\Rightarrow \qquad 2525 = \frac{\Sigma x_i^2}{100}$$

$$\therefore \qquad \Sigma x_i^2 = 252500$$

Q. 31 If *a*, *b*, *c*, *d* and *e* be the observations with mean *m* and standard deviation *s*, then find the standard deviation of the observations a + k, b + k, c + k, d + k and e + k is

(a) s (b) ks (c) s + k (d)
$$\frac{3}{k}$$

Sol. (a) Given observations are a, b, c, d and e.
Mean = $m = \frac{a+b+c+d+e}{5}$
 $\Sigma x_i = a+b+c+d+e = 5m$
Now, mean = $\frac{a+k+b+k+c+k+d+k+e+k}{5}$
 $= \frac{(a+b+c+d+e)+5k}{5} = m+k$
 \therefore SD = $\sqrt{\frac{\Sigma(x_i+k)^2}{5} - (m+k)^2}$

$$=\frac{(2 + b + c + a + e) + 5k}{5} = m + k$$

$$SD = \sqrt{\frac{\Sigma(x_i + k)^2}{n} - (m + k)^2}$$

$$= \sqrt{\frac{\Sigma(x_i^2 + k^2 + 2k x_i)}{n} - (m^2 + k^2 + 2mk)}$$

$$= \sqrt{\frac{\Sigma x_i^2}{n} - m^2 + \frac{2k\Sigma x_i}{n} - 2mk}$$

$$= \sqrt{\frac{\Sigma x_i^2}{n} - m^2 + 2km - 2mk}$$

$$= \sqrt{\frac{\Sigma x_i^2}{n} - m^2}$$

$$= s$$

Q. 32 If x_1 , x_2 , x_3 , x_4 and x_5 be the observations with mean m and standard deviation s then, the standard deviation of the observations kx_1 , kx_2 , kx_3 , kx_4 and kx_5 is

(a)
$$k + s$$

(b) $\frac{s}{k}$
(c) ks
(d) s
Sol. (c) Here,
 $m = \frac{\Sigma x_i}{5}, s = \sqrt{\frac{\Sigma x_i^2}{5} - \left(\frac{\Sigma x_i}{5}\right)^2}$
 \therefore
 $SD = \sqrt{\frac{k^2 \Sigma x_i^2}{5} - \left(\frac{k\Sigma x_i}{5}\right)^2}$
 $= \sqrt{\frac{k^2 \Sigma x_i^2}{5} - k^2 \left(\frac{\Sigma x_i}{5}\right)^2} = \sqrt{\left(\frac{\Sigma x_i^2}{5}\right) - \left(\frac{\Sigma x_i}{5}\right)^2} = ks$

Q. 33 Let $x_1, x_2, ..., x_n$ be *n* observations. Let $w_i = lx_i + k$ for i = 1, 2, ..., n, where l and k are constants. If the mean of x_i 's is 48 and their standard deviation is 12, the mean of w_i 's is 55 and standard deviation of w_i 's is 15, then the value of *l* and *k* should be

(a) $l = 1.25, k = -5$	(b) $l = -1.25, k = 5$
(c) $l = 2.5, k = -5$	(d) $l = 2.5, k = 5$

Sol. (a) Given, $w_i = x_i + k$, $\overline{x_i} = 48$, $sx_i = 12$, $w_i = 55$ and $sw_i = 15$ Then, $\overline{W}_i = \overline{x}_i + k$ [where, \overline{w}_i is mean w_i 's and \overline{x}_i is mean of x_i 's] 55 = 48 + k \Rightarrow

Now,
SD of
$$w_i = SD$$
 of x_i
 \Rightarrow
 $15 = 12$
 \Rightarrow
 $l = \frac{15}{12}$
 $= 1.25$
From Eqs. (i) and (ii),
 $k = 55 - 1.25 \times 48$
 $= -5$

 ${f Q}$. ${f 34}$ The standard deviations for first natural numbers is

(a) 5.5 (b) 3.87 (c) 2.97 (d) 2.87 **Sol.** (d) We know that, SD of first n natural number = $\sqrt{\frac{n^2 - 1}{12}}$:. SD of first 10 natural numbers = $\sqrt{\frac{(10)^2 - 1}{12}}$ $=\sqrt{\frac{100-1}{12}}=\sqrt{\frac{99}{12}}=\sqrt{8.25}=2.87$

 $igcup_{ullet}$ $m{35}$ Consider the numbers 1, 2, 3, 4, 5, 6, 7, 8, 9, and 10. If 1 is added to each number the variance of the numbers, so obtained is (a) 6.5 (b) 2.87 (c) 3.87 (d) 8.25

Sol. (d) Given numbers are 1, 2, 3, 4, 5, 6, 7, 8, 9 and 10. If 1 is added to each number, then observations will be 2, 3, 4, 5, 6, 7, 8, 9, 10 and 11. $\Sigma x_i = 2 + 3 + 4 + \dots + 11$ *:*..

and

$$= \frac{10}{2} [2 \times 2 + 9 \times 1] = 5[4 + 9] = 65$$

$$\Sigma x_i^2 = 2^2 + 3^2 + 4^2 + 5^2 + \dots + 11^2$$

$$= (1^2 + 2^2 + 3^2 + \dots + 11^2) - (1^2)$$

$$= \frac{11 \times 12 \times 23}{6} - 1$$

$$= \frac{11 \times 12 \times 23 - 6}{6} = 505$$

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...(i)

$$s^{2} = \frac{\Sigma x_{i}^{2}}{n} - \left(\frac{\Sigma x_{i}}{n}\right)^{2} = \frac{505}{10} - \left(\frac{65}{10}\right)^{2}$$
$$= 50.5 - (6.5)^{2}$$
$$= 50.5 - 42.25$$
$$= 8.25$$

Q. 36 Consider the first 10 positive integers. If we multiply each number by -1 and, then add 1 to each number, the variance of the numbers, so obtained is

Sol. (*a*) Since, the first 10 positive integers are1, 2, 3, 4, 5, 6, 7, 8, 9 and 10.

On multiplying each number by -1, we get
-1, -2, -3, -4, -5, -6, -7, -8, -9, -10
On adding 1 in each number, we get
0, -1, -2, -3, -4, -5, -6, -7, -8, -9

$$\therefore$$
 $\Sigma x_i = 0 - 1 - 2 - 3 - 4 - 5 - 6 - 7 - 8 - 9$
 $= -\frac{9 \times 10}{2}$
and $\Sigma x_i^2 = 0^2 + (-1)^2 + (-2)^2 + ... + (-9)^2$
 $= \frac{9 \times 10 \times 19}{6}$
 $= 285$
 \therefore $SD = \sqrt{\frac{285}{10} - (\frac{-45}{10})^2} = \sqrt{\frac{285}{10} - \frac{2025}{100}}$
 $= \sqrt{\frac{2850 - 2025}{100}} = \sqrt{8.25}$
Now, variance = $(SD)^2 = (\sqrt{8.25})^2 = 8.25$

Q. 37 The following information relates to a sample of size 60, $\Sigma x^2 = 18000$, and $\Sigma x = 960$. Then, the variance is

- (a) 6.63 (b) 16 (c) 22 (d) 44 **Sol.** (d) Variance $= \frac{\Sigma x_i^2}{n} - \left(\frac{\Sigma x_i}{n}\right)^2$ $= \frac{18000}{60} - \left(\frac{960}{60}\right)^2 = 300 - 256 = 44$
- Q. 38 If the coefficient of variation of two distributions are 50, 60 and their arithmetic means are 30 and 25 respectively, then the difference of their standard deviation is

(a) 0	(b) 1
(c) 1.5	(d) 2.5
Sol. (a) Here	$CV_1 = 50$, $CV_2 = 60$, $\bar{x}_1 = 30$ and $\bar{x}_2 = 25$

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$$\therefore \qquad CV_1 = \frac{\sigma_1}{\overline{x}_1} \times 100 \implies 50 = \frac{\sigma_1}{30} \times 100$$

$$\therefore \qquad \sigma_1 = \frac{30 \times 50}{100} = 15 \text{ and } CV_2 = \frac{\sigma_2}{\overline{x}_2} \times 100$$

$$\implies \qquad 60 = \frac{\sigma_2}{25} \times 100$$

$$\therefore \qquad \sigma_2 = \frac{60 \times 25}{100} = 15$$

Now,
$$\sigma_1 - \sigma_2 = 15 - 15 = 0$$

Q. 39 The standard deviation of some temperature data in °C is 5. If the data were converted into °F, then the variance would be

(a) 81 (b) 57 (c) 36 (d) 25
Sol. (a) Given,

$$\sigma_C = 5 \implies \frac{5}{9}(F - 32) = C$$

 $F = \frac{9C}{5} + 32$
 $\sigma_F = \frac{9}{5}\sigma_C = \frac{9}{5} \times 5 = 9$
Here,
 $\sigma_F^2 = (9)^2 = 81$

Fillers

Q. 40 Coefficient of variation = $\frac{\dots}{\text{Mean}} \times 100$

Sol. $CV = \frac{SD}{Mean} \times 100$

Sol. If \overline{x} is the mean of *n* values of *x*, then $\sum_{i=1}^{n} (x_i - \overline{x}) = 0$ and if *a* has any value other than \overline{x} , then $\sum_{i=1}^{n} (x_i - \overline{x})^2$ is less than $\sum (x_i - a)^2$.

- Q. 42 If the variance of a data is 121, then the standard deviation of the data is
- **Sol.** If the variance of a data is 121. Then,

 $SD = \sqrt{Variance} \\ = \sqrt{121} = 11$

- **Q. 43** The standard deviation of a data is of any change in origin but is of change of scale.
- **Sol.** The standard deviation of a data is independent of any change in origin but is dependent of change of scale.
- **Q. 44** The sum of squares of the deviations of the values of the variable is when taken about their arithmetic mean.
- **Sol.** The sum of the squares of the deviations of the values of the variable is minimum when taken about their arithmetic mean.
- Q. 45 The mean deviation of the data is when measured from the median.
- Sol. The mean deviation of the data is least when measured from the median.
- **Q. 46** The standard deviation is to the mean deviation taken from the arithmetic mean.
- **Sol.** The SD is greater than or equal to the mean deviation taken from the arithmetic mean.