# Construction of Polygons

#### • Construction of quadrilateral when one angle and four sides are given:

# **Example:**

Construct a quadrilateral PQRS with PQ = 6 cm, QR = 7 cm, RS = 8.5 cm, PS = 6.5 cm and  $\angle Q = 90^{\circ}$ .

#### **Solution:**

**Step 1:** Draw line segment PQ of length 6 cm.

**Step 2:** Draw  $\angle XQP = 90^{\circ}$  at point Q.

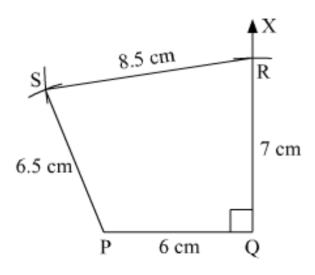
**Step 3:** Taking Q as centre and 7 cm as radius, mark an arc on QX and name the point of intersection as R.

**Step 4:** Taking R as centre and 8.5 cm as radius, mark an arc.

**Step 5:** Taking P as centre and 6.5 cm as radius, mark an arc. Let it intersect the previous arc at point S.

Step 6: Join PS and RS.

PQRS is the required quadrilateral.



# • Construction of a quadrilateral when three sides and two included angles are given

# **Example:**

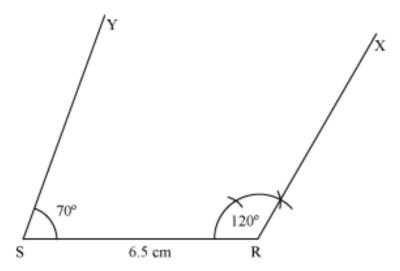
Construct a quadrilateral PQRS with SR = 6.5 cm, PS = 5 cm, QR = 3 cm,  $\angle$ R = 120°, and  $\angle$ S = 70°.

### **Solution:**

The steps of construction are as follows:

# Step 1:

Draw SR = 6.5 cm. Draw  $\angle SRX = 120^{\circ}$  at R and  $\angle RSY = 70^{\circ}$  at S.

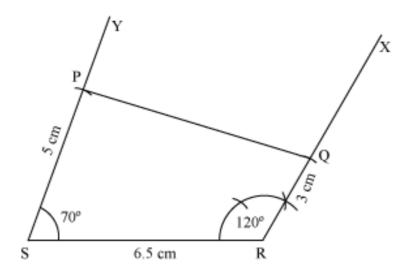


# Step 2:

With S as centre, draw an arc of radius 5 cm intersecting SY at P.

With R as centre, draw an arc of radius 3 cm intersecting RX at Q.

Join PQ to obtain the required quadrilateral PQRS.



- A unique quadrilateral can be constructed, if any five measurements of the quadrilateral are given.
- Construction of a quadrilateral when four sides and a diagonal are given:

### **Example:**

Construct a quadrilateral WXYZ, where WX = 4.5 cm, XY = 5 cm, YZ = 5.5 cm, ZW = 3 cm, and WY = 6 cm.

#### **Solution:**

## Step 1:

Draw a line WY of length 6 cm. Draw an arc of radius 4.5 cm with W as centre and another arc of length 5 cm with Y as centre. The intersection of the two arcs will be the point, X.

Join WX and XY.

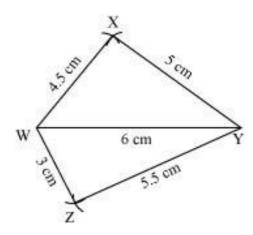
# **Step 2:**

The point, Z, will be on the opposite side of point X with respect to WY.

Draw an arc of length 3 cm taking W as centre and another arc of length 5.5 cm taking Y as centre. The intersection of these arcs will be the point, Z.

Join WZ and YZ.

WXYZ is the required quadrilateral.



# • Construction of a quadrilateral when two diagonals and three sides are given

# **Example:**

Construct a quadrilateral PQRS, where PR = 7 cm, QS = 8 cm, PQ = 5 cm, QR = 5 cm, and PS = 5.5 cm.

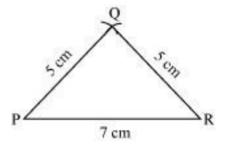
#### **Solution:**

The steps of constructing quadrilateral PQRS are as follows:

# Step 1:

Draw a line PR of length 7 cm. Draw an arc of radius 5 cm taking P as centre and an arc of radius 5 cm taking R as centre. The point of intersection of these two arcs will be the point, Q.

Join PQ and RQ.

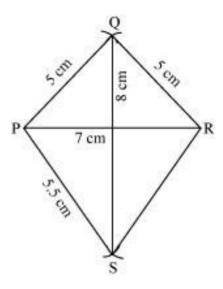


# Step 2:

With Q as centre, draw an arc of radius 8 cm. The point, S, will lie on this arc.

Then, taking P as centre, draw an arc of radius 5.5 cm. The intersection point of the two arcs will be the point, S.

Join PS and RS.



PQRS is the required quadrilateral.

# **Construction of Parallelograms**

Type: 1 To construct a parallelogram, whose two consecutive sides and the included angle are given.

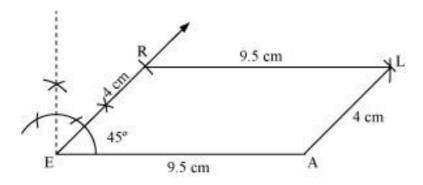
Let a parallelogram REAL has RE = 4 cm, EA = 9.5 cm, and  $m \angle$  REA = 45°.

The steps of construction for this figure are as follows:

**Step 1** Draw a line segment EA of 9.5 cm and an angle of 45° at point E. As vertex R is 4 cm away from vertex E, cut a line segment EA of 4.5 cm on this ray.

**Step 2** Vertex L is 9.5 cm and 4 cm away from vertices R and A respectively. By taking radius as 9.5 cm and 4 cm, draw arcs from point R and A respectively. These will be intersecting each other at point L.

**Step 3** Join L to R and A.



REAL is the required parallelogram.

# Type: 2 To construct a parallelogram, whose one side and both the diagonals are given.

Let a parallelogram STAR has TA = 7 cm, AS = 13 cm, and TR = 15 cm.

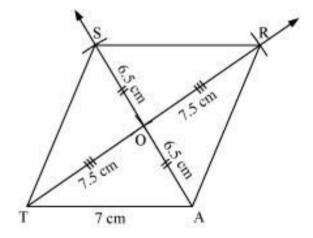
The steps of construction for this figure are as follows:

**Step 1**  $\triangle$ OTA can be constructed by using the given measurements as:

**Step 2.** Vertex TR is on the line joining TO and it is 7.5 cm from point O. Therefore, extend line segment TO and draw an arc of radius OT = 7.5 cm, taking centre as O that cuts ray TO at point R.

**Step 3** Extend line segment AO and draw an arc of radius OA = 6.5 cm, taking centre as O that cuts ray AO at point S.

Step 4 Join AR, RS, and ST.



STAR is the required parallelogram.

# Type: 3 To construct a parallelogram, whose two consecutive sides and one diagonal is given.

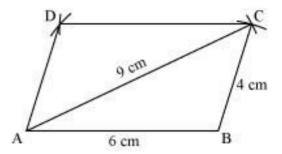
Let a parallelogram has adjacent sides of measures 6 cm and 4 cm and one diagonal of measure 9 cm.

The steps of construction for this figure are as follows:

**Step 1:** Draw line segment AB of length 6 cm. With A and B as centres, and radii 9 cm and 4 cm respectively, draw arcs intersecting each other at C.

**Step 2:** Taking C and A as centres and radii 6 cm and 4 cm respectively, draw arcs intersecting each other at D.

Step 3: Join AD and CD.



ABCD is the required parallelogram.

# Type: 4 To construct a parallelogram, whose two diagonals and included angle are given.

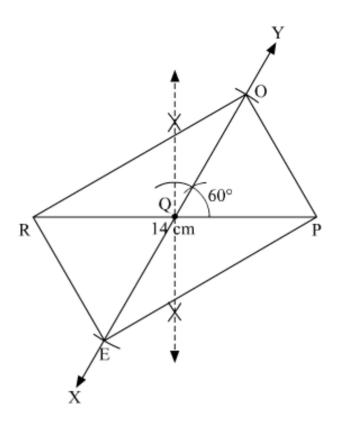
Let parallelogram ROPE has diagonals RP = 12 cm and EO = 14 cm amd the acute angle between the diagonals is  $60^{\circ}$ .

**Step 1:** Draw RP = 14 cm. Then draw perpendicular bisector of RP to get the midpoint Q.

**Step 2:** Draw line XY, such that angle  $YQP = 60^{\circ}$ .

**Step : 3** From line XY, cut QO = EO2=122=6 cm and QE = EO2=122=6 cm.

Step: 4 Join RO, OP, PE and ER.



Type: 5 To construct a parallelogram, whose two adjacent sides and height are given.

Let parallelogram ROPE has diagonals RP = 12 cm and EO = 14 cm amd the acute angle between the diagonals is  $60^{\circ}$ .

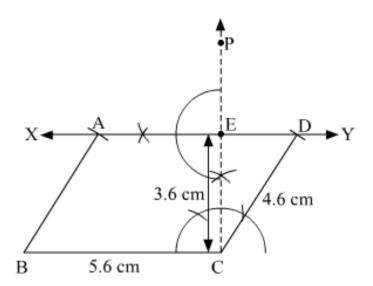
**Step : 1** Draw BC = 5.6 cm. Then draw perpendicular at C. CP is perpendicular to BC.

Step: 2 From CP, cut 3.6 cm, i.e height of the parallelogram.

**Step: 3** Through E, draw perpendicular to CP to get XY parallel to BC.

**Step: 4** With B as a centre and radius 4.6 cm, draw an arc which cuts XY at A.

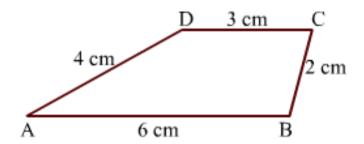
**Step: 5** With C as a centre and radius 4.6 cm, draw one more arc which cuts XY at D.



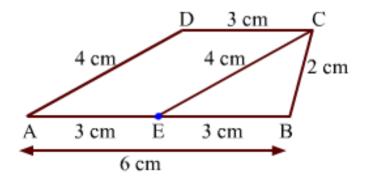
## • Construction of a trapezium when measures of all the sides are given:

Let us construct a trapezium ABCD, in which AB = 6 cm, BC = 2 cm, CD = 3 cm, DA = 4 cm.

Rough sketch:.



A suitable point, E, is marked on AB (EB = AB – CD), so as to draw a line segment, EC, parallel to AD. AECD becomes a parallelogram.



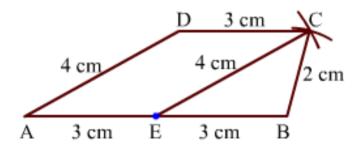
$$\therefore$$
 EC = AD = 4 cm

Also, 
$$EB = AB - CD = 6 \text{ cm} - 3 \text{ cm} = 3 \text{ cm}$$

$$\therefore$$
 AE = 3 cm

The trapezium, ABCD, can be constructed by following the given steps of construction:

- 1) Draw a line segment, AB, of length 6 cm as the bottom side of the trapezium. Then, mark a point, E, at a distance of 3 cm from its right end such that EB is of length 3 cm.
- 2) Taking E and B as the centres and radii as 4 cm and 2 cm respectively, draw arcs intersecting each other at point C. Join EC and BC.
- 3) Draw a line segment, DC, of length 3 cm, parallel to the bottom line, AB, through the top vertex of  $\Delta ECB$ .
- 4) Join AD.

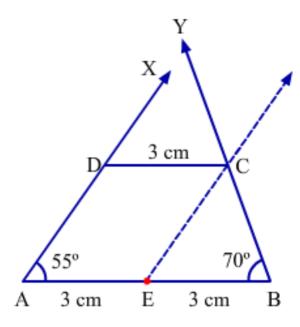


• Construction of a trapezium when the measures of parallel sides and the angles on the longer side are given:

To construct a trapezium, in which AB = 6 cm,  $\angle$ A = 55°,  $\angle$ B = 70°, CD = 3 cm, we need to follow the given steps:

- 1) Draw a line segment, AB, of length 6 cm as the bottom side of the trapezium. Then, mark a point, E, at a distance of 3 cm from its right end such that EB is of length 3 cm.
- 2) Draw  $\angle BAX = 55^{\circ}$  and  $\angle ABY = 70^{\circ}$  at points A and B respectively.
- 3) Draw a ray parallel to ray AX from point E such that it intersects ray BY at point C.

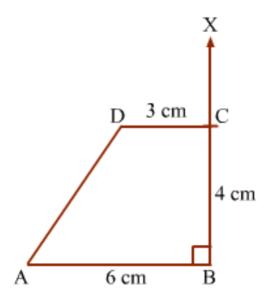
4) Draw a line segment from point C, parallel to the bottom line, AB, which intersects the ray AX at point D.



• Construction of a trapezium when measures of three sides and one included angle are given:

To construct a trapezium, ABCD, AB = 6 cm, CD = 3 cm, BC = 4 cm and  $\angle$ ABC = 90°, we need to follow the given steps:

- 1) Draw a line segment, AB, of length 6 cm as the bottom side of the trapezium.
- 2) Draw  $\angle ABX = 90^{\circ}$  at point B.
- 3) Taking B as the centre and radius 4 cm, draw an arc on ray BX and name the point of intersection as C.
- 4) From point C, draw a line segment CD parallel to the bottom line segment, AB, of length 3 cm.
- 5) Join AD.

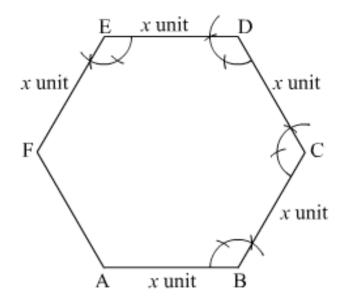


## • Construction of regular hexagon:

- We can construct a regular hexagon by making use of any of the following rules relating to a regular hexagon:
  - (1) Each interior angle of a regular hexagon =  $120^{\circ}$
- (2) Length of a side of a regular hexagon = Radius of its circumcircle
- To construct the regular hexagon ABCDEF of side x unit using the first rule, i.e., each interior angle of a regular hexagon is equal to  $120^{\circ}$ .

The steps of construction are as follows:

- (1) Draw AB of length x unit.
- (2) At B, draw  $\angle ABC = 120^{\circ}$ , where BC = x unit.
- (3) At C, draw  $\angle BCD = 120^{\circ}$ , where CD = x unit.
- (4) At D, draw  $\angle CDE = 120^{\circ}$ , where DE = x unit.
- (5) At E, draw  $\angle DEF = 120^{\circ}$ , where EF = x unit. Join AF.

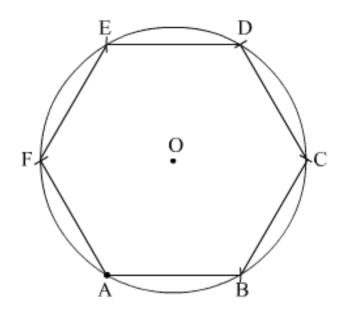


ABCDEF is the required regular hexagon of side *x* unit.

• To construct a regular hexagon using the second rule, i.e., the length of a side of a regular hexagon is equal to the radius of its circumcircle.

The steps of construction are as follows:

- (1) Draw a circle of radius x unit.
- (2) Take any point A on its circumference. With A as the centre and radius as x unit, draw two arcs to cut the circle at points B and F.
- (3) With B as the centre and radius as x unit, draw an arc that cuts the circle at point C.
- (4) With C as the centre and radius as x unit, draw an arc that cuts the circle at point D.
- (5) With D as the centre and radius as x unit, draw an arc that cuts the circle at point E.
- (6) Join AB, BC, CD, DE, EF and AF.



ABCDEF is the required regular hexagon of side x unit.

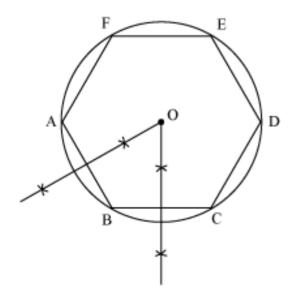
### • Construction of circumcircle of a regular hexagon:

Following are the steps of construction of circumcircle of a regular hexagon ABCDEF.

**Step 1:** Construct a regular hexagon of side *x* unit.

**Step 2:** Draw perpendicular bisectors of sides AB and BC. Let them intersect at a point O.

Step 3: With O as centre and radius equal to OA, draw a circle.



This circle touches all the vertices A, B, C, D, E, and F of the regular hexagon ABCDEF. Hence, it is the required circumcircle of the regular hexagon.

# • Construction of incircle of a regular hexagon:

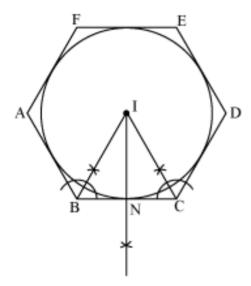
Following are the steps of construction of incircle of a regular hexagon ABCDEF.

**Step 1:** Construct a regular hexagon of side *x* unit.

**Step 1:** Draw the bisectors of  $\angle B$  and  $\angle C$ . Let them meet at point I.

**Step 2:** From I, draw IN perpendicular to BC.

**Step 3:** Taking I as centre and radius equal to IN, draw a circle.



This circle touches each side of regular hexagon ABCDEF. Hence, it is the required incircle.